

Black Hole Superradiance of Self-Interacting Scalar Fields

Marios Galanis

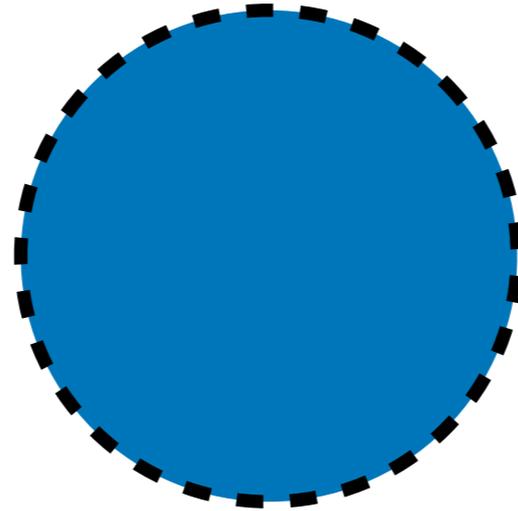
Stanford University

07/30/2021

Based on Phys. Rev. D **103**, 095019, with M. Baryakhtar, R. Lasenby and O. Simon (2021)

CHEW 2021

How to spin down a rotating cylinder

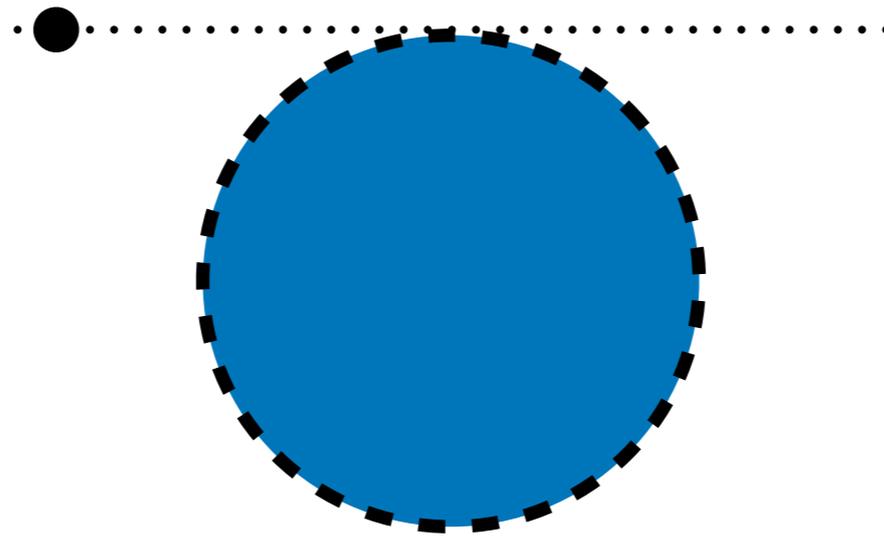


How to spin down a rotating cylinder

Simple: throw a slow ball tangentially to it

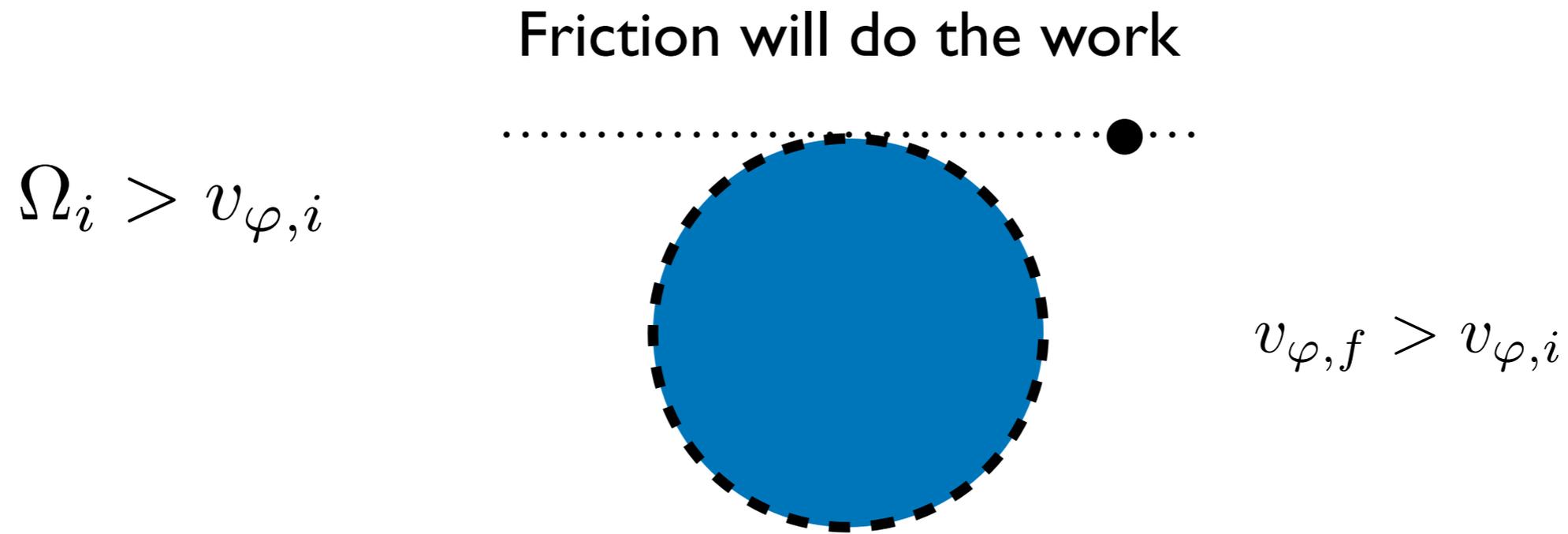
Friction will do the work

$$\Omega_i > v_{\varphi,i}$$



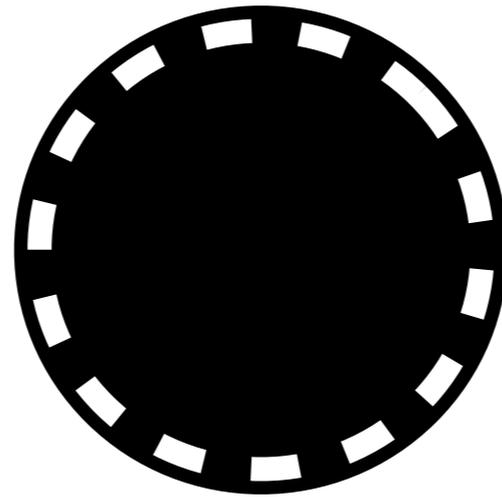
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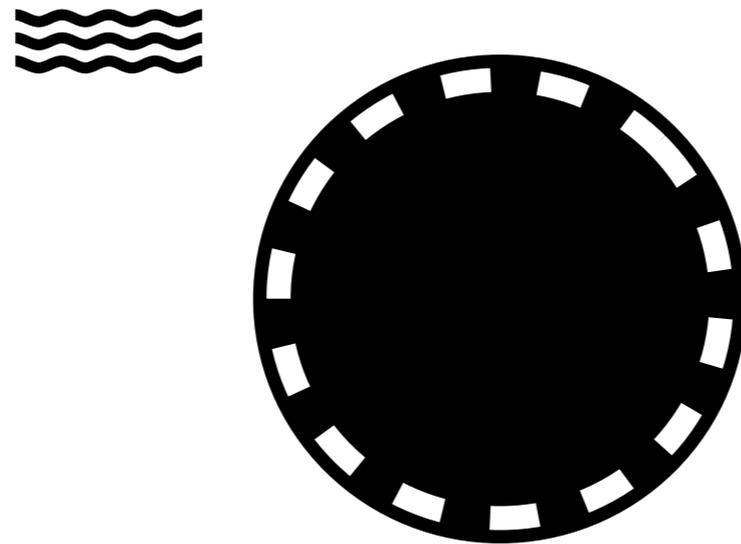
The ball **extracted energy** and **angular momentum** from the cylinder

How to spin down a Black Hole



How to spin down a Black Hole

With waves $\propto e^{-i\omega t + im\phi}$ $v_{\varphi,i} < \Omega_i \rightarrow \omega/m < \Omega$

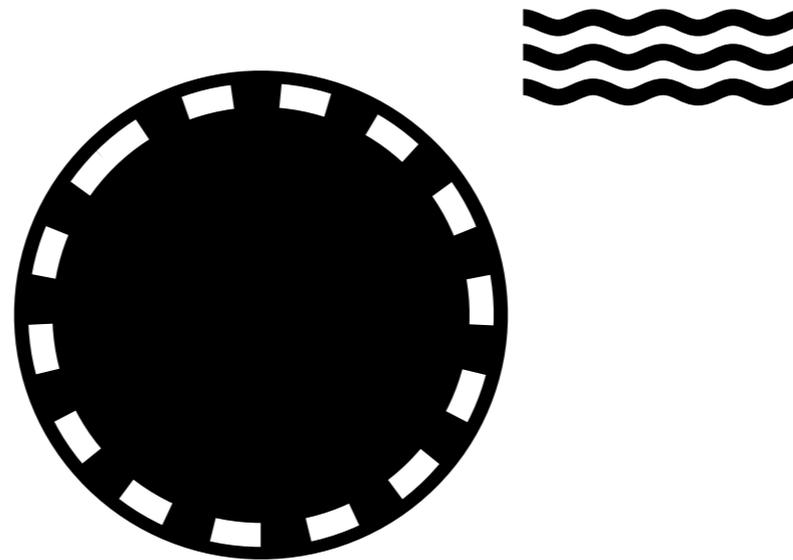


Zeldovich '71; Zeldovich '72;
Starobinski '73

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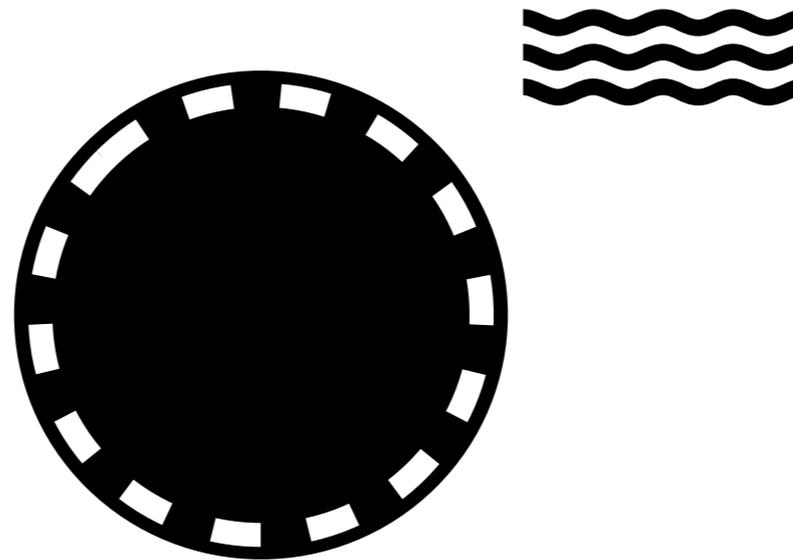
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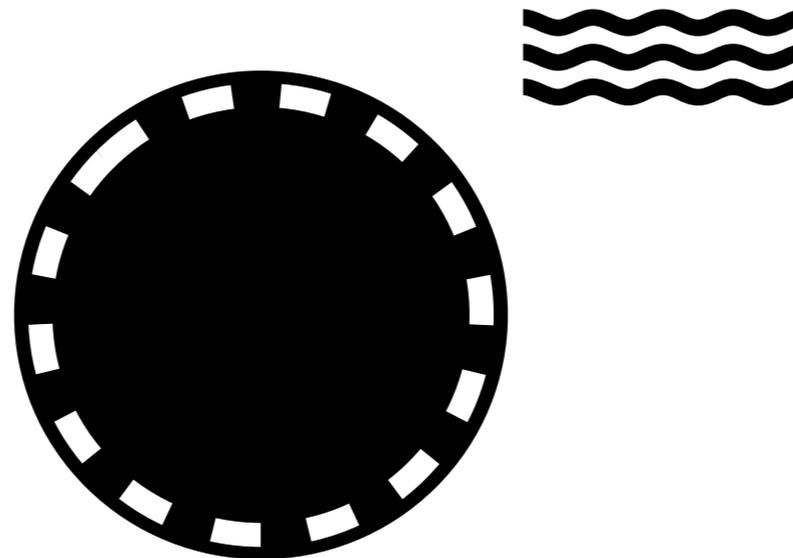


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But what plays the role of friction here?

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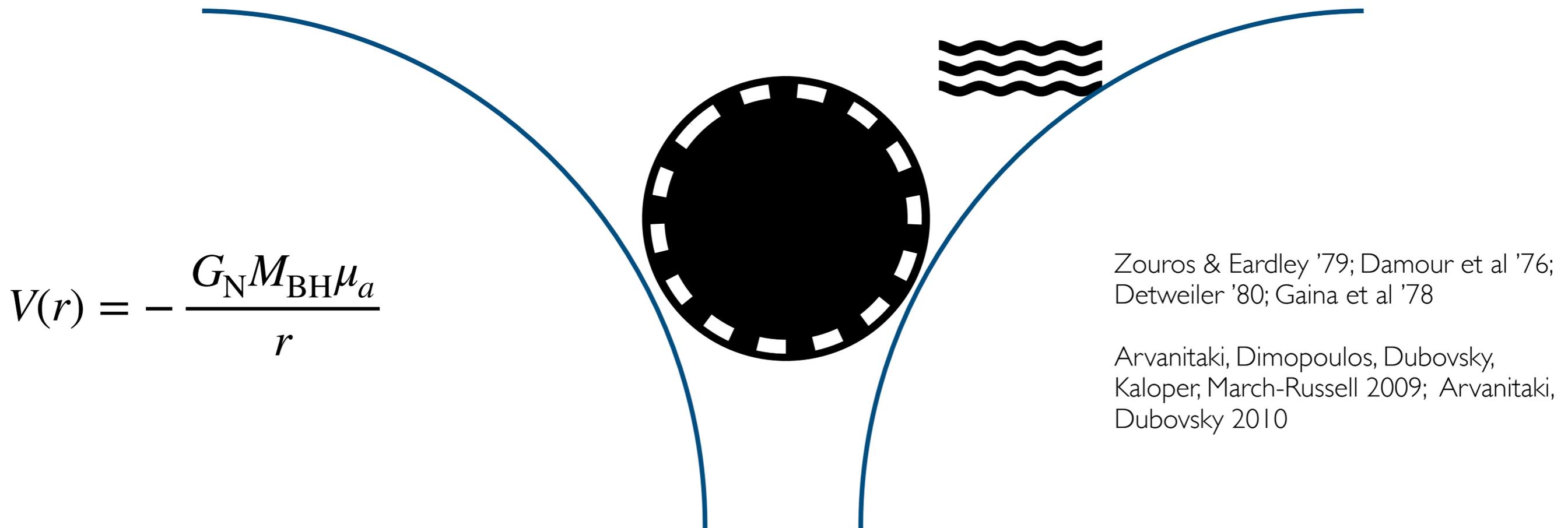
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But what plays the role of friction here?

The absorbing horizon

How to spin down a Black Hole

What if I make the wave bound?

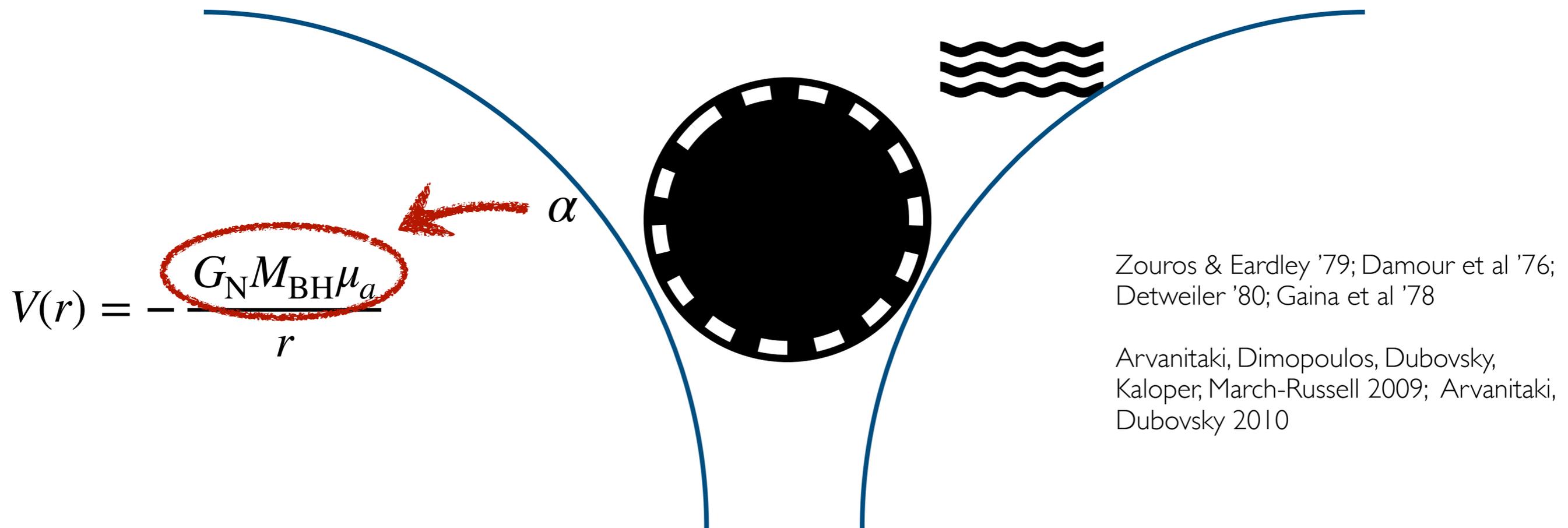


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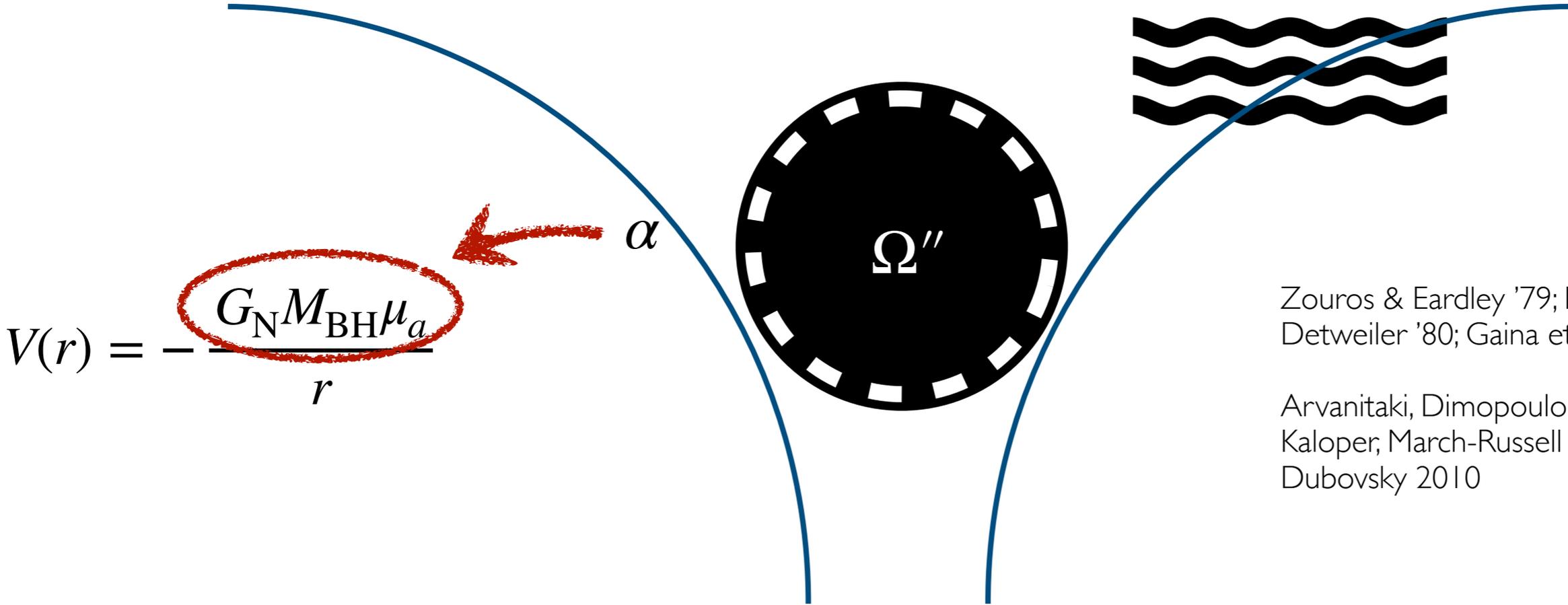
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$$\Omega'' = \omega/m$$



Zouros & Eardley '79; Damour et al '76; Detweiler '80; Gaina et al '78

Arvanitaki, Dimopoulos, Dubovsky, Kaloper, March-Russell 2009; Arvanitaki, Dubovsky 2010

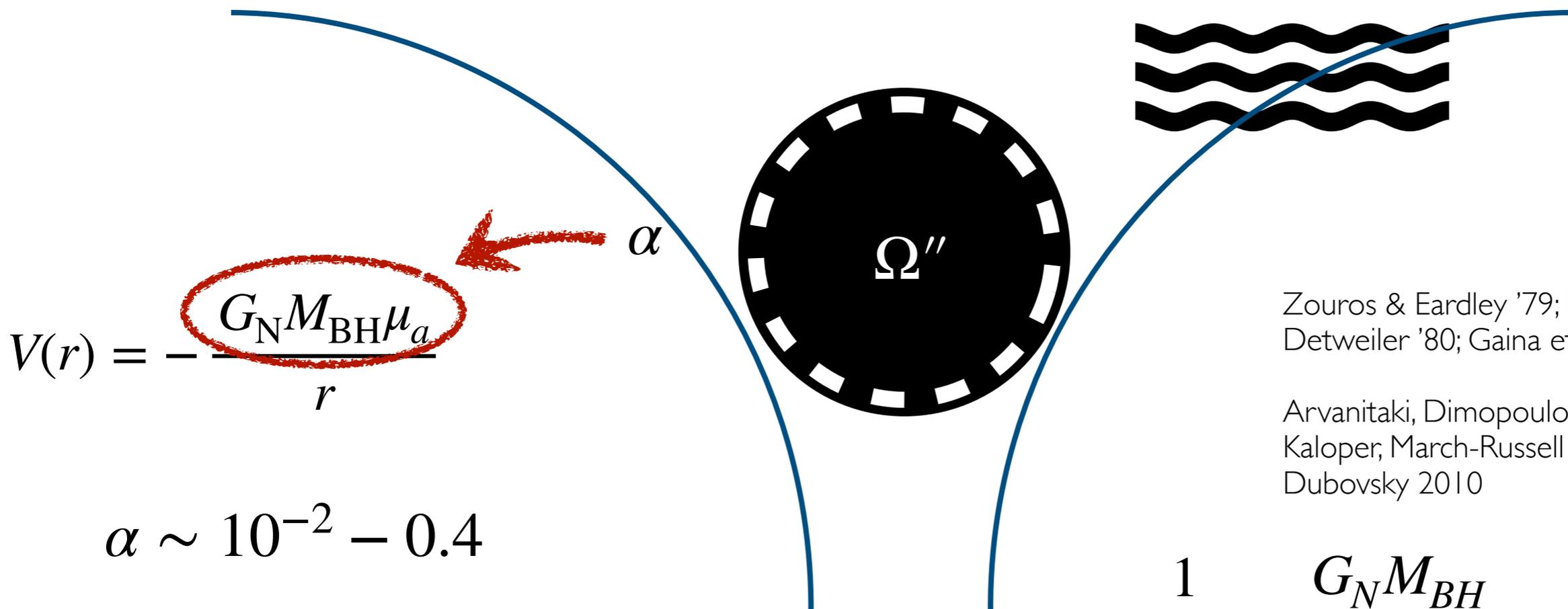
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$$V(r) = - \frac{G_N M_{BH} \mu_a}{r}$$

$$\alpha \sim 10^{-2} - 0.4$$

Bohr Radius

Energy Levels

Growth Rates (Scalar)

Zouros & Eardley '79; Damour et al '76;
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$$a_0 = \frac{1}{\mu_a \alpha} = \frac{G_N M_{BH}}{\alpha^2}$$

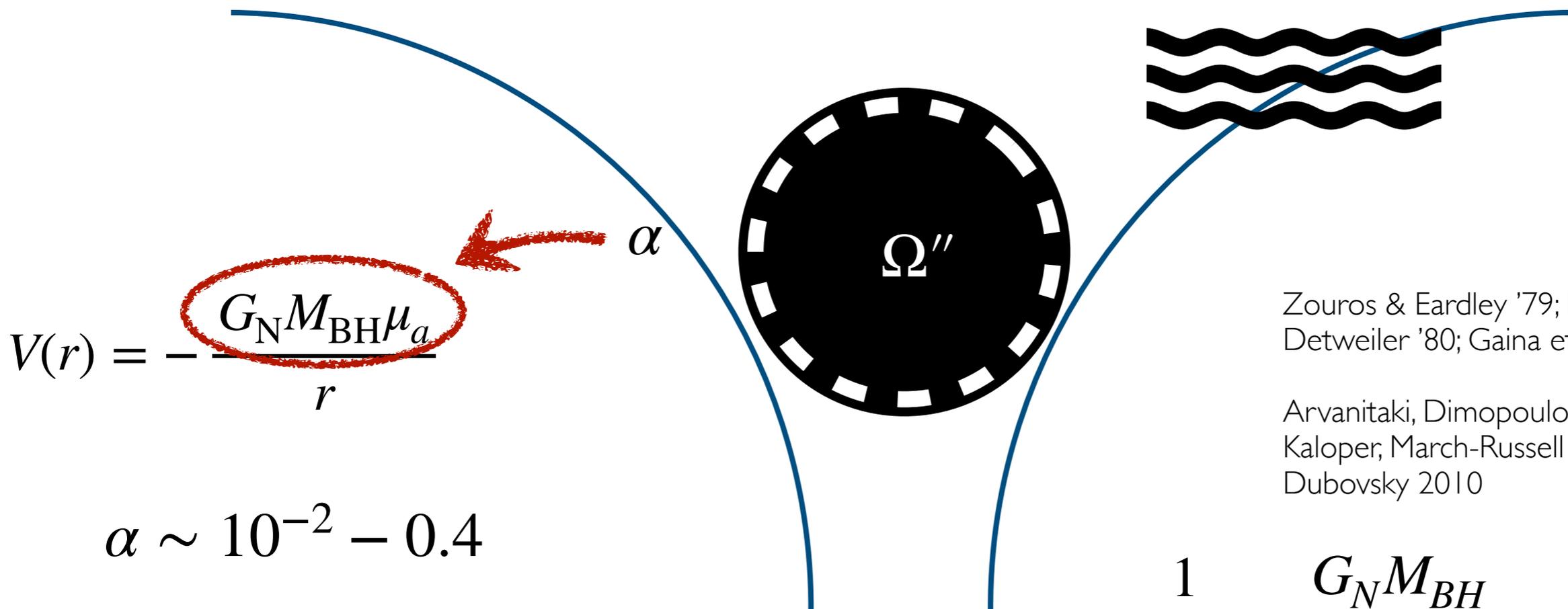
$$E_{n\ell m} = \mu_a \left(1 - \frac{\alpha^2}{2n^2} \right)$$

$$\Gamma_{n\ell m} \propto \mu_a \alpha^{4\ell+4} (m\Omega - \omega)$$

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Numbers to have in mind

$$\Omega > \omega/m$$

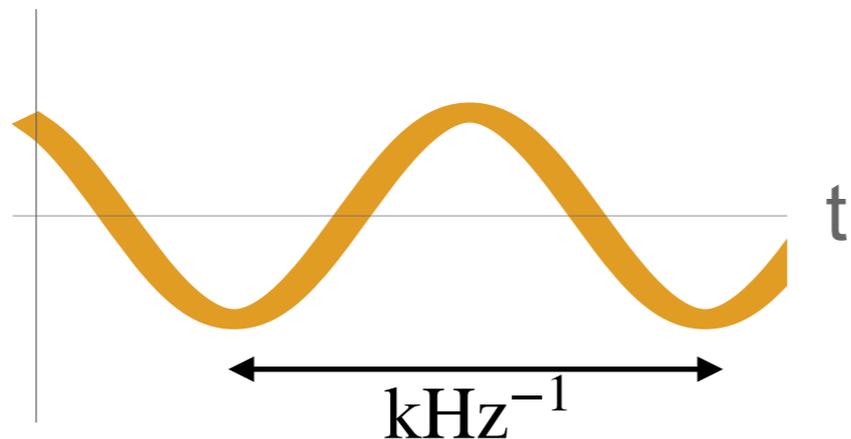


black hole ($30 M_{\odot}$)

100 km

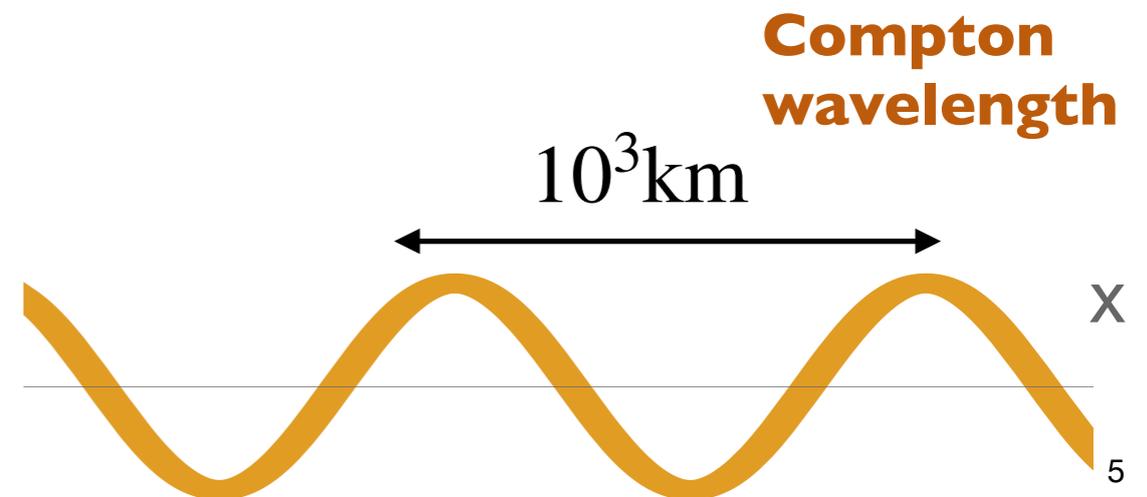
$$\alpha = \mu_a G_N M_{BH} \sim 0.22$$

for a 10^{-12} eV particle:



frequency

- Set a typical length scale, and are a huge source of energy
- Sensitive to QCD axions with GUT- to Planck-scale decay constants f_a



Key Takeaways

- **Dissipation** is key to amplification

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- They **grow spontaneously** when a rapidly rotating BH is formed, **independent of any** pre-existing (cosmological or otherwise) **abundance**

Key Takeaways

- **Dissipation** is key to amplification
- Ultralight axions with **compton wavelength** comparable to **black hole radius** form 'gravitational atoms'
- They **grow spontaneously** when a rapidly rotating BH is formed, **independent of any** pre-existing (cosmological or otherwise) **abundance**
- **Number of axions increases exponentially** by extracting the BH's energy and angular momentum

Gravitational Superradiance

Gravitational Superradiance

- If new light axions exist, fast-spinning black holes will superradiate: lose energy and angular momentum to exponentially growing bound states of axions

Arvanitaki, Dimopoulos, Dubovsky,
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Arvanitaki, Baryakhtar, Huang 2015

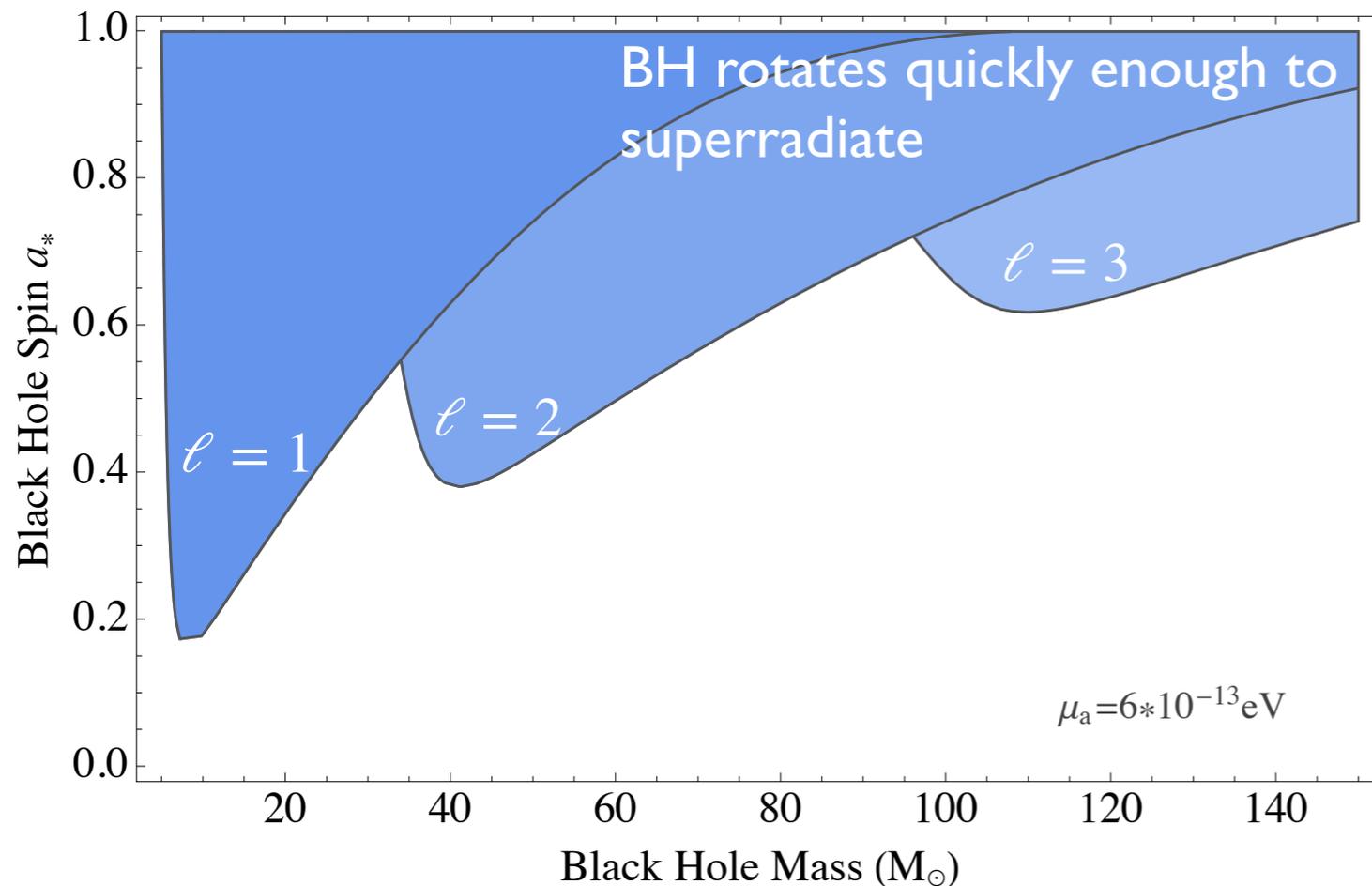
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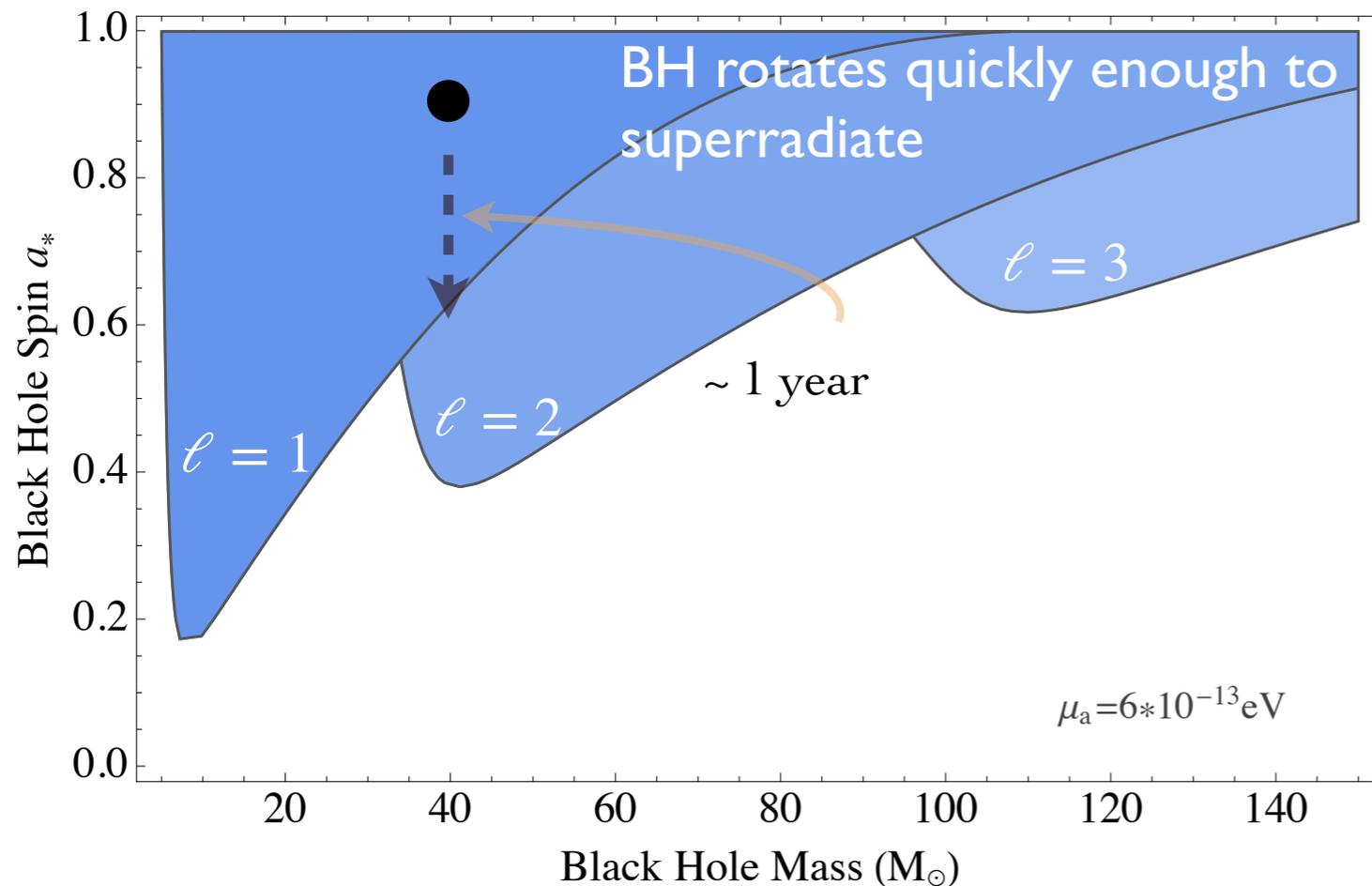
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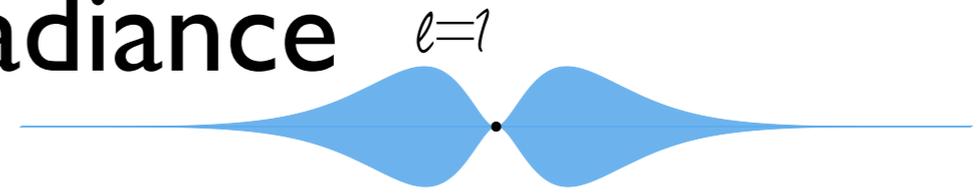
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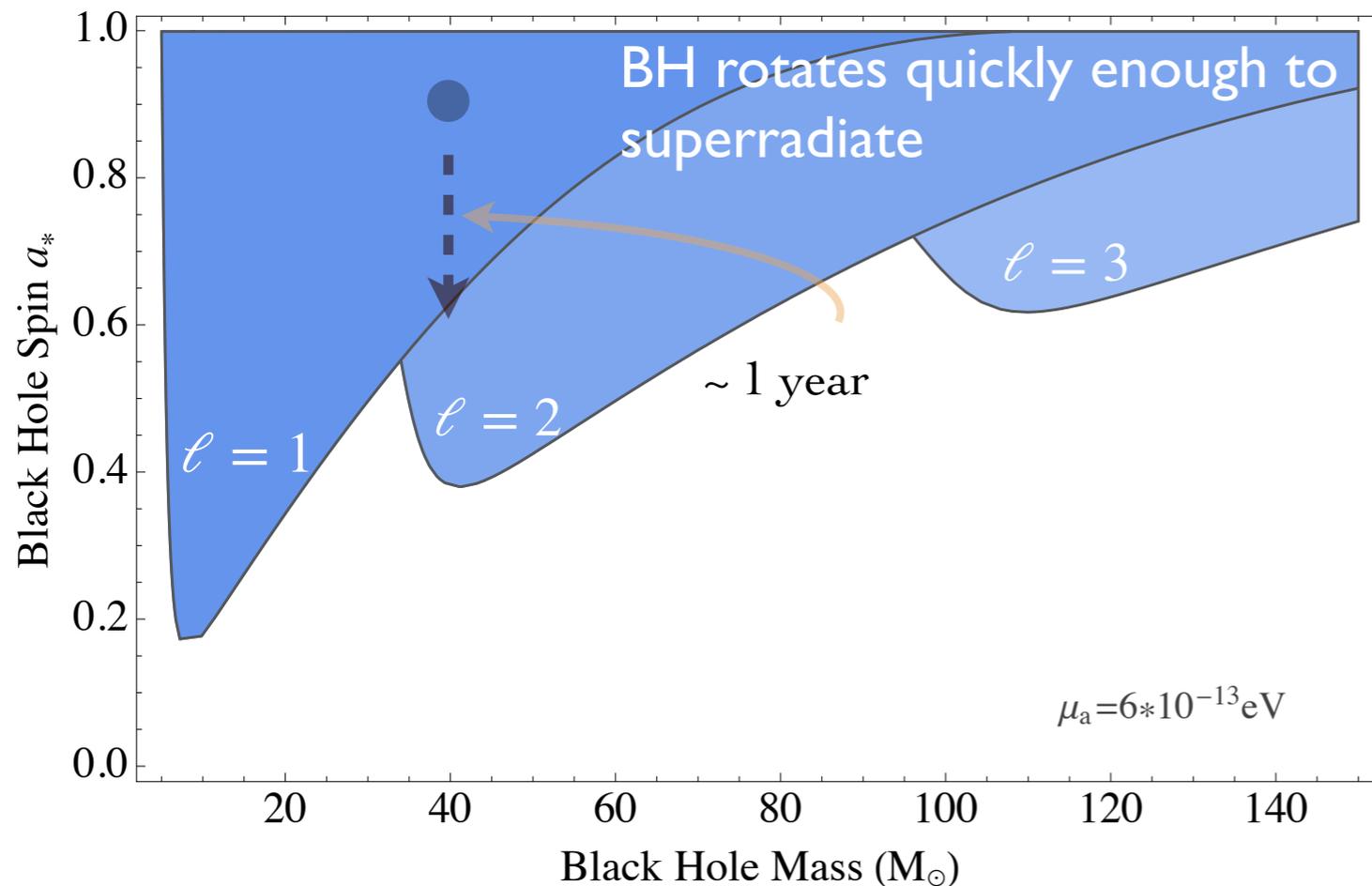
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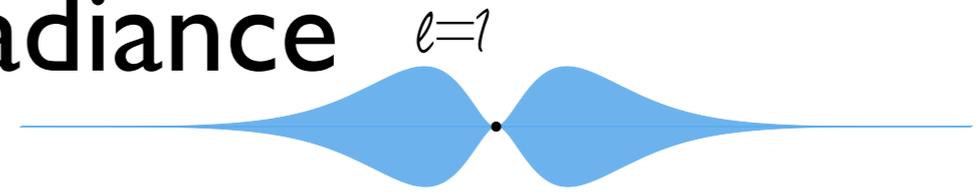
Gravitational Superradiance $\ell=1$



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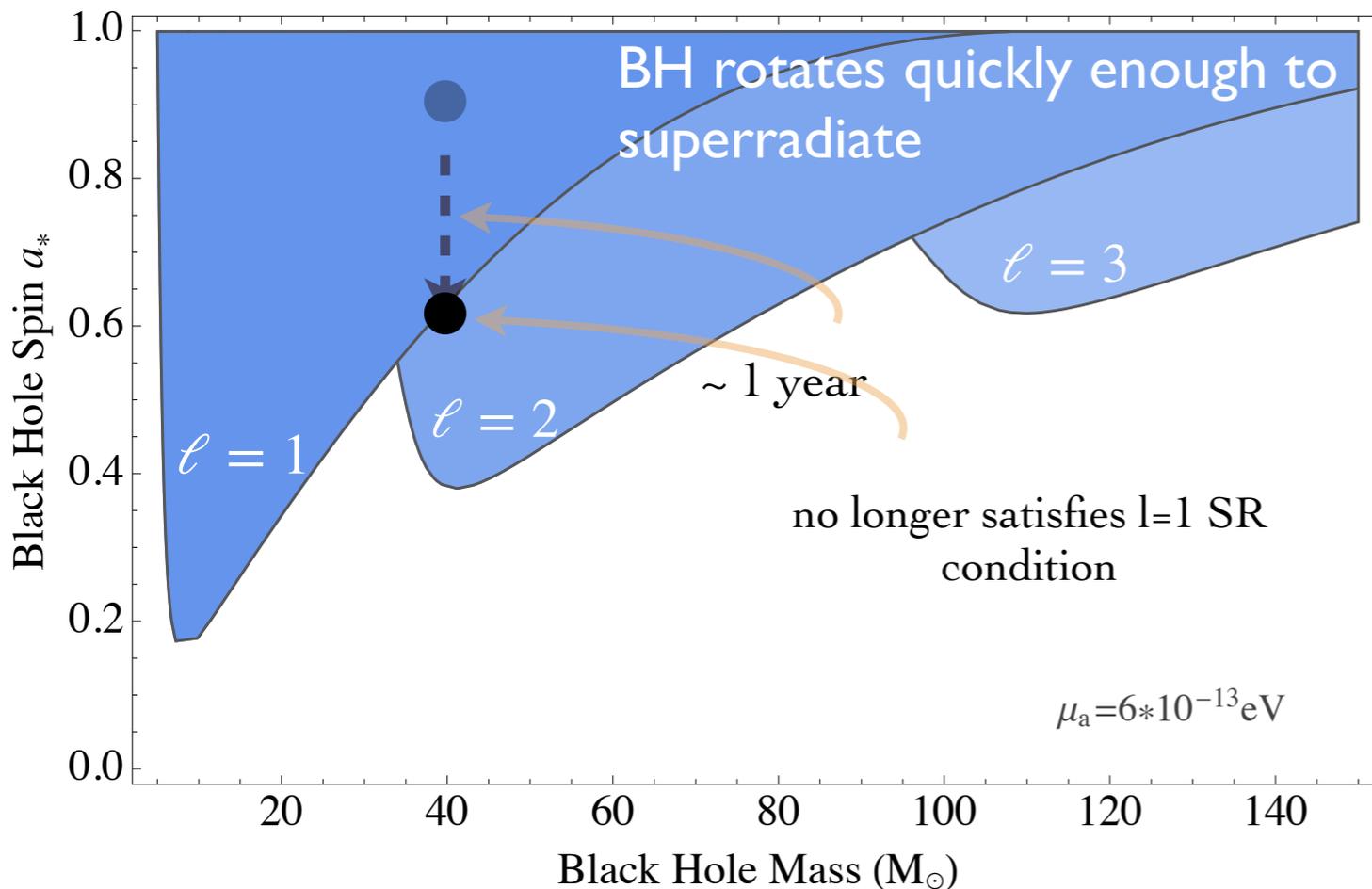
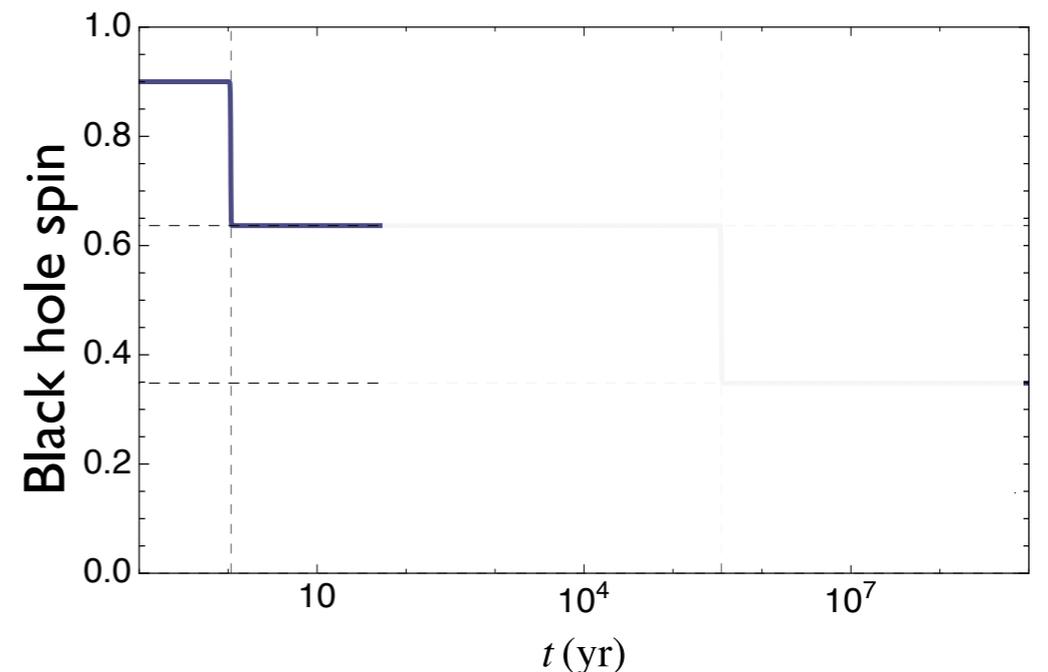
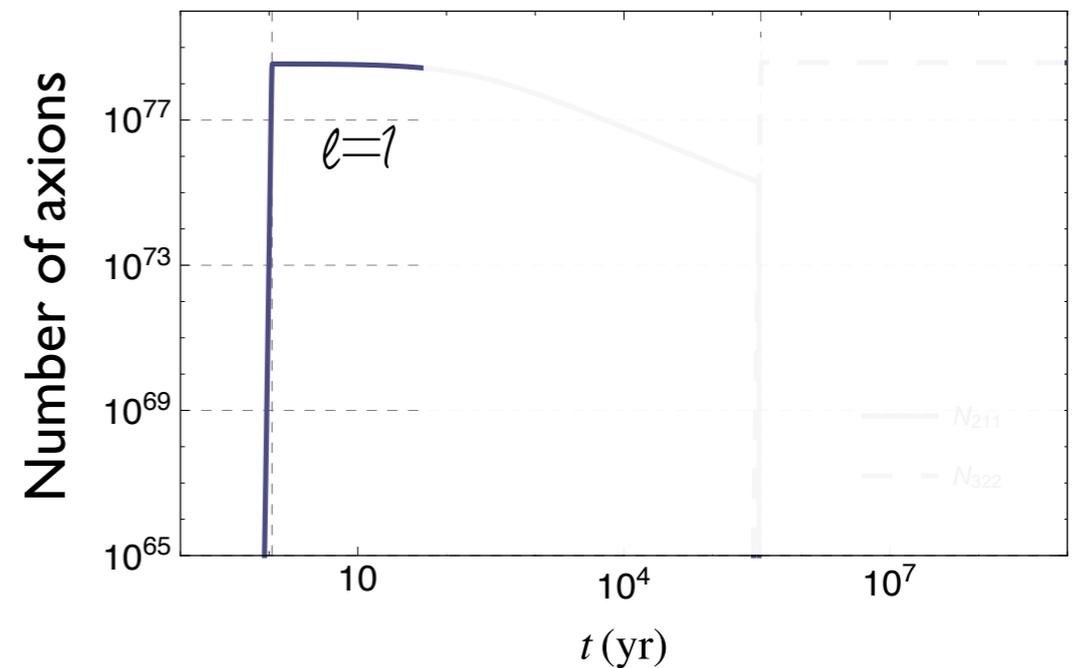


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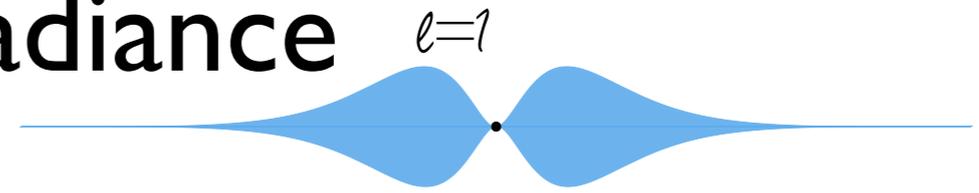


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Time evolution

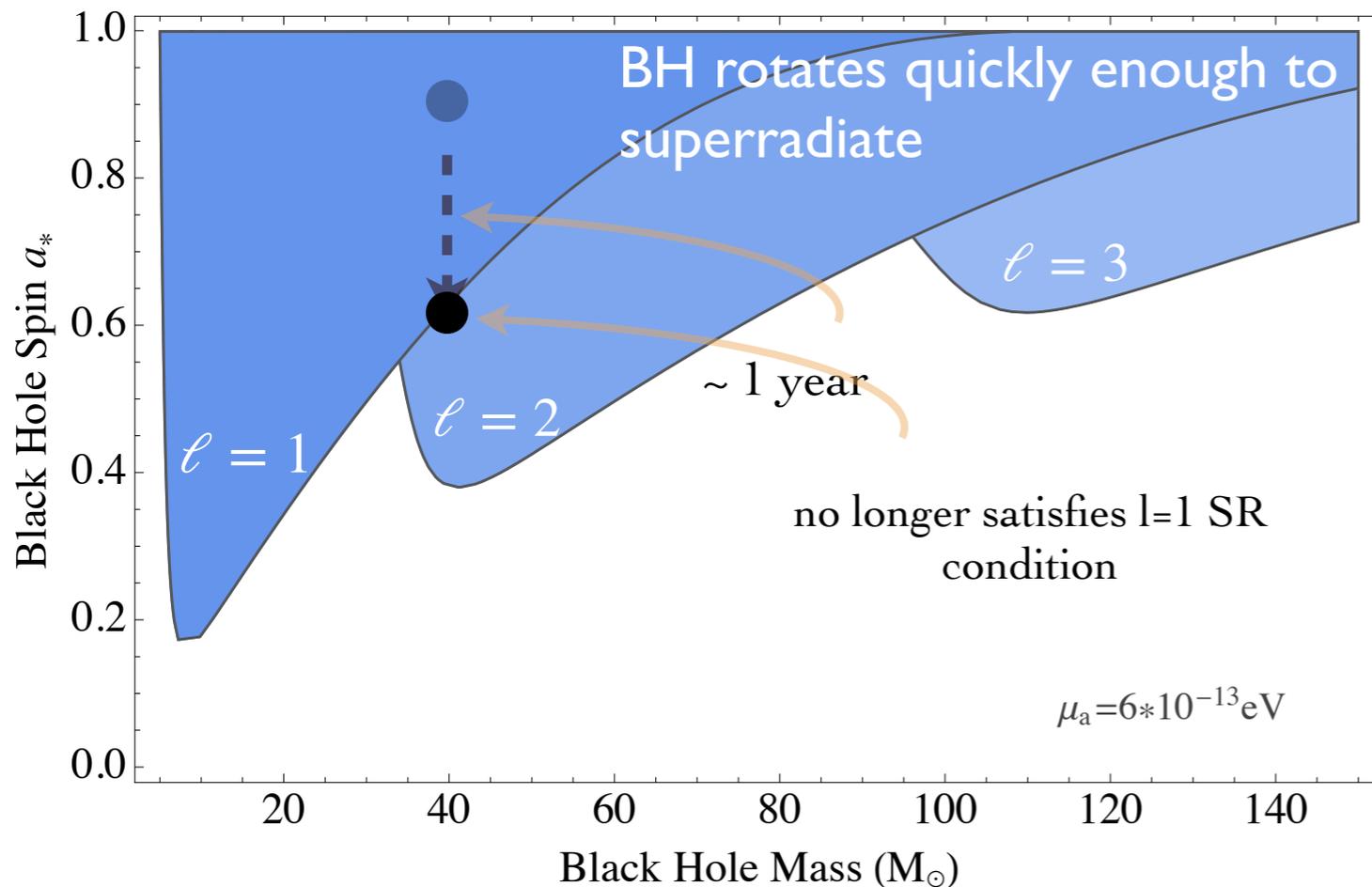
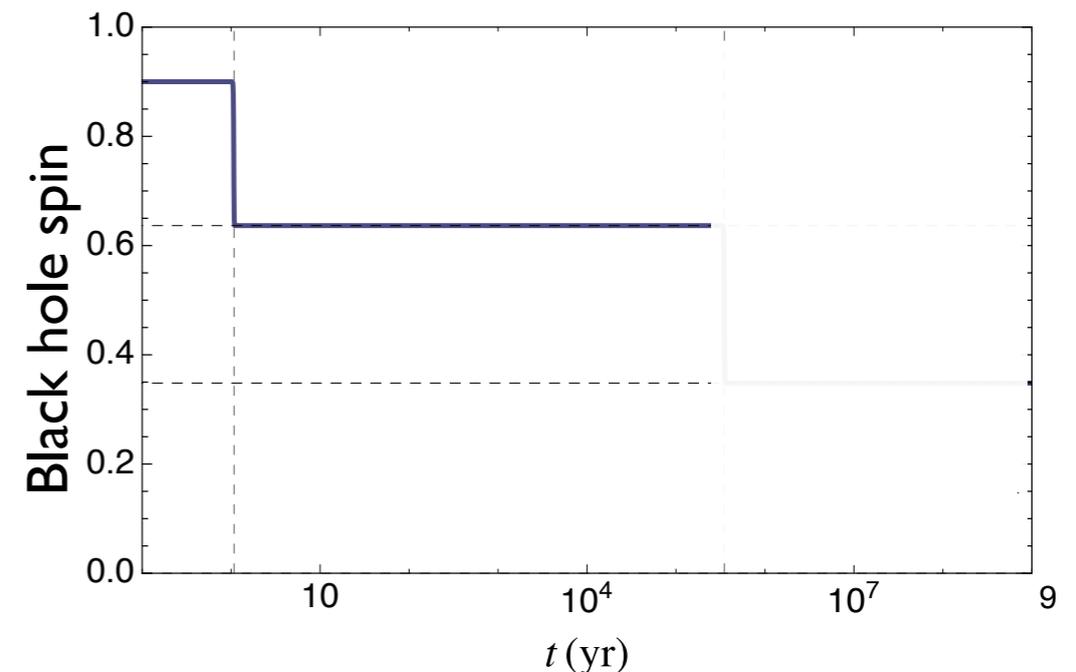
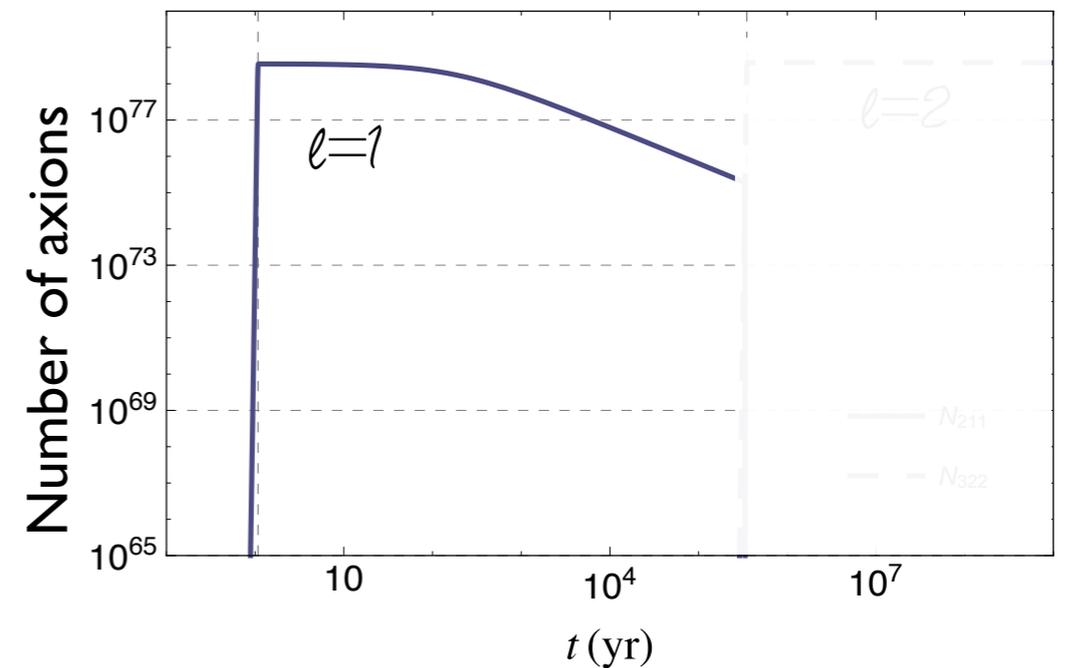


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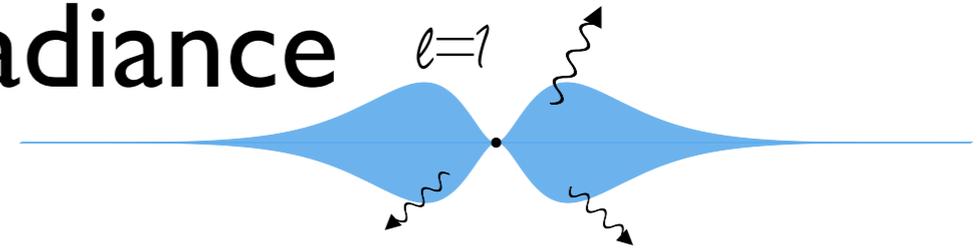


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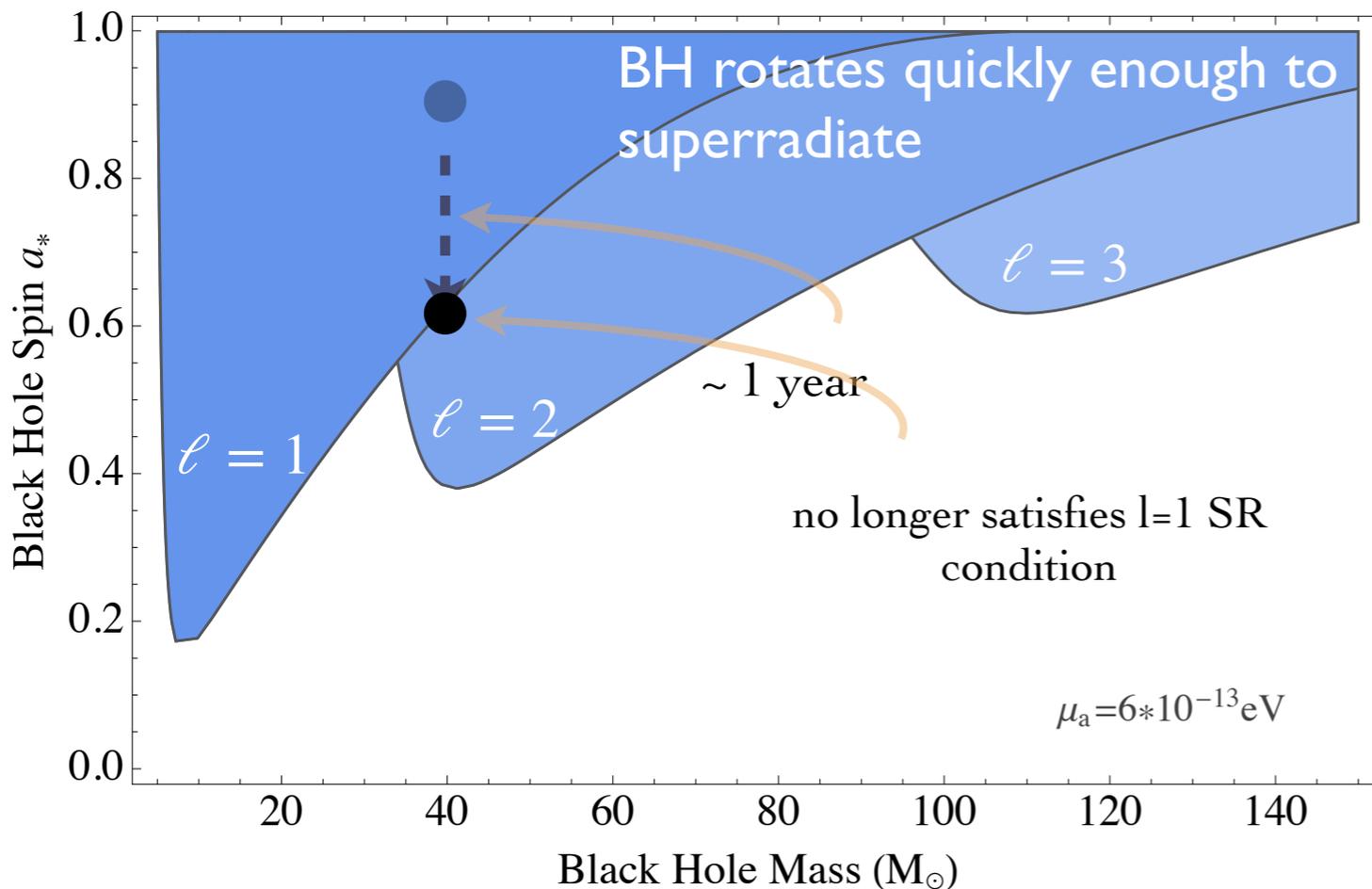
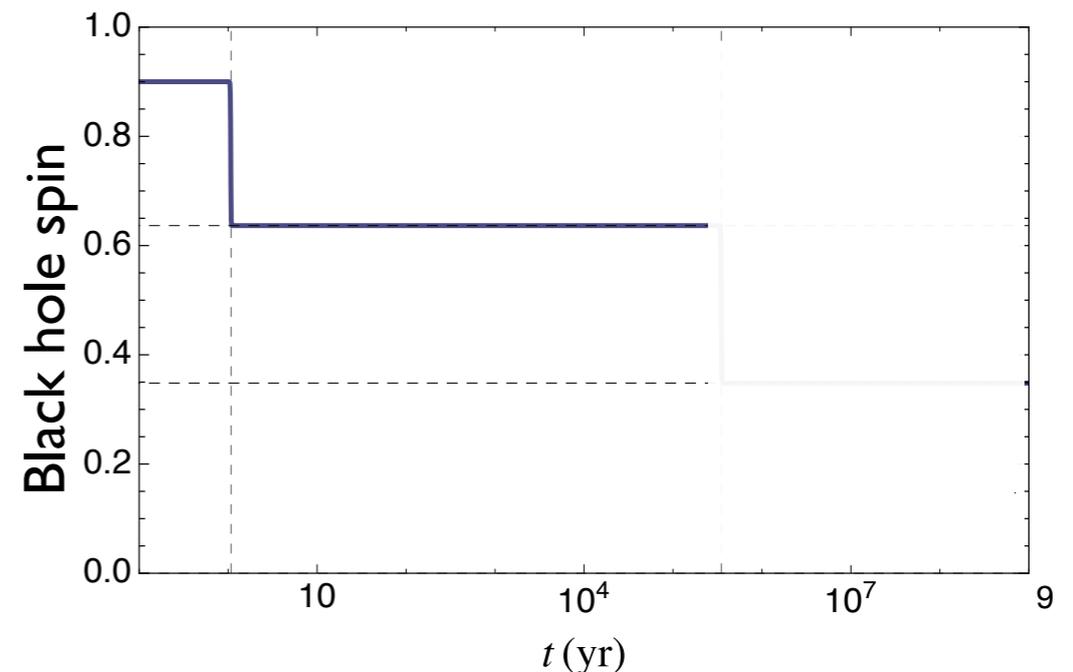
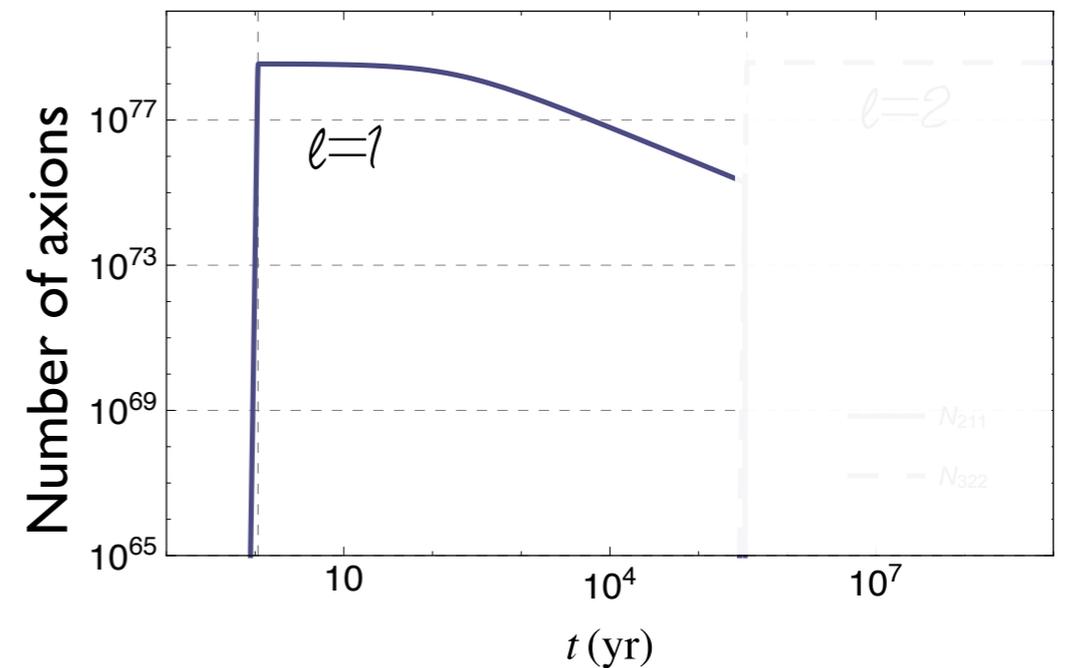


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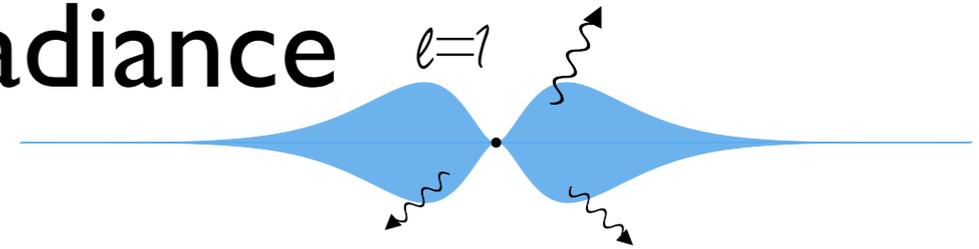


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- Axion cloud depletes through gravitational wave radiation

Time evolution



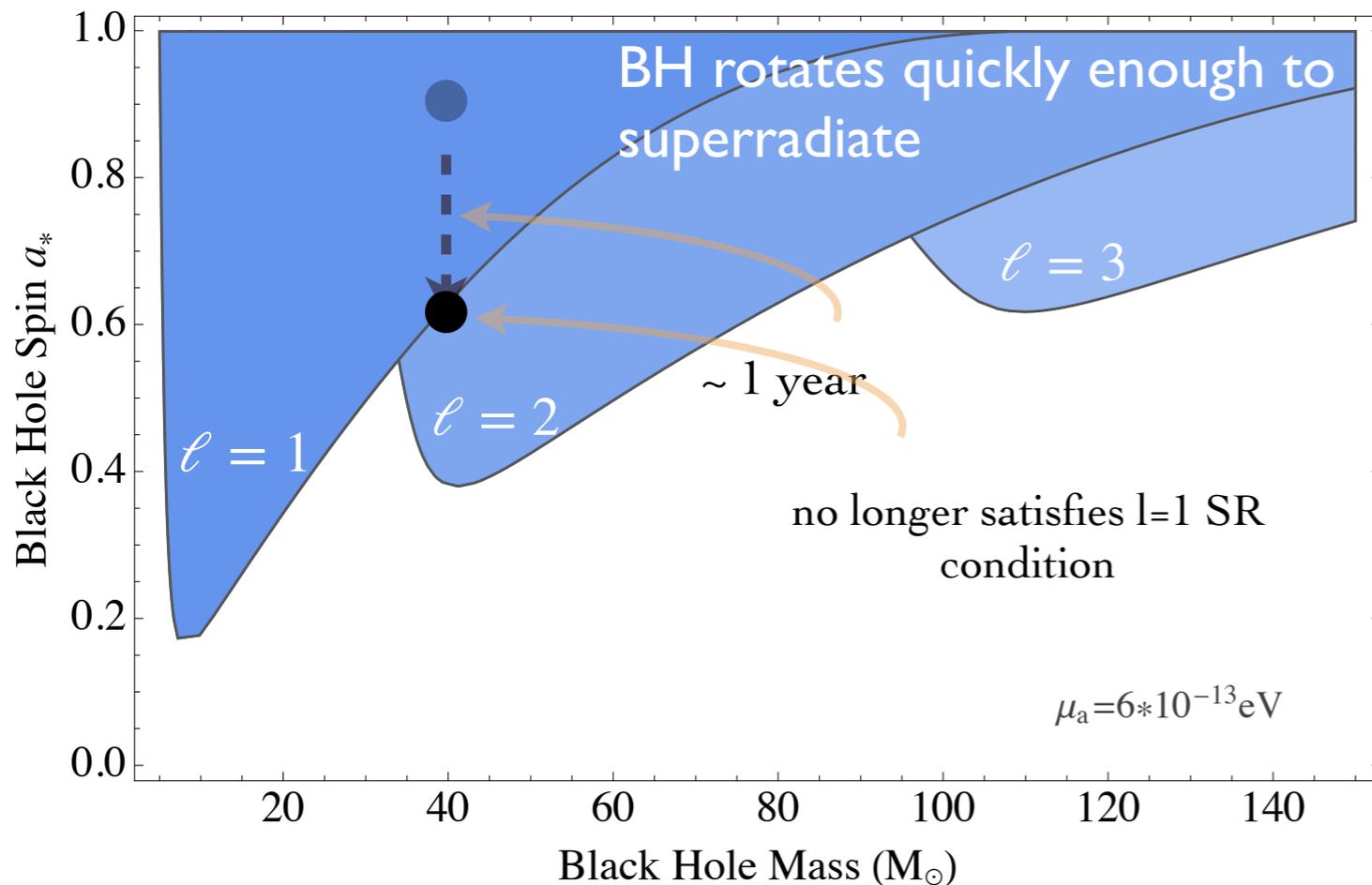
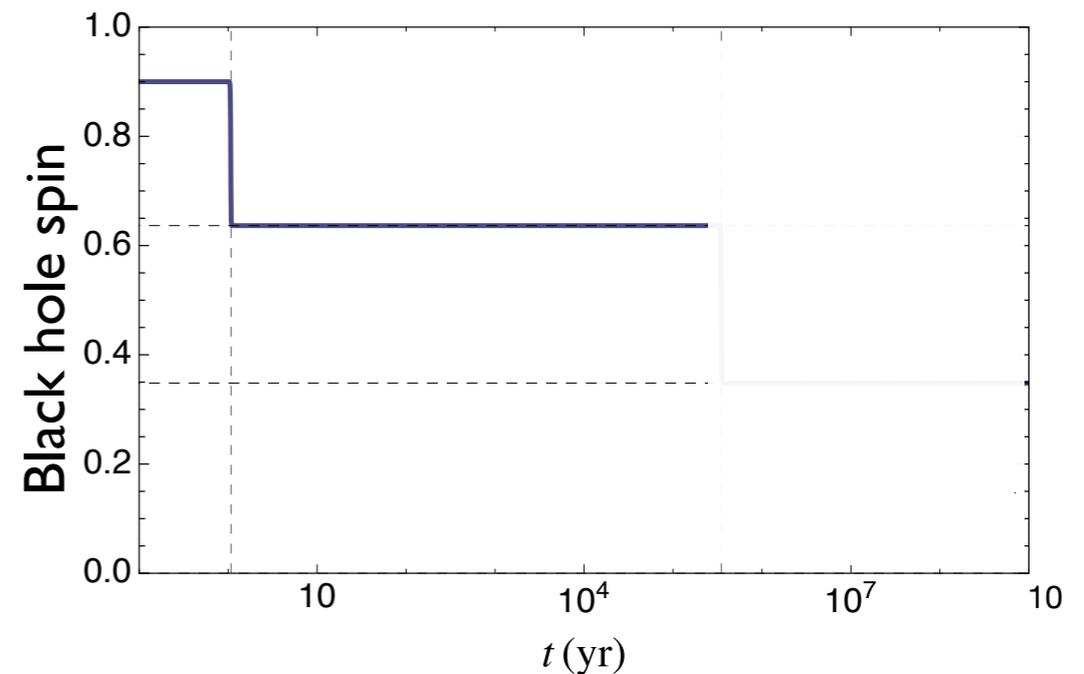
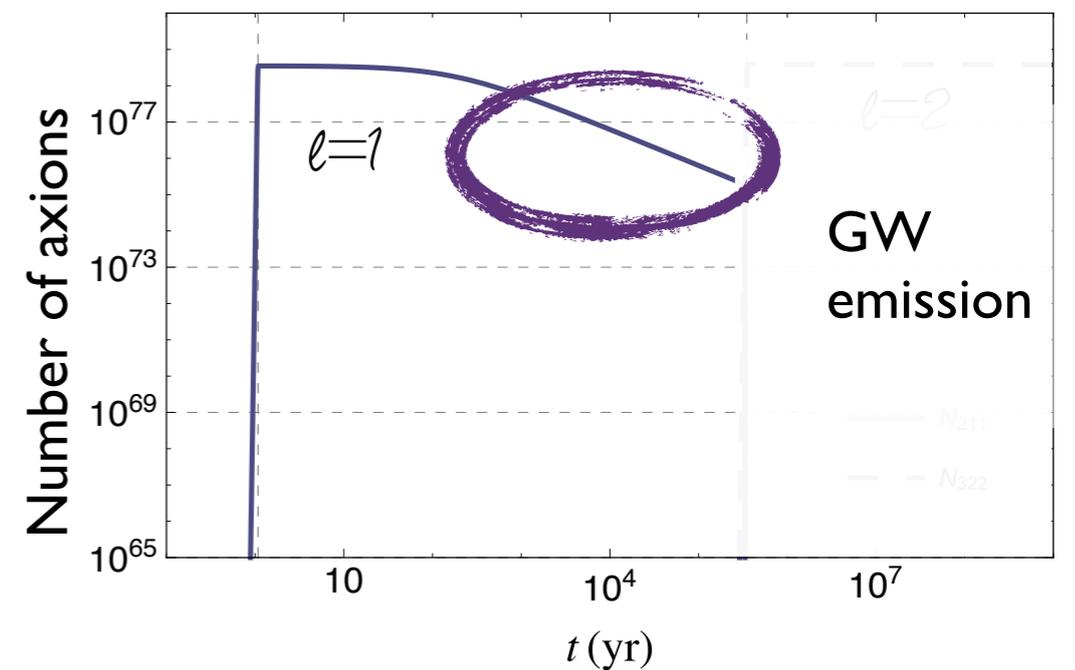
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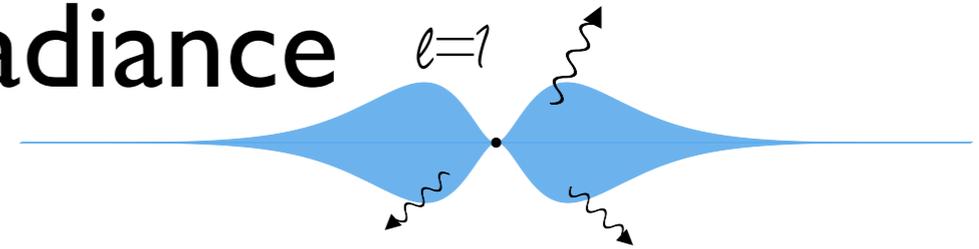
Up to **thousands of observable signals** above current LIGO upper limits — lack of observation can disfavor a range of axion masses

Zhu, Baryakhtar, Papa, Tsuna, Kawanaka, Eggenstein (2020)

Time evolution



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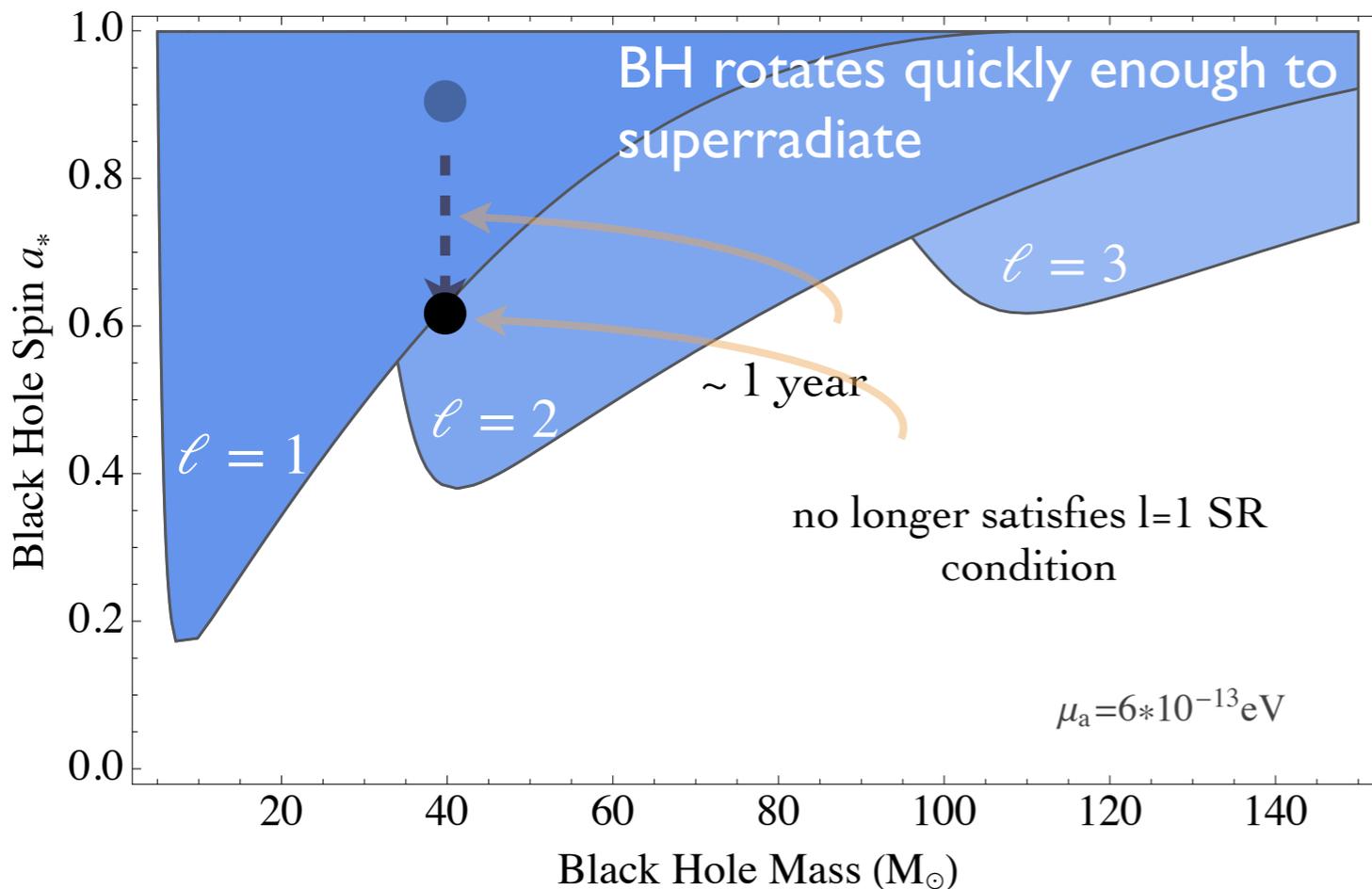
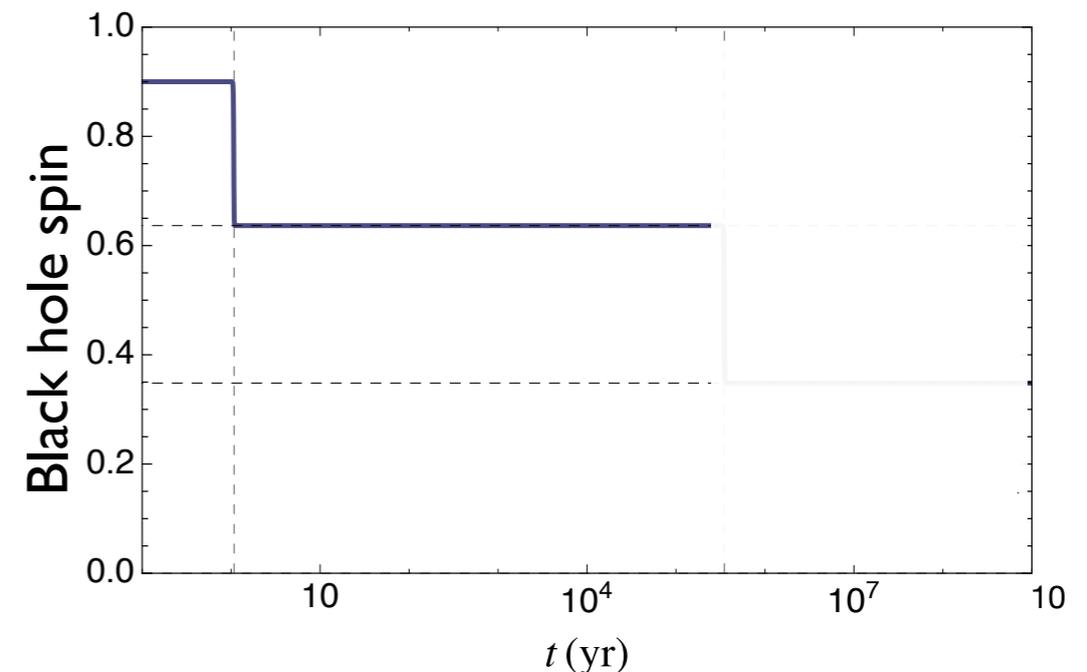
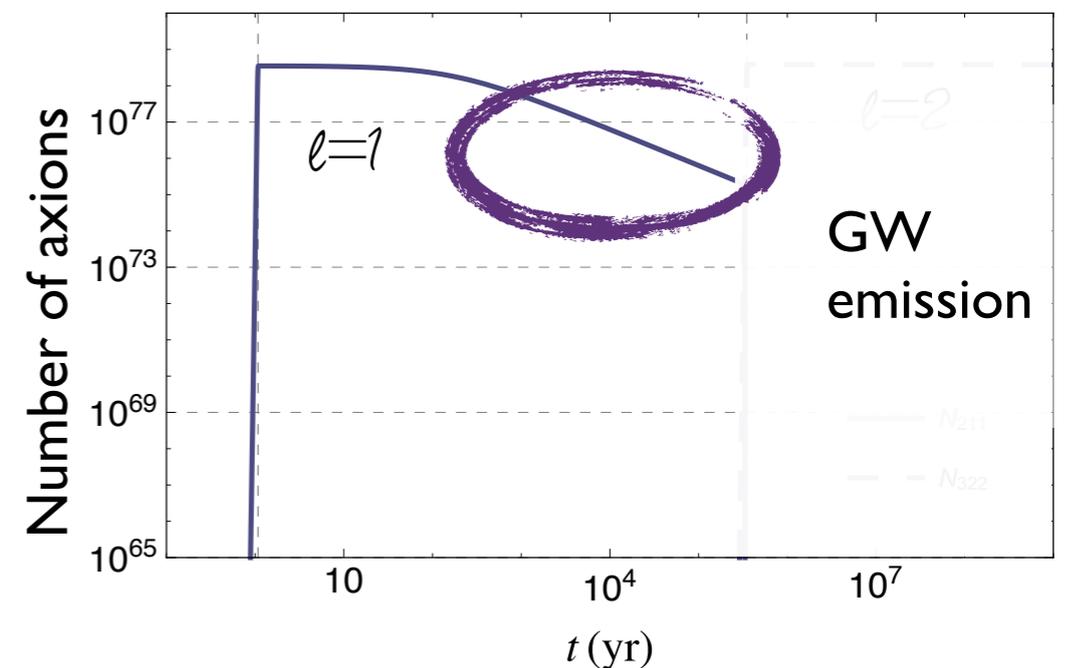


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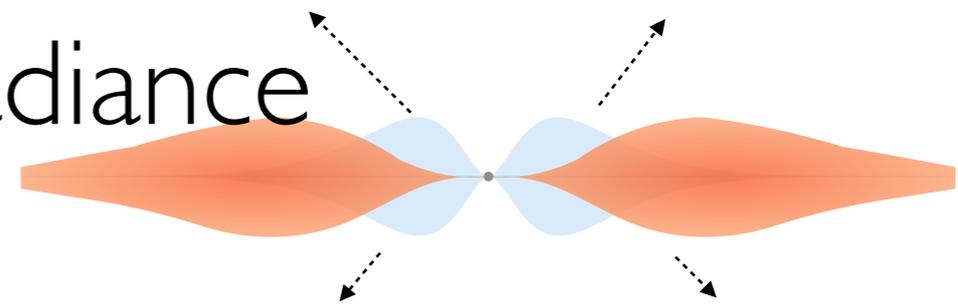
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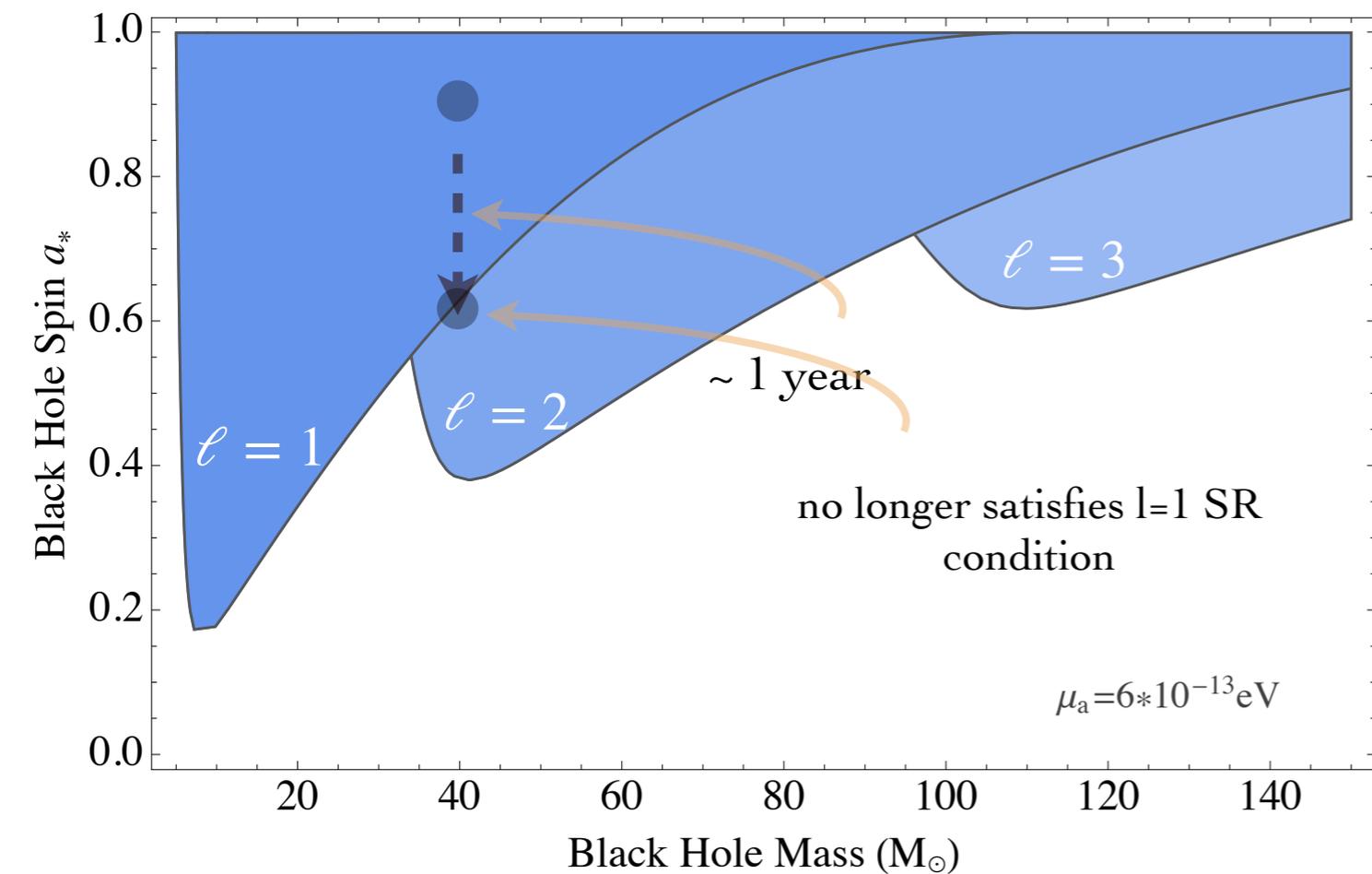
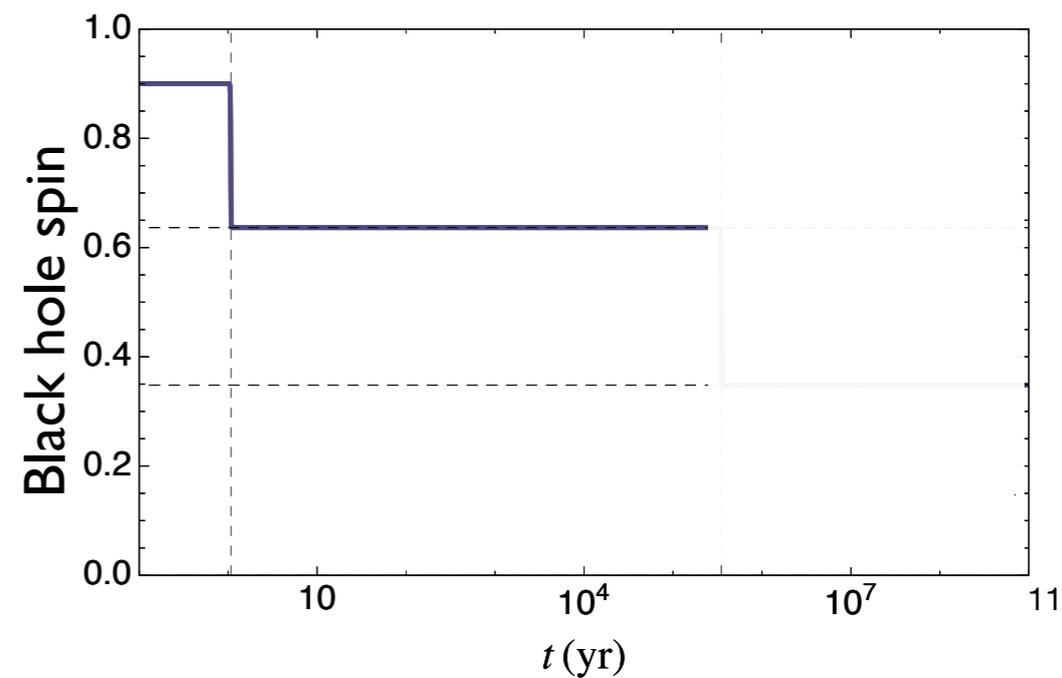
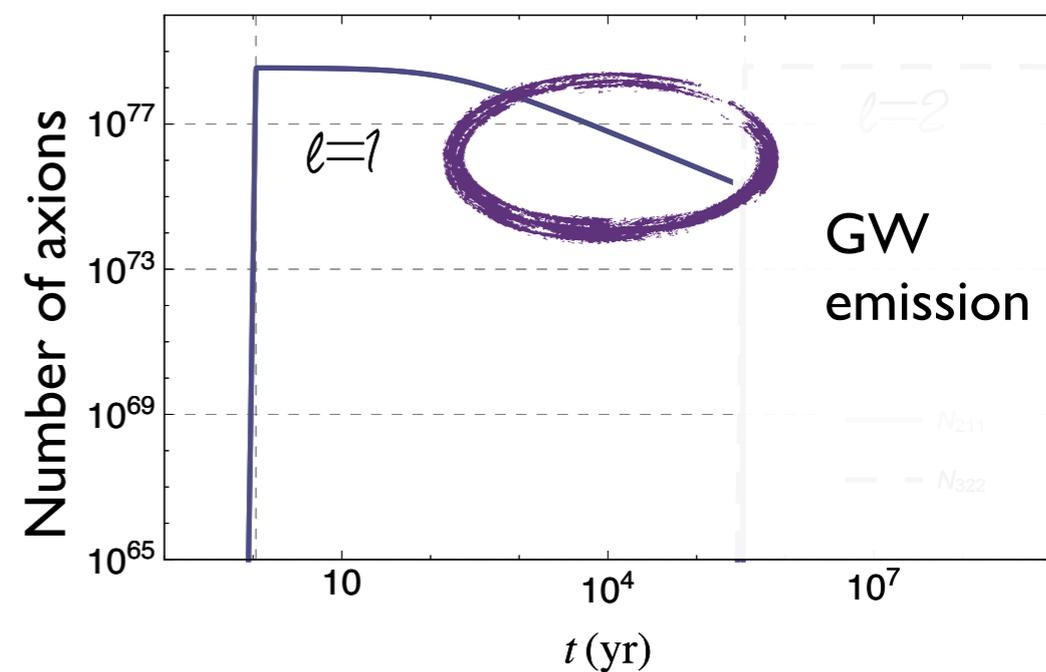
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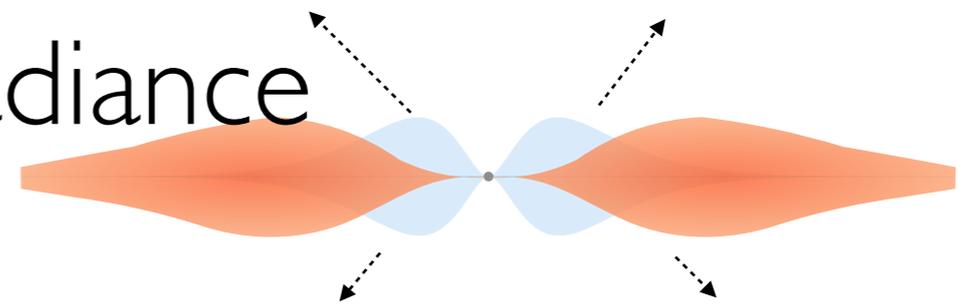
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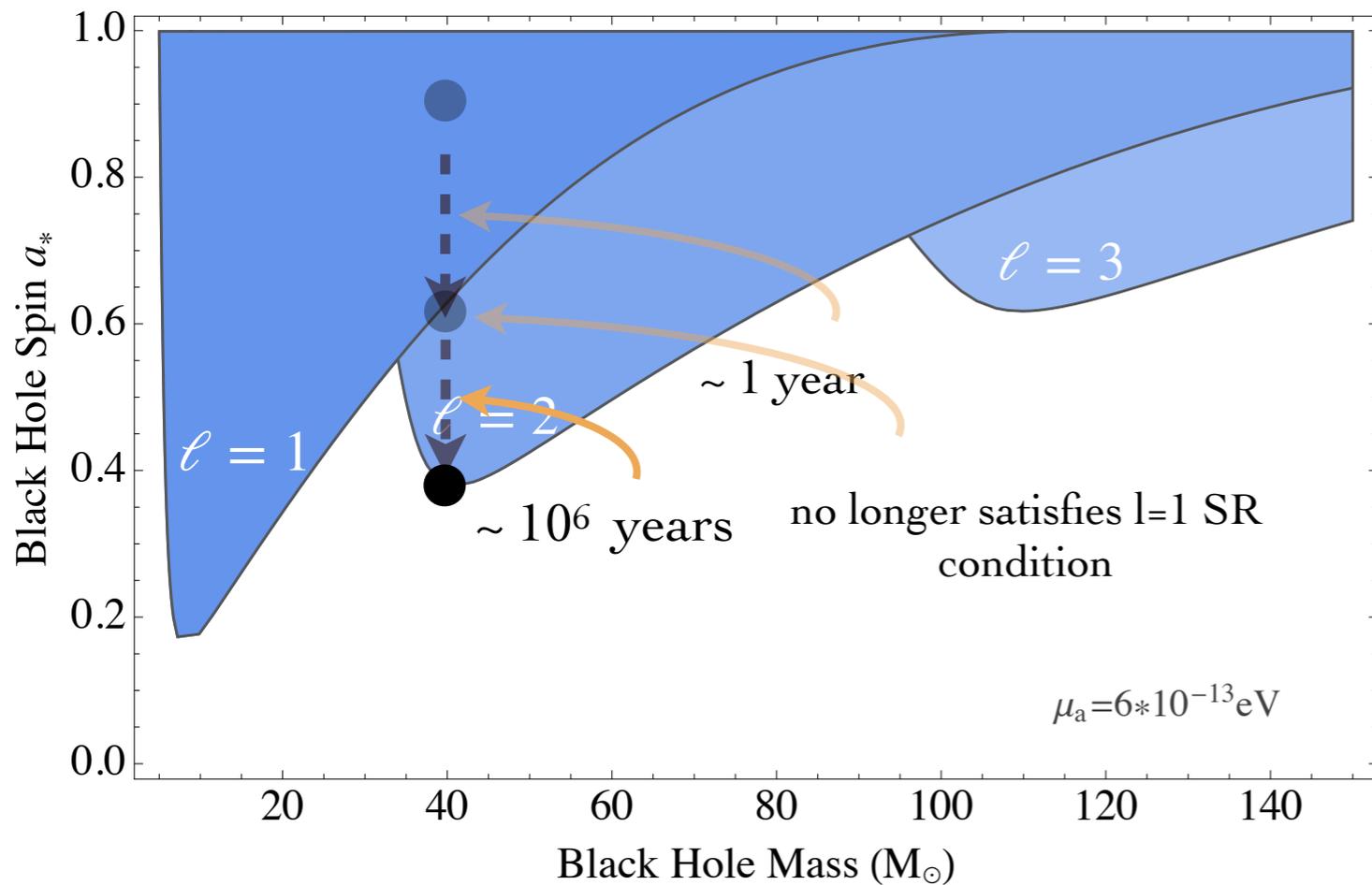
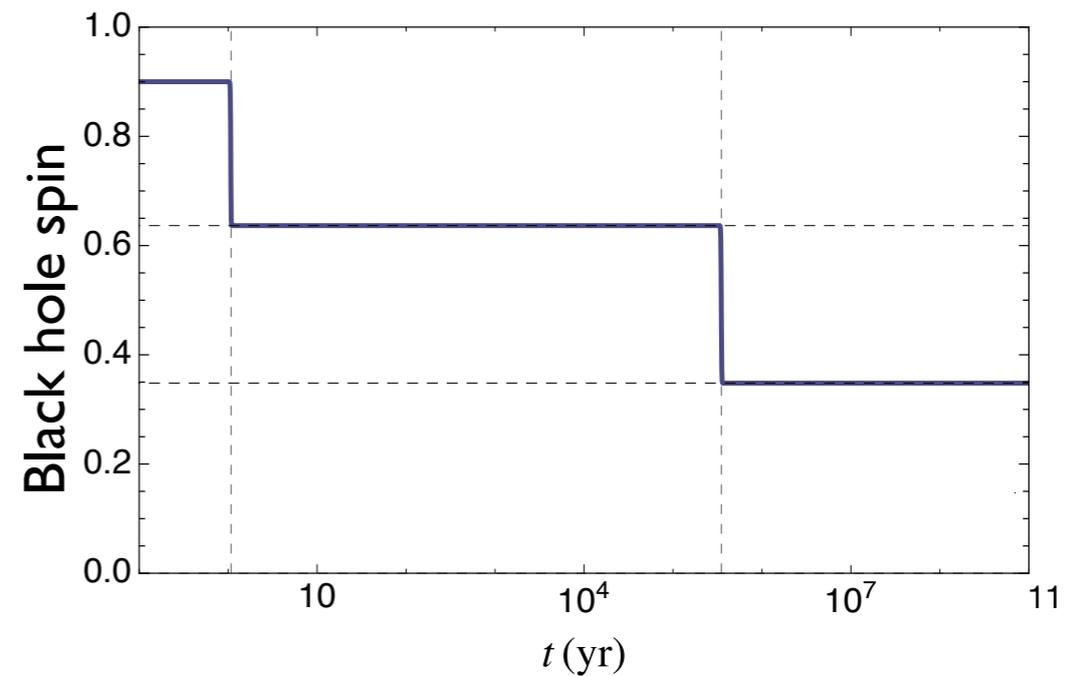
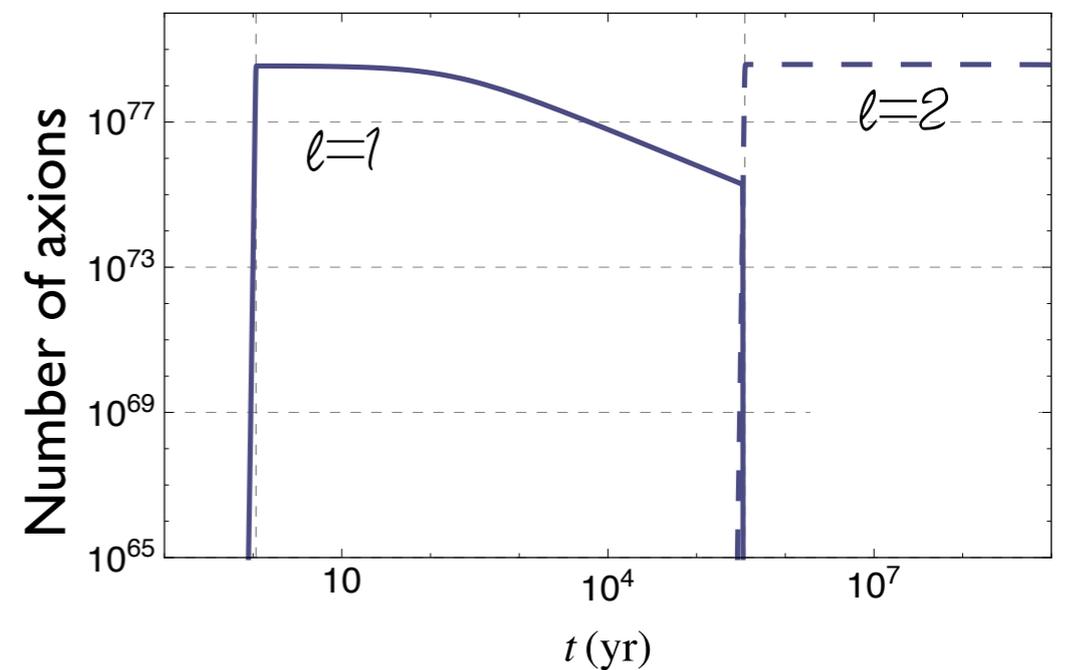
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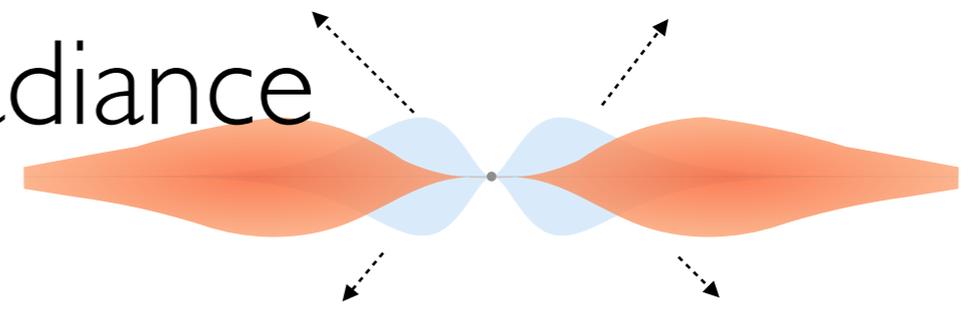
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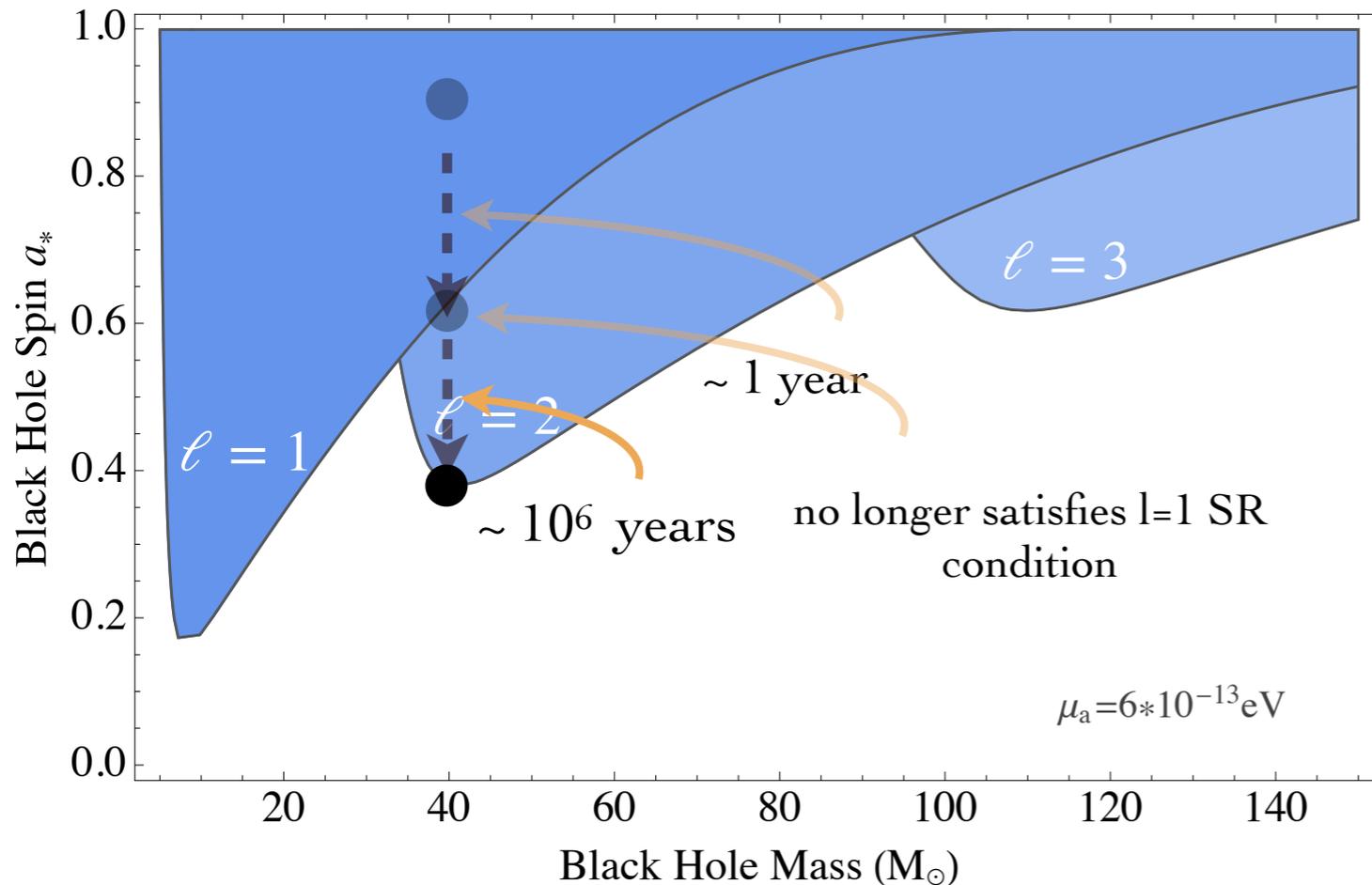
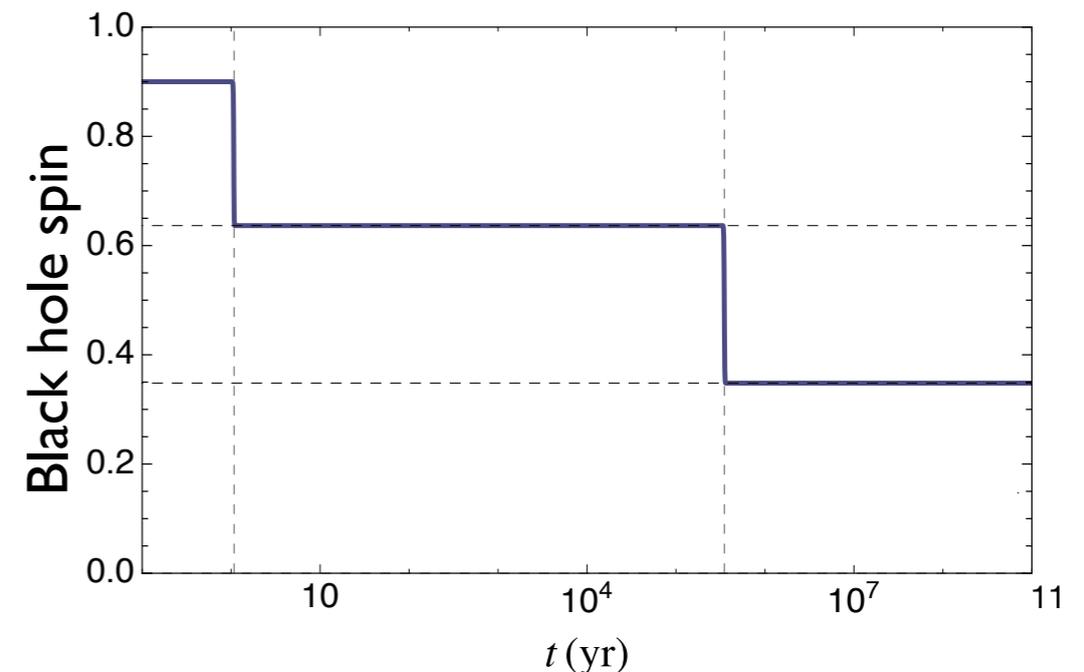
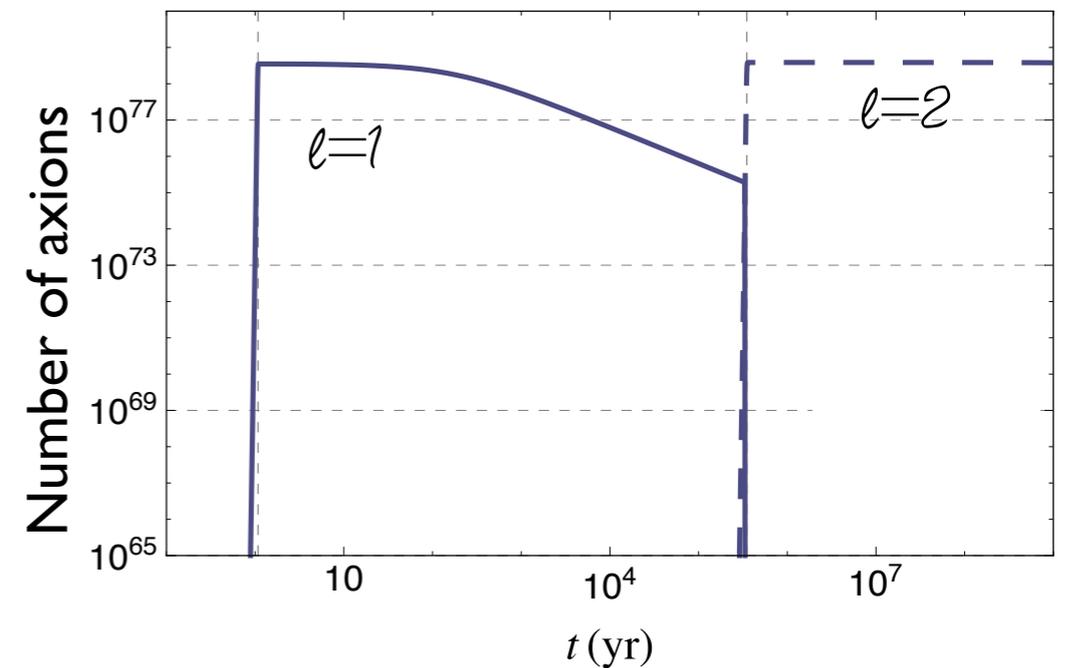


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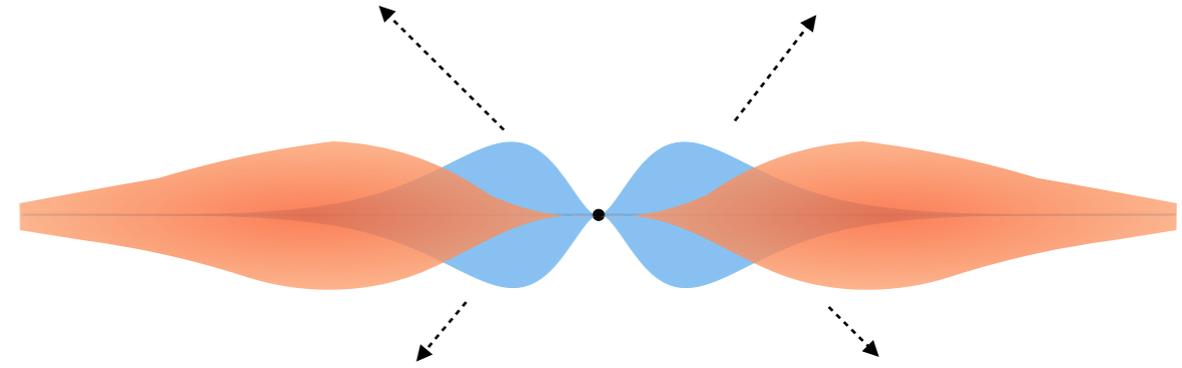
- Bound state with higher angular momentum grows exponentially
- Growth parametrically longer due to angular momentum barrier: less overlap with black hole, less efficient energy extraction

Time evolution



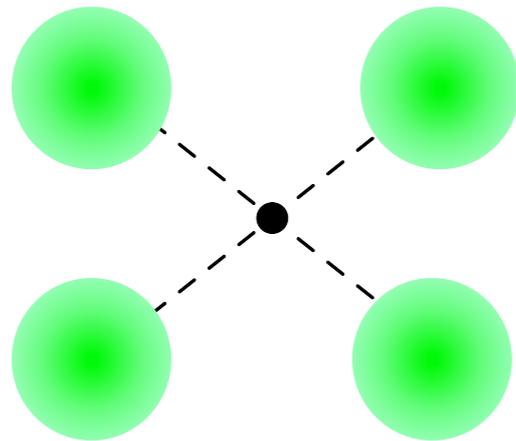
Self-Interactions

Cloud can carry up to a few percent of the black hole mass: huge energy density



M. Baryakhtar, **MG**, R. Lasenby, O. Simon 2021

- What new effects arise when axion self-interactions become important?



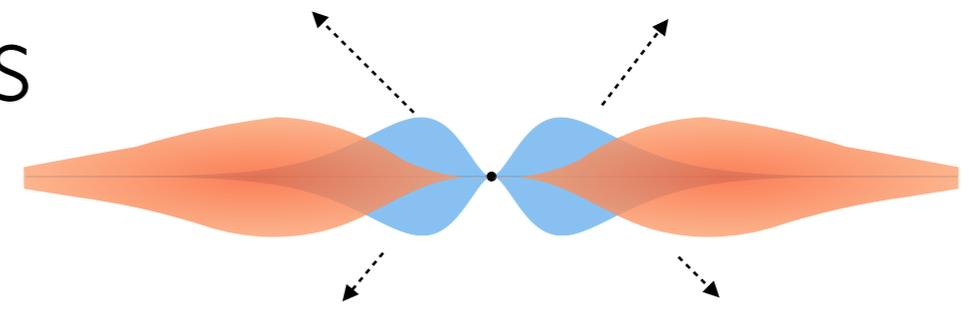
Fukuda, Nakayama JHEP01 (2020) 128
A. Gruzinov, 1604.06422

Free real scalar field $+ \frac{\lambda}{4!} \phi^4$

$\frac{\mu_a^2}{f_a^2}$

(A red arrow points from the fraction $\frac{\mu_a^2}{f_a^2}$ to the λ in the equation above.)

Self-Interactions

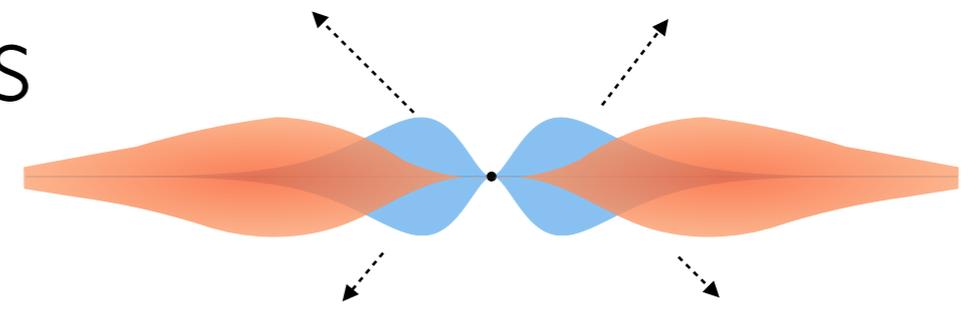


M. Baryakhtar, **MG**, R. Lasenby, O. Simon 2021

Larger self-interactions:

- Black hole energy sources the cloud through superradiance

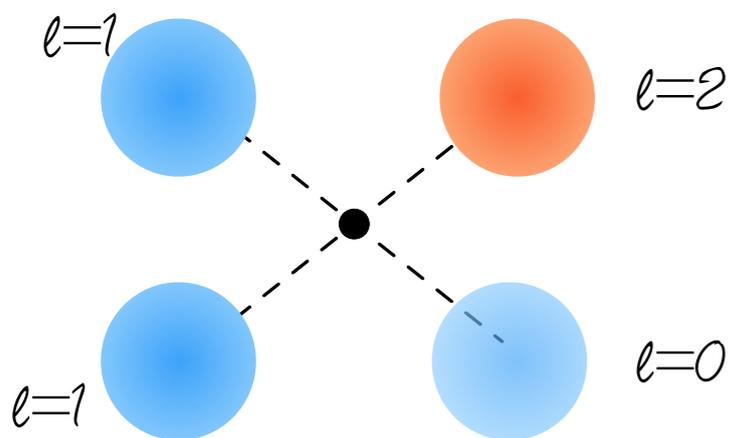
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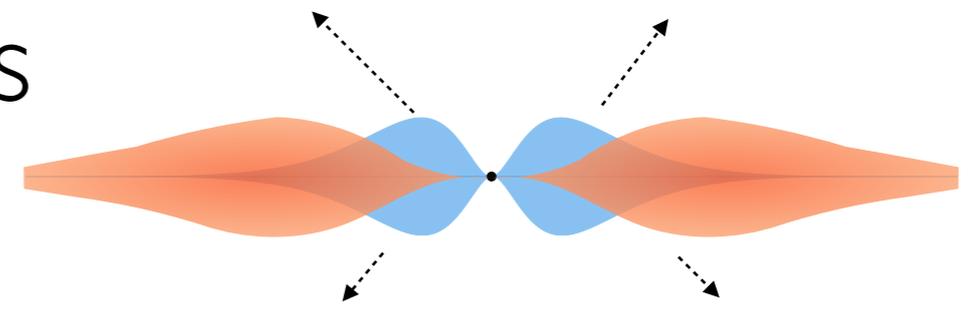
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- Second level populated through self-interactions



A. Gruzinov, 1604.06422

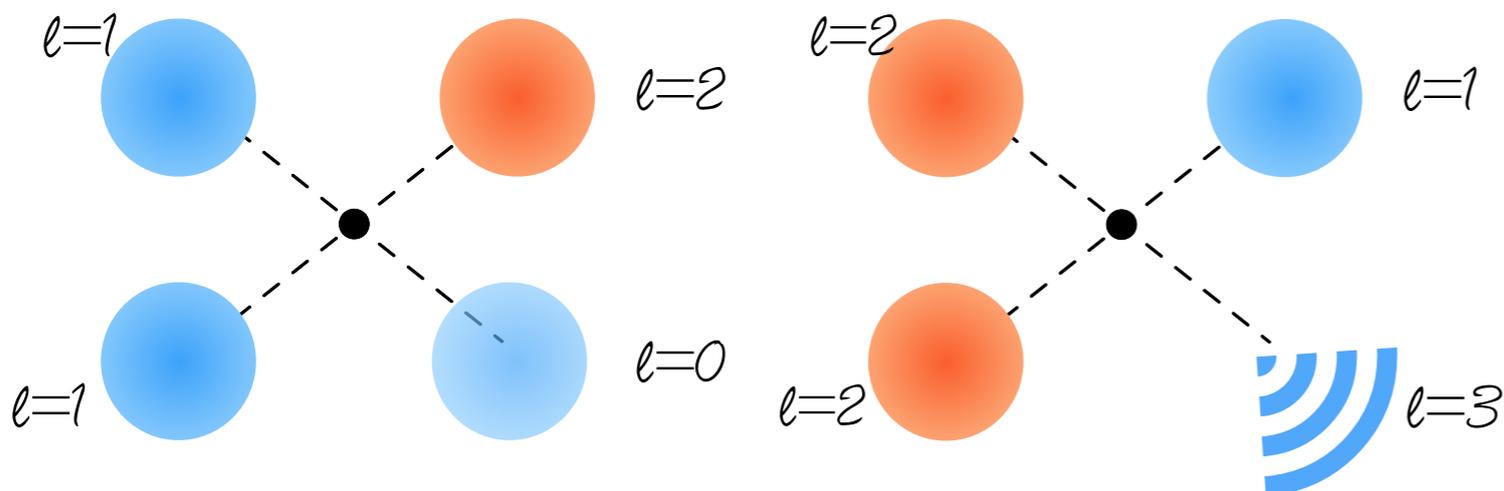
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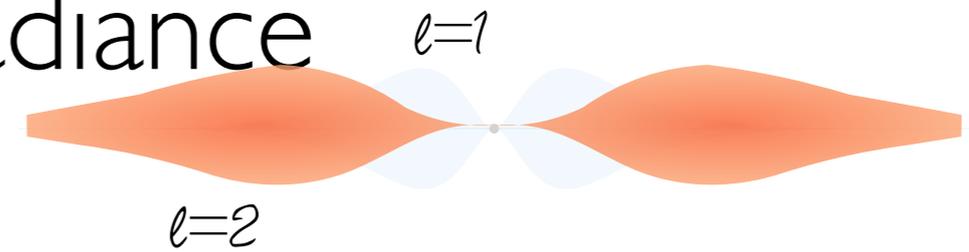
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- Second level populated through self-interactions
- Non-relativistic axion waves carry energy to infinity



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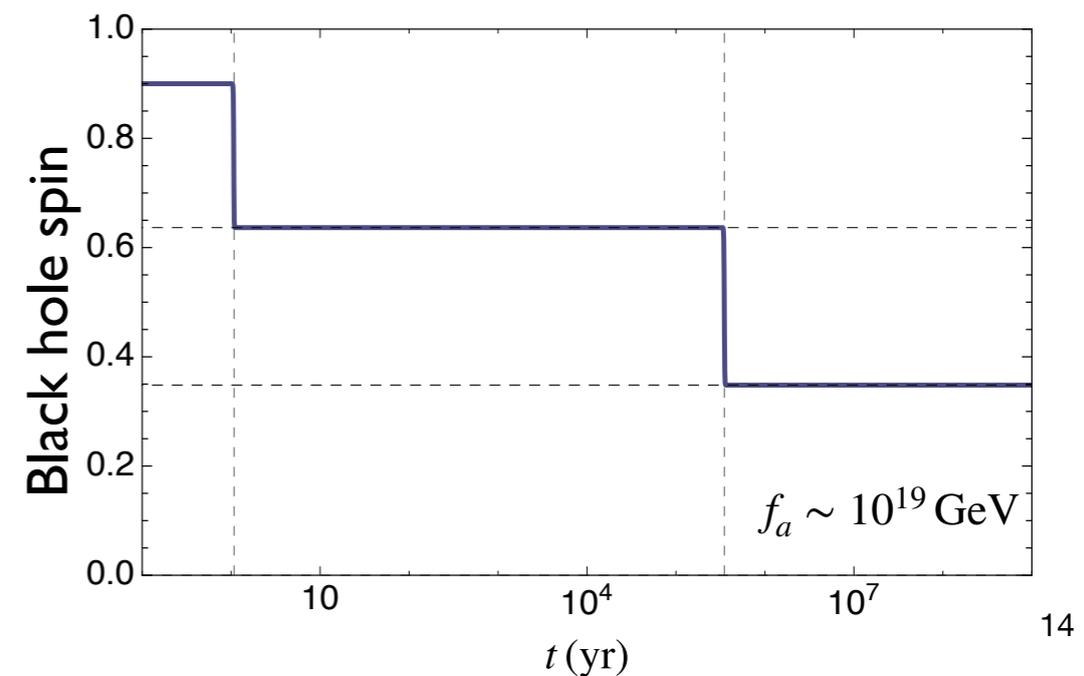
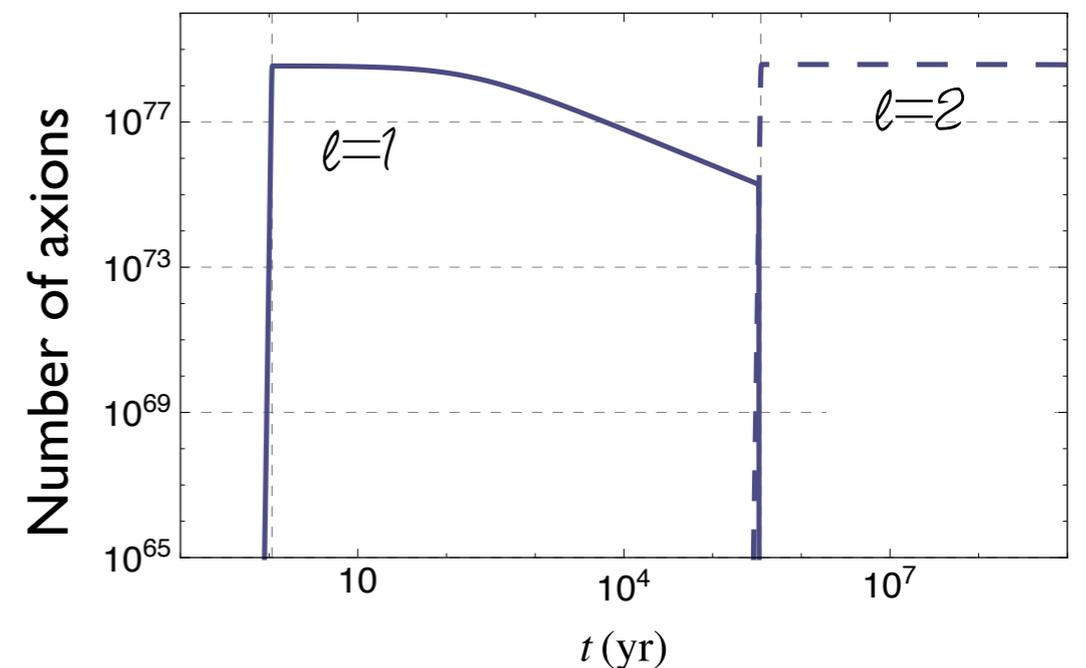


Gravitational self-interactions $f_a \sim M_{\text{Pl}}$

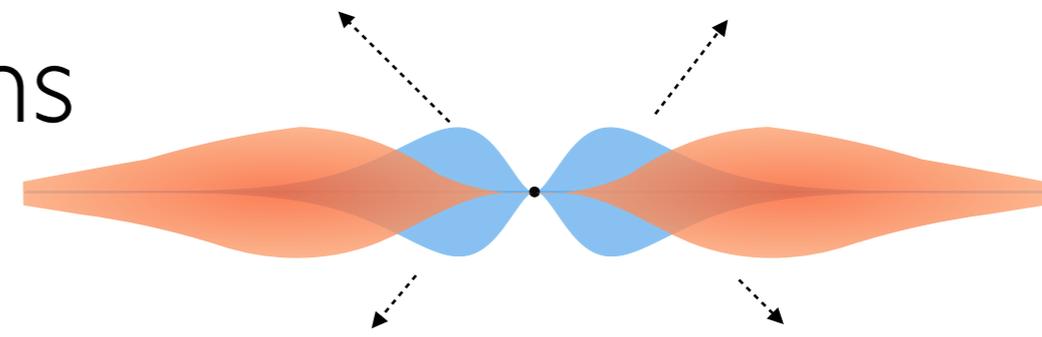
M. Baryakhtar, **MG**, R. Lasenby, O. Simon 2021

- One bound state at a time
- Gravitational radiation

Time evolution



Self-Interactions

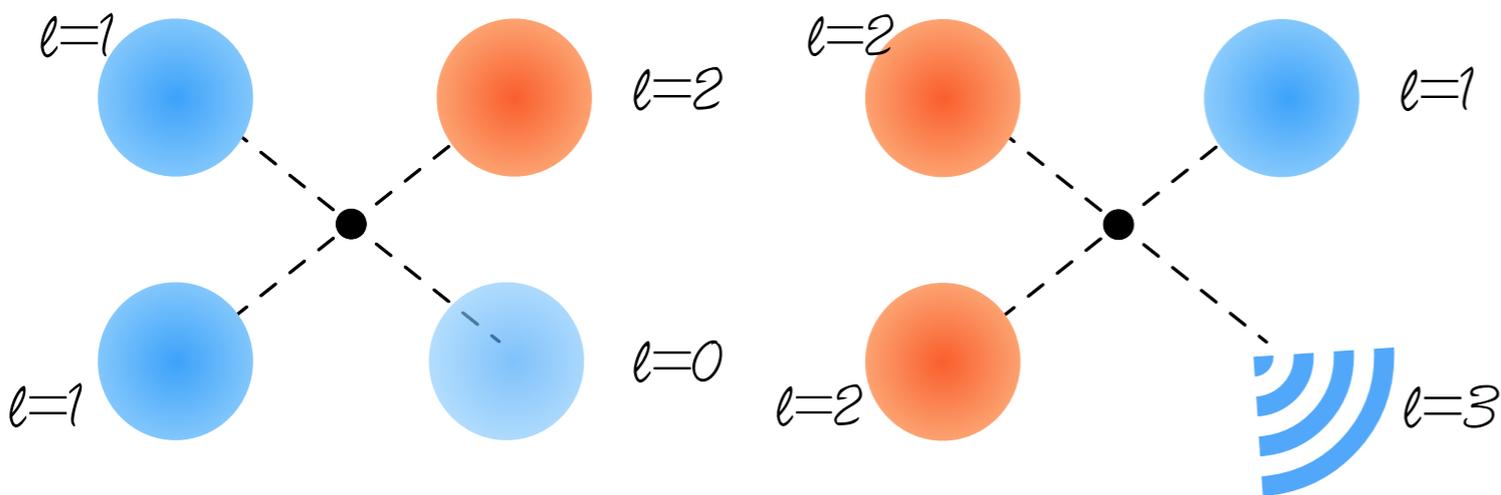
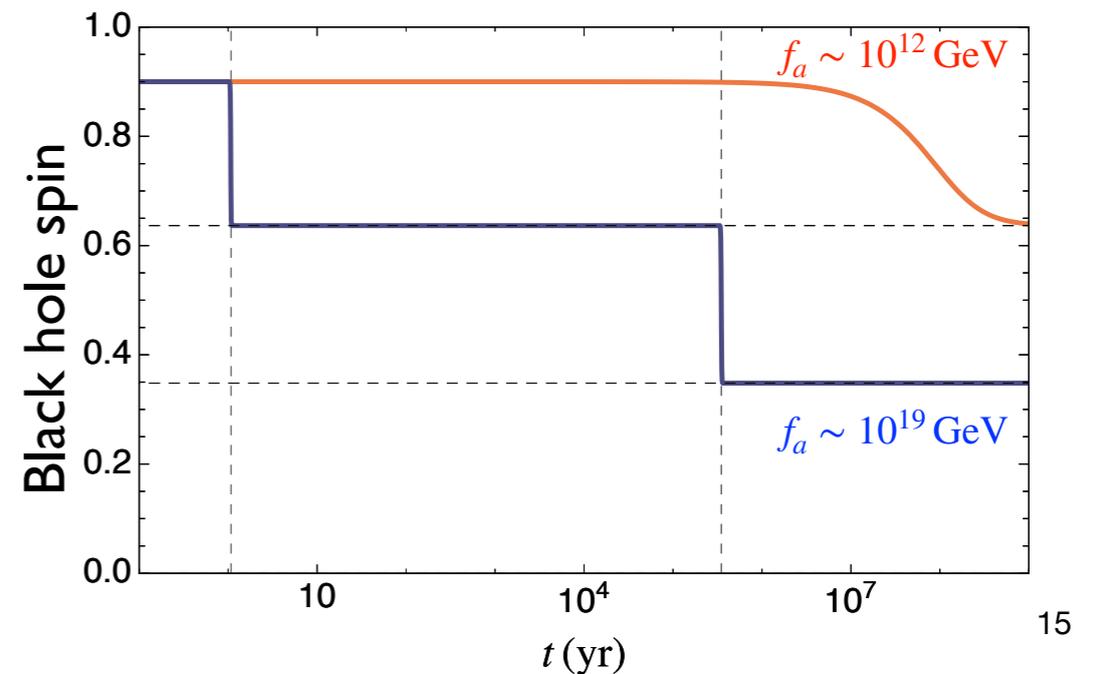
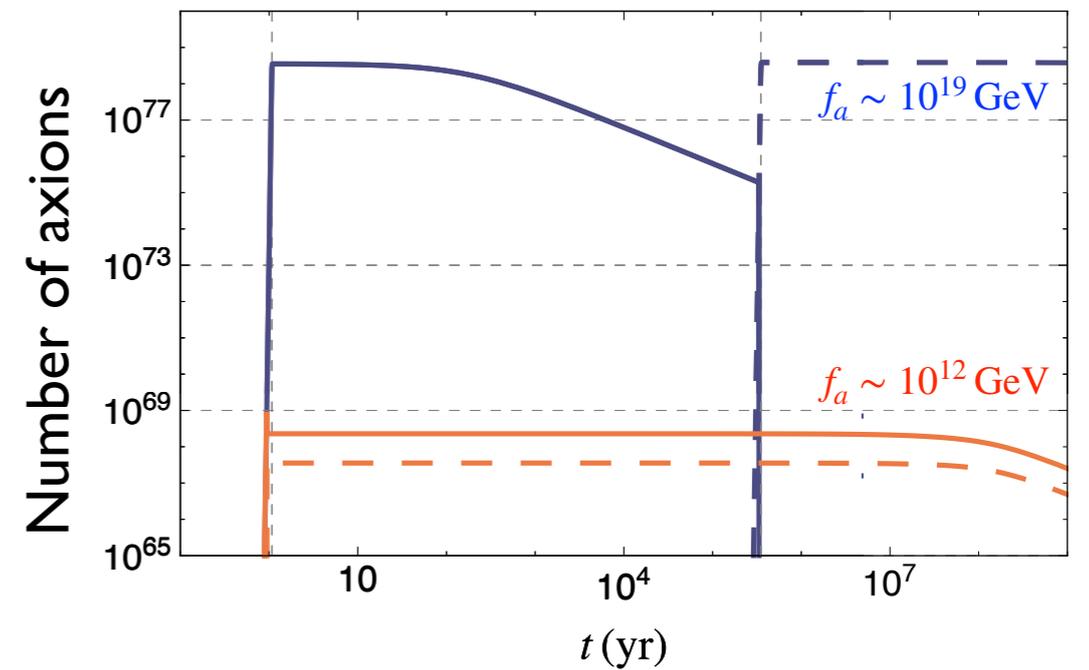


M. Baryakhtar, **MG**, R. Lasenby, O. Simon 2021

Larger self-interactions: $f_a \sim 10^{12} \text{ GeV}$

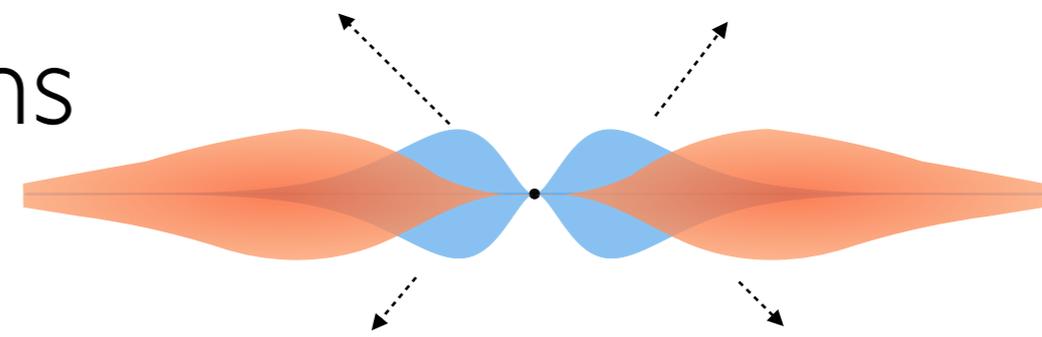
- Two levels populated simultaneously
- Axion radiation

Time evolution



A. Gruzinov, 1604.06422

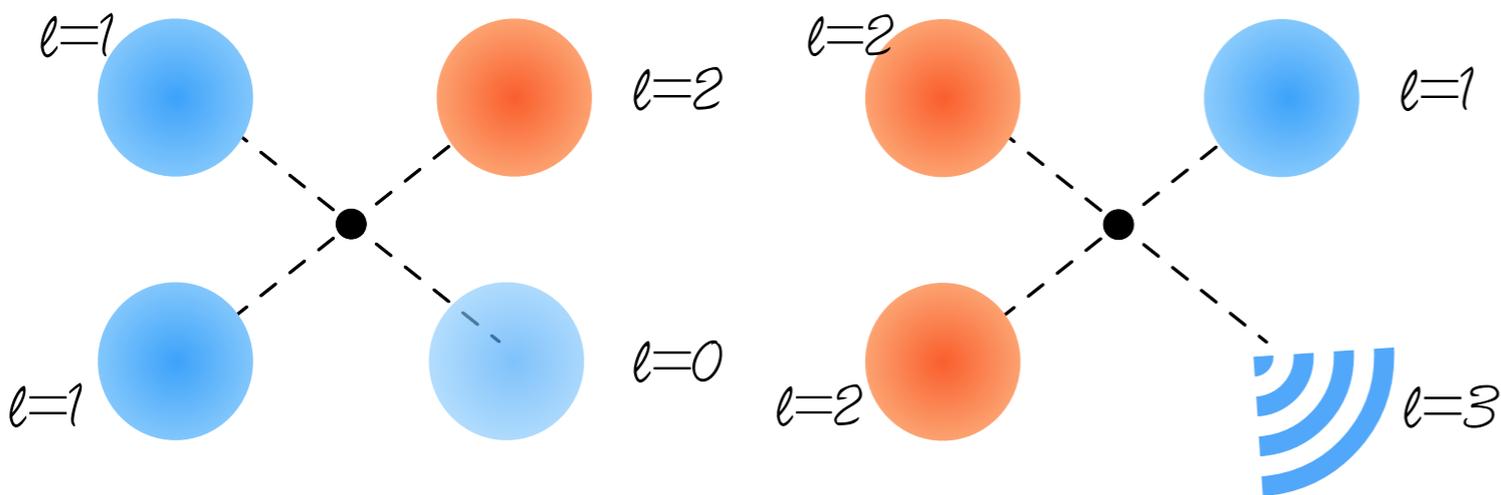
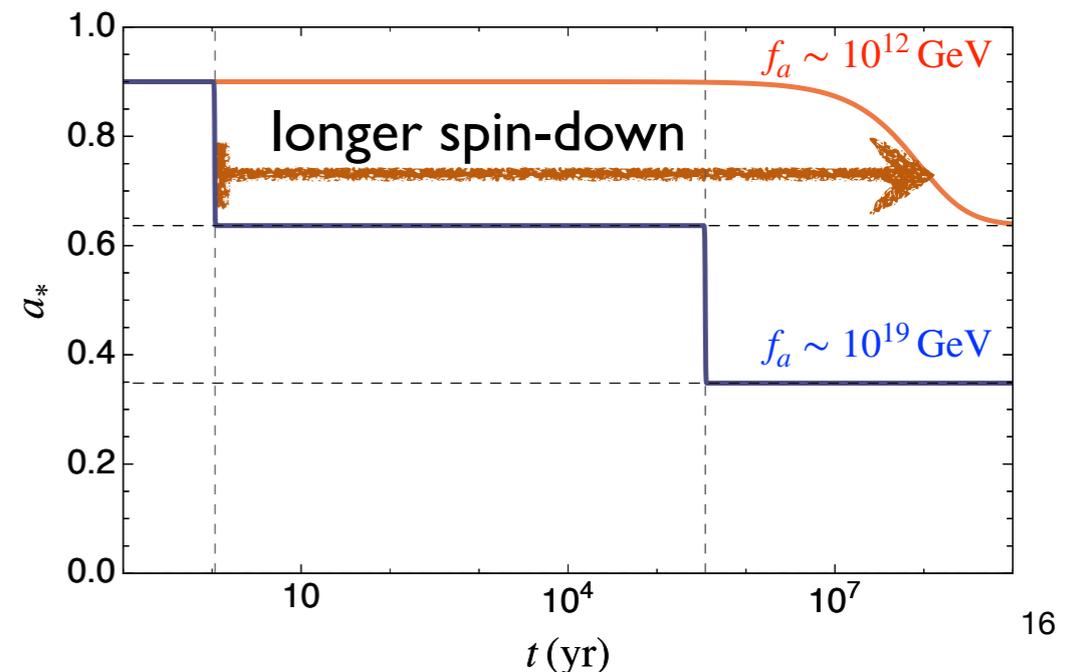
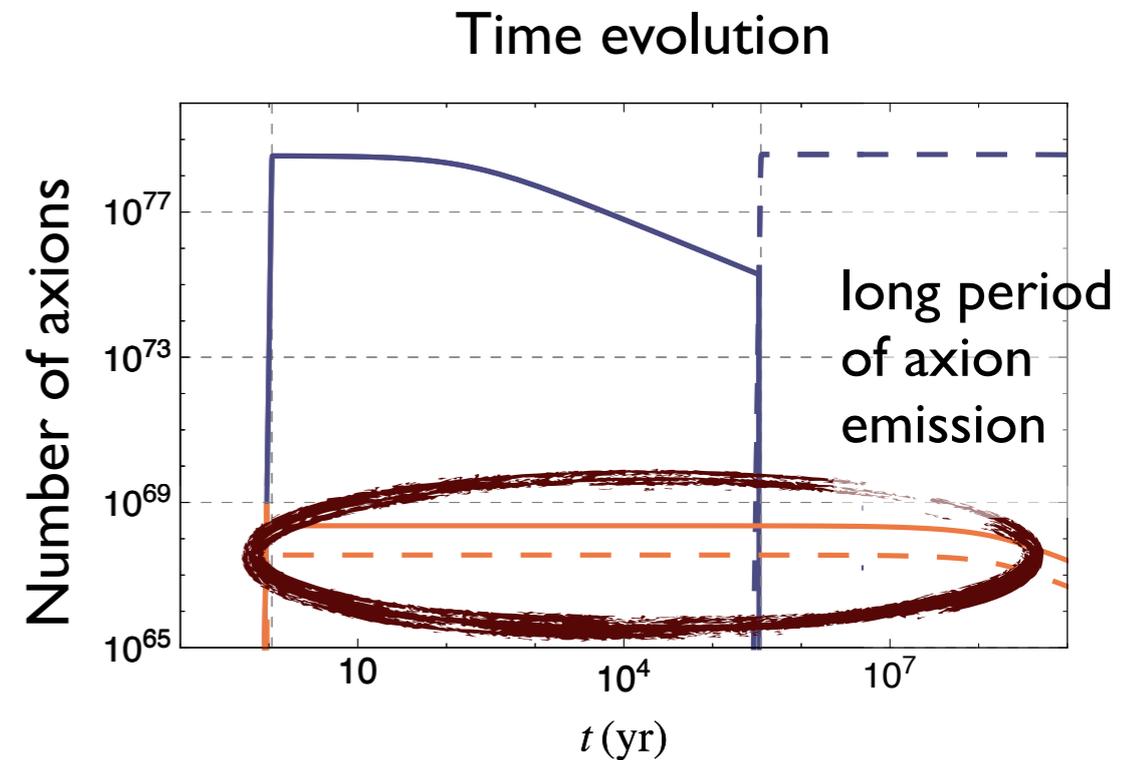
Self-Interactions



M. Baryakhtar, **MG**, R. Lasenby, O. Simon 2021

Larger self-interactions: $f_a \sim 10^{12} \text{ GeV}$

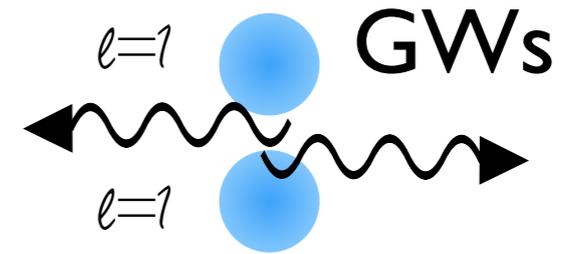
- Quasi-equilibrium with constant energy emission in scalar waves over \sim Hubble time
- Black hole spin-down time increased
- New gravitational wave emission: transitions



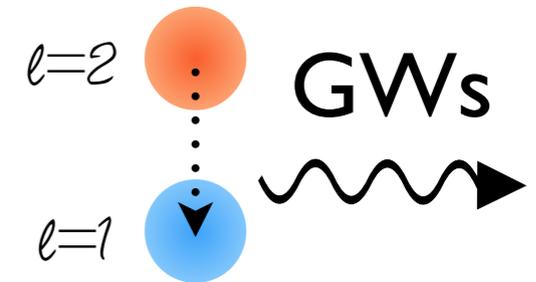
A. Gruzinov, 1604.06422

Signatures

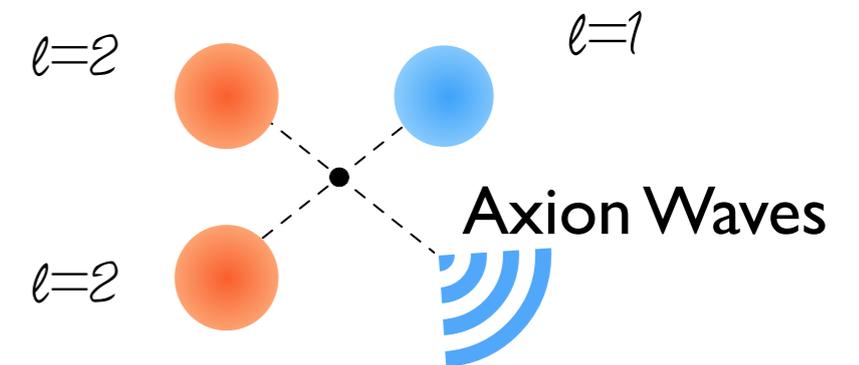
- Gravitational Waves from Annihilations



- Gravitational Waves from Transitions



- Axion Waves

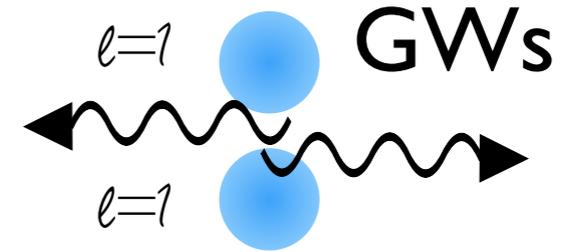


Constraints

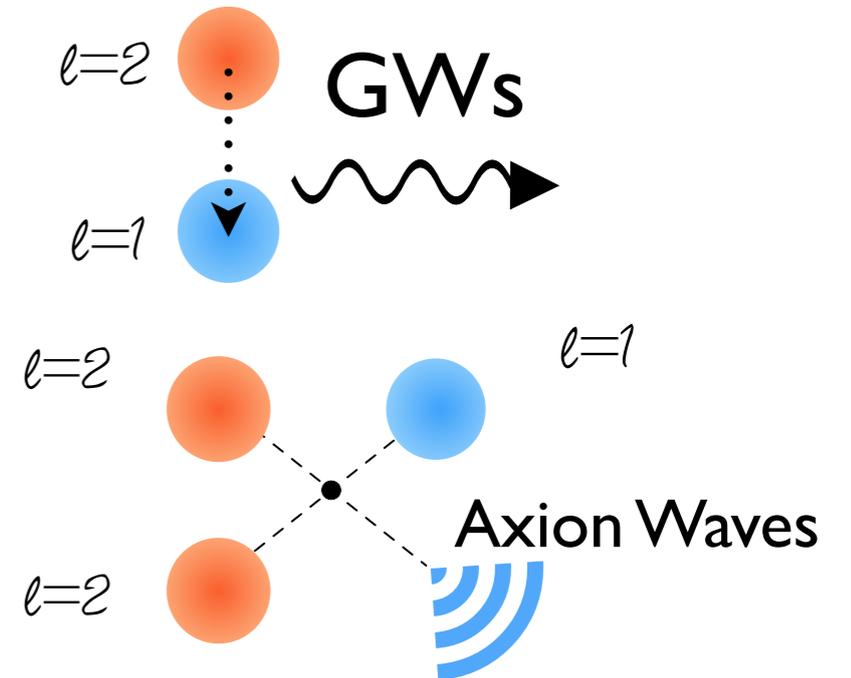
- Black Hole Spindown

Signatures

- Gravitational Waves from Annihilations



- Gravitational Waves from Transitions



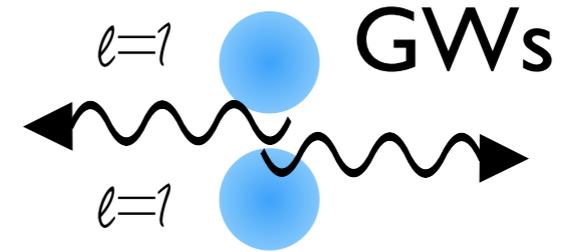
- Axion Waves

Constraints

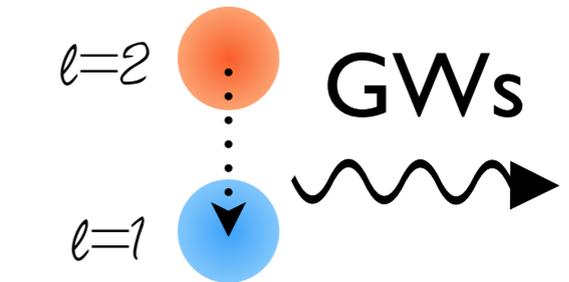
- Black Hole Spindown

Signatures

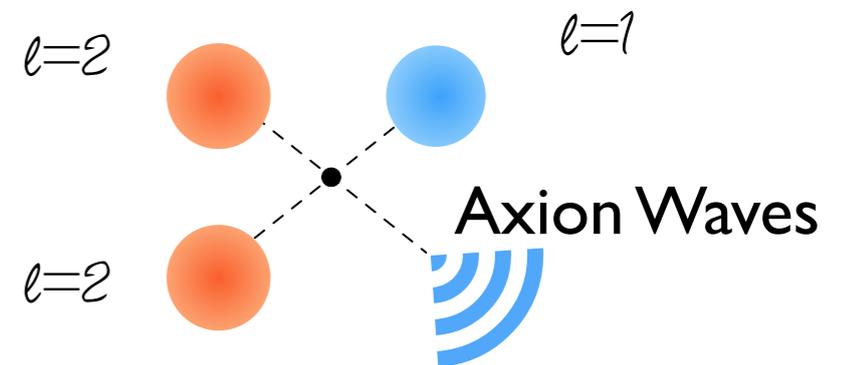
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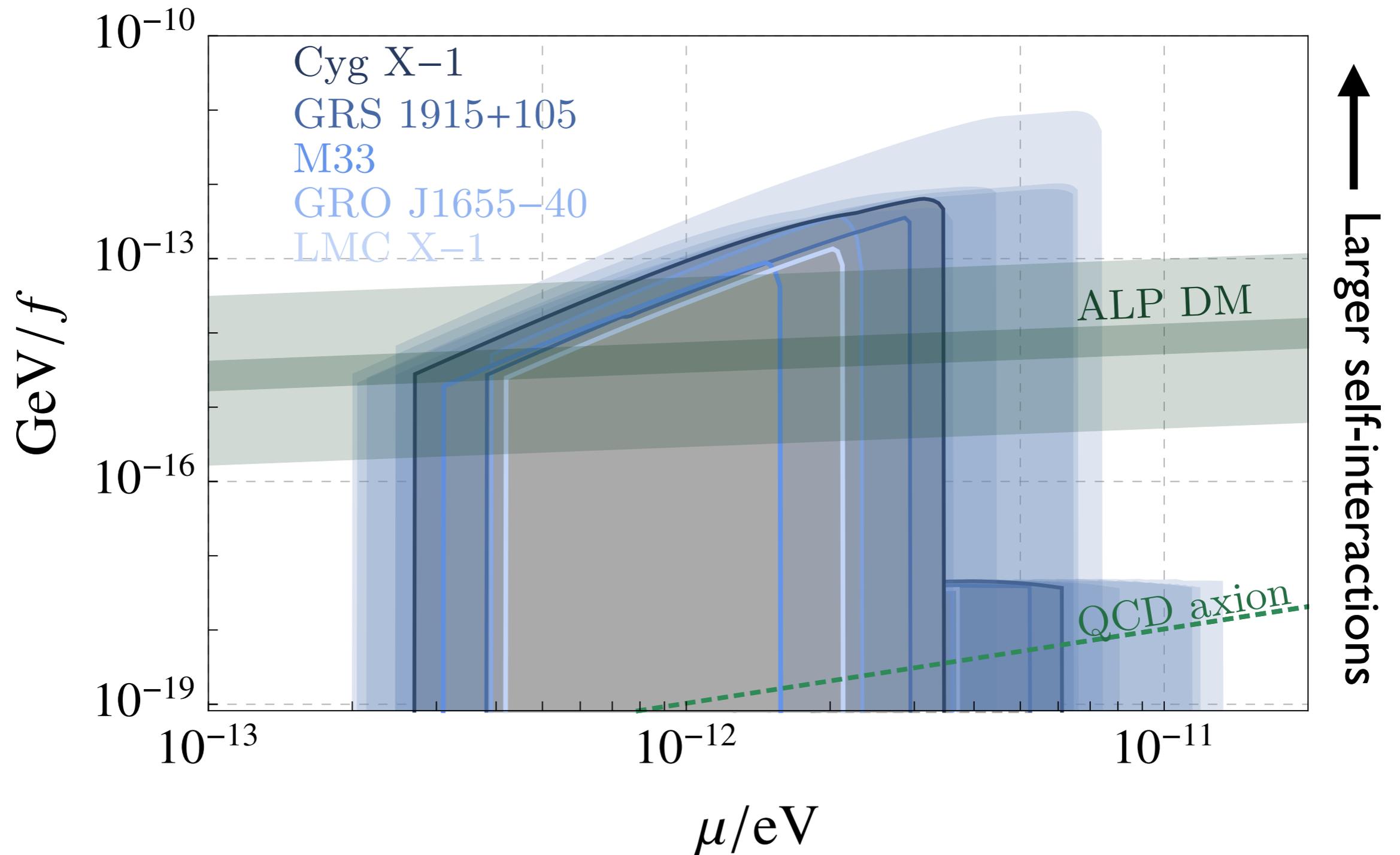
- Axion Waves



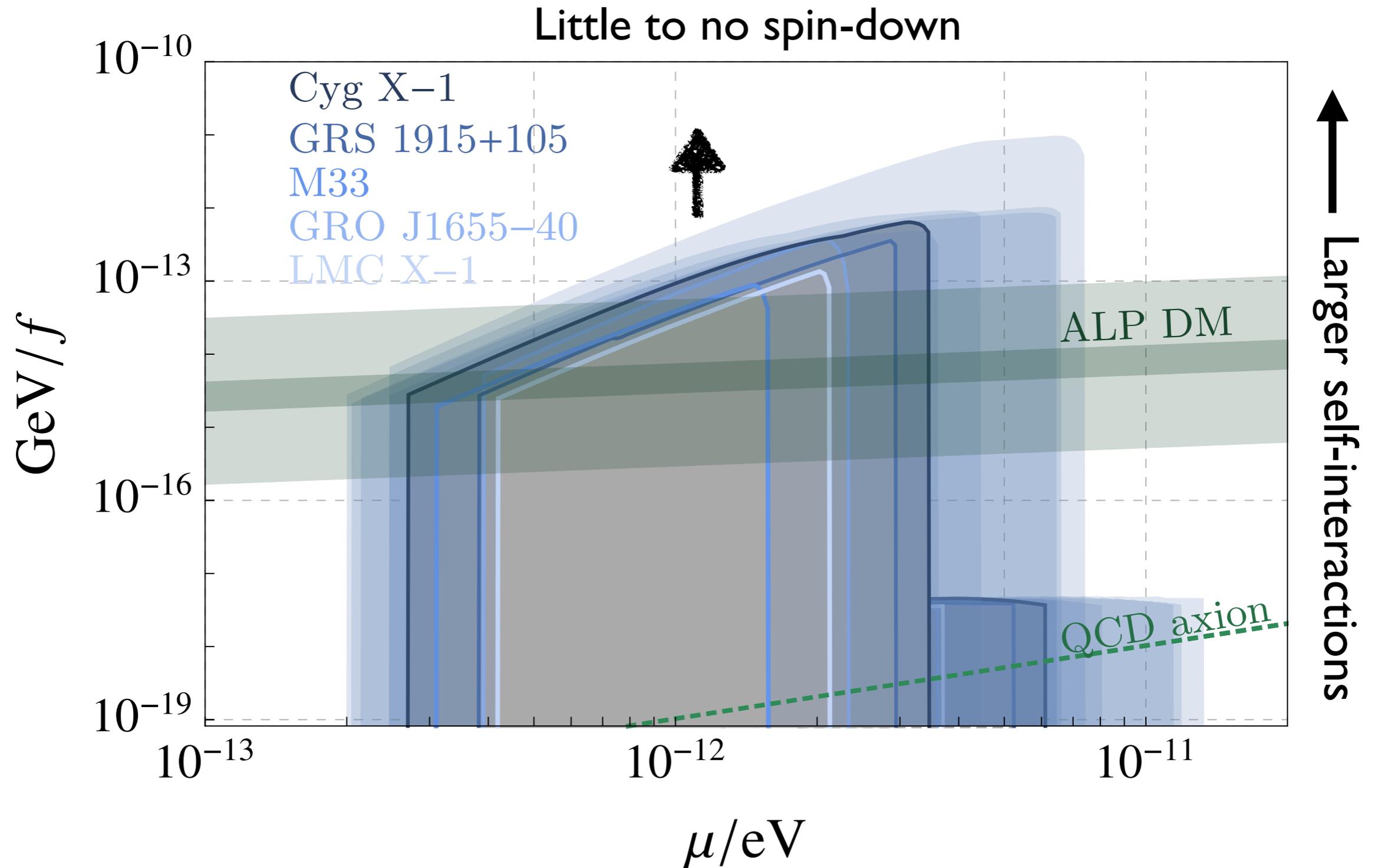
Constraints

- Black Hole Spindown

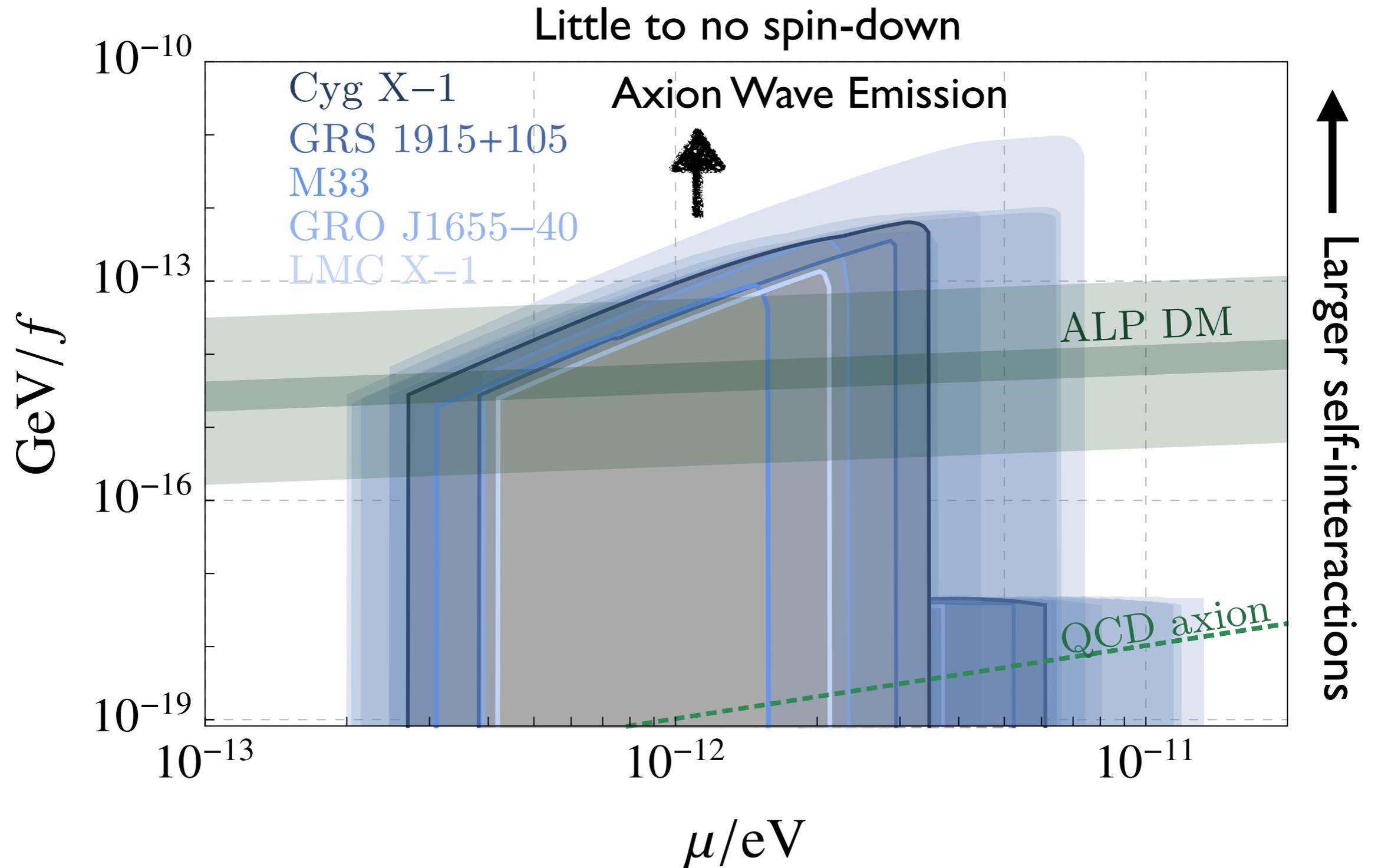
Black Hole Spin-down Constraints



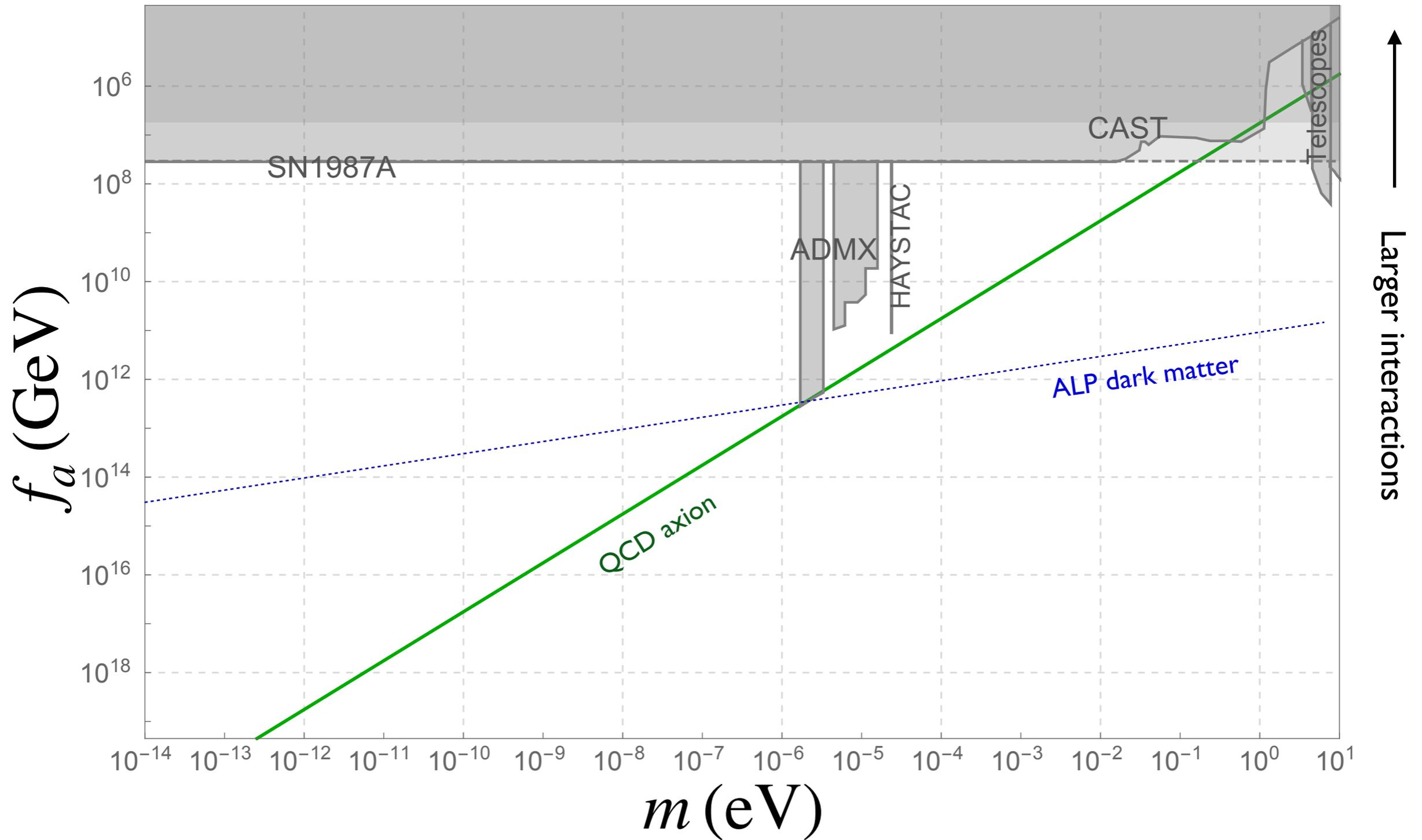
Black Hole Spin-down Constraints



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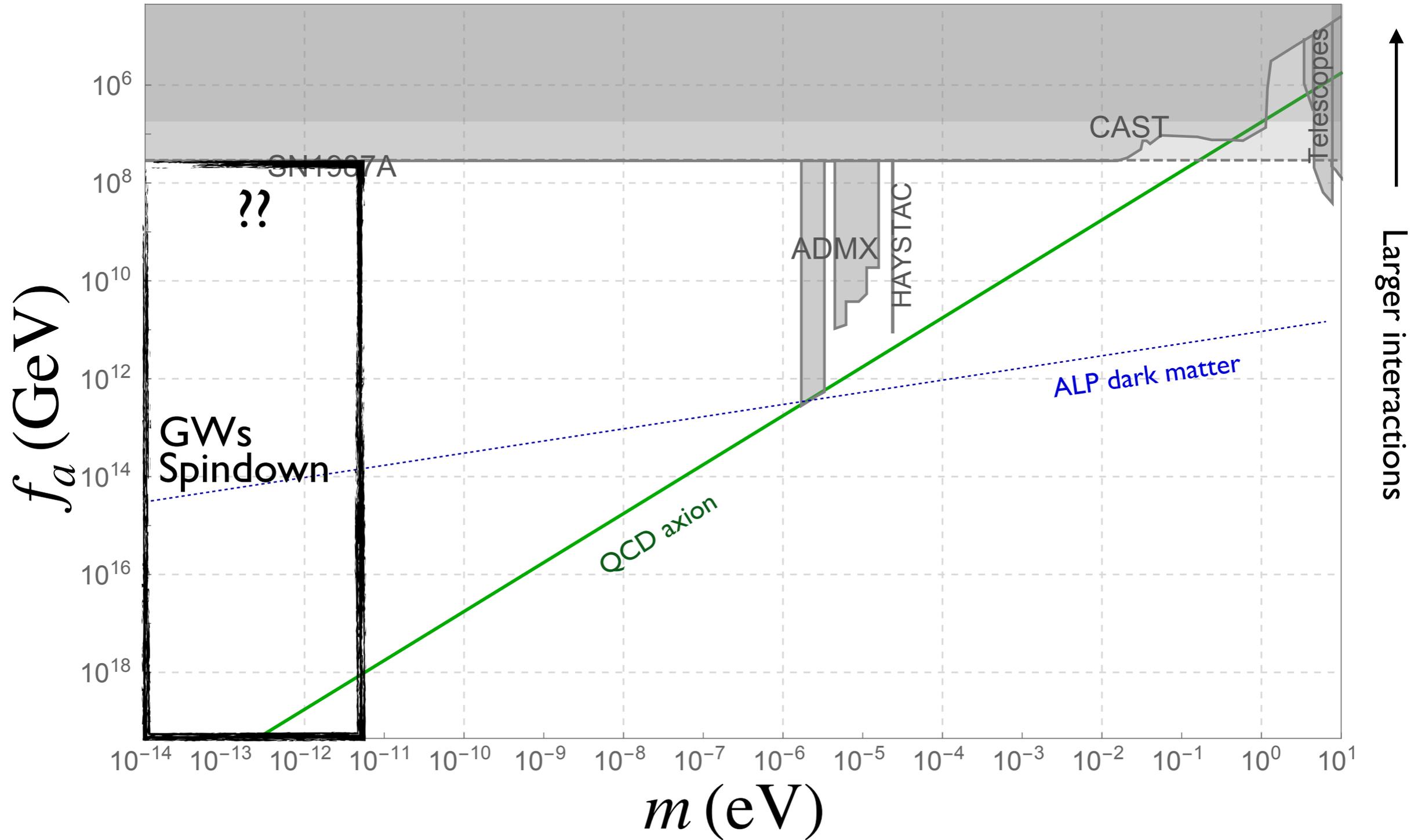


Axion Parameter Space

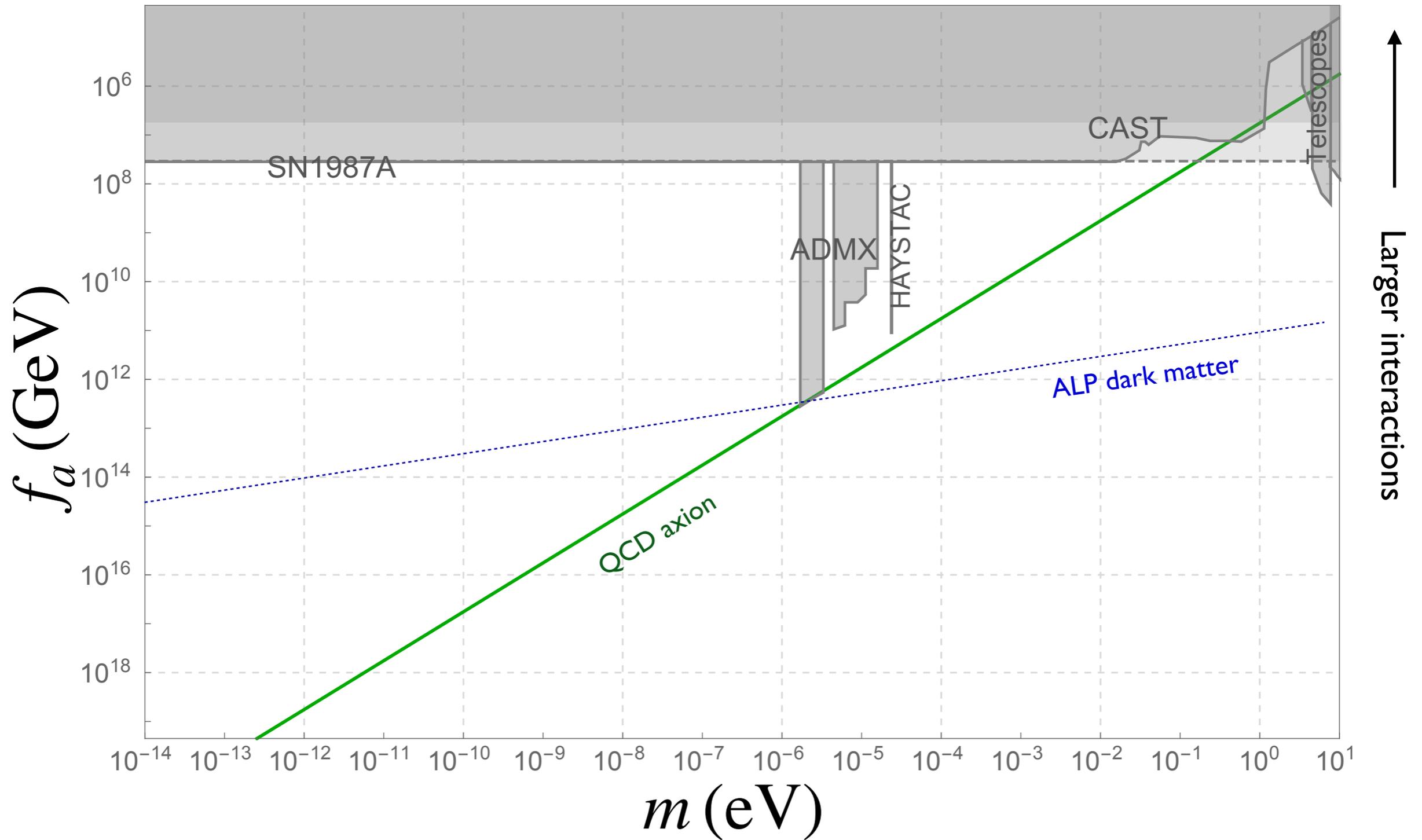


Axion Parameter Space

Before

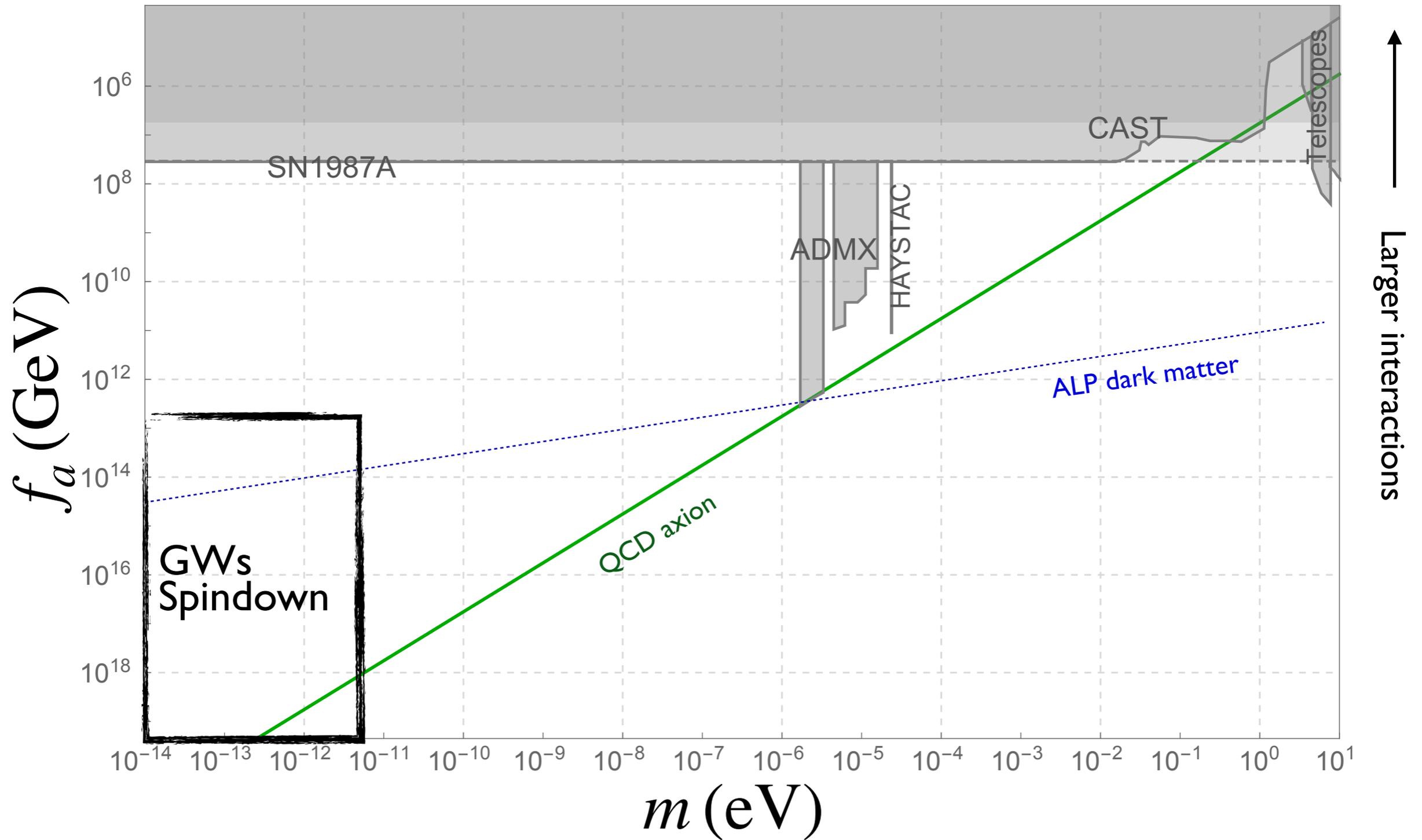


Axion Parameter Space



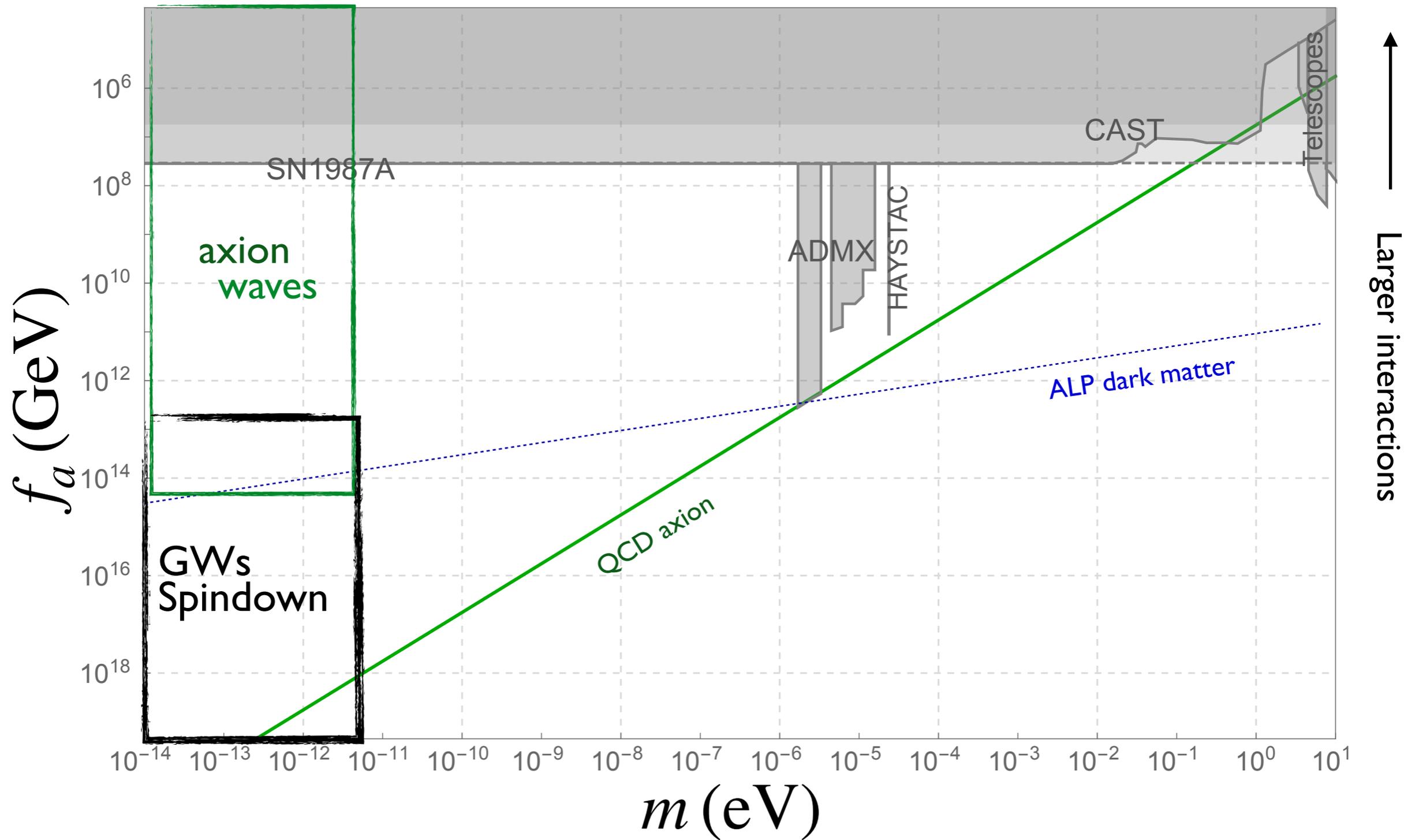
Axion Parameter Space

Our Result



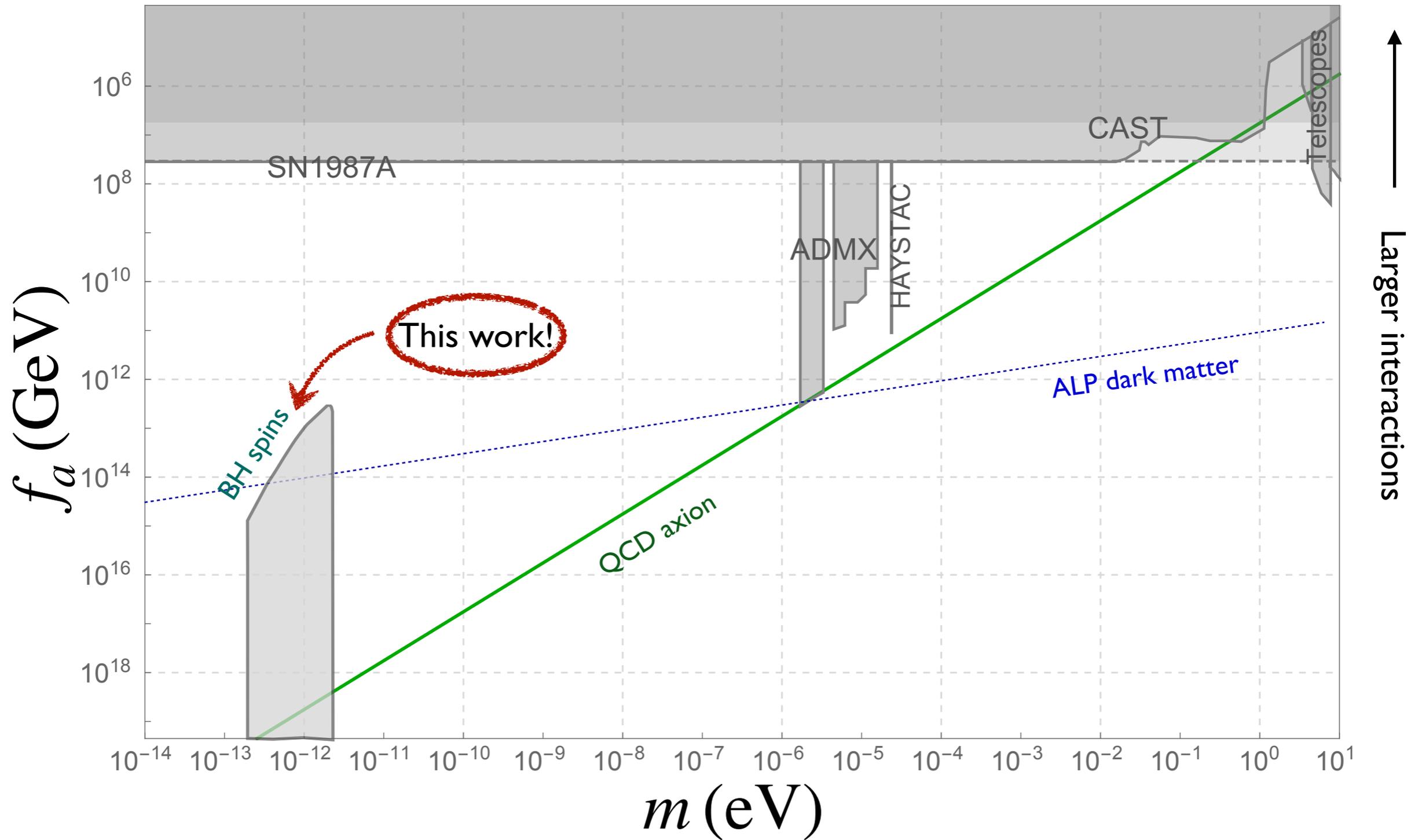
Axion Parameter Space

Our Result

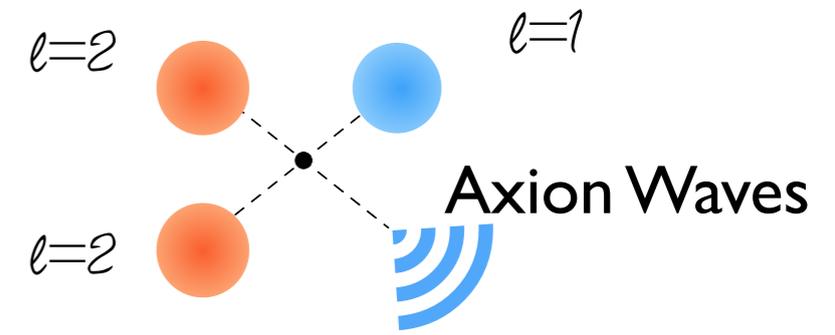


Axion Parameter Space

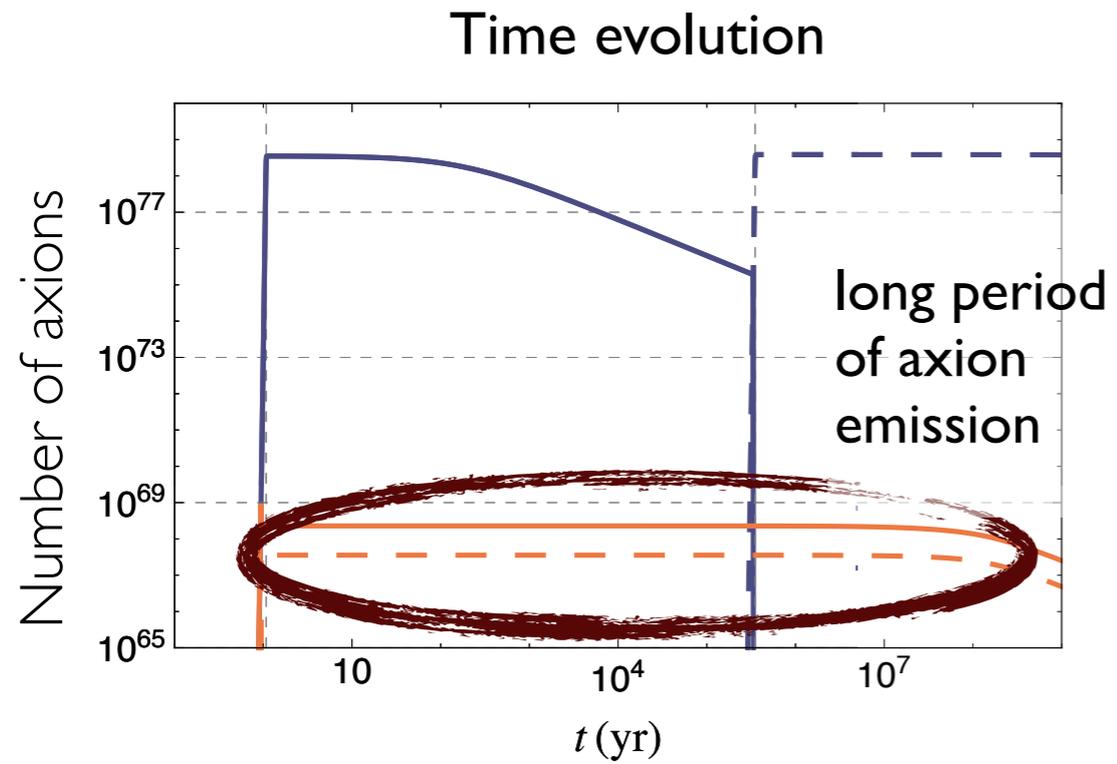
Our Result



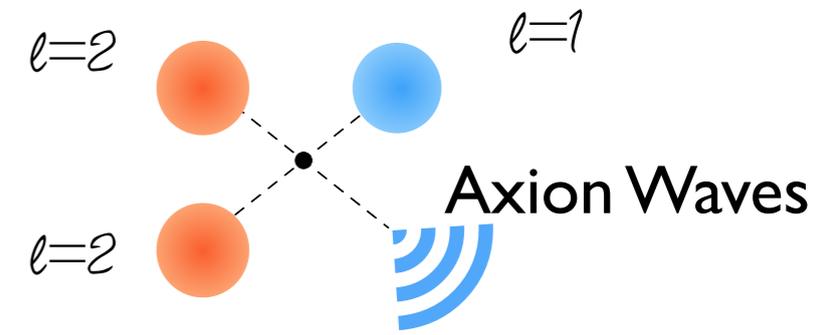
Axion Wave Emission



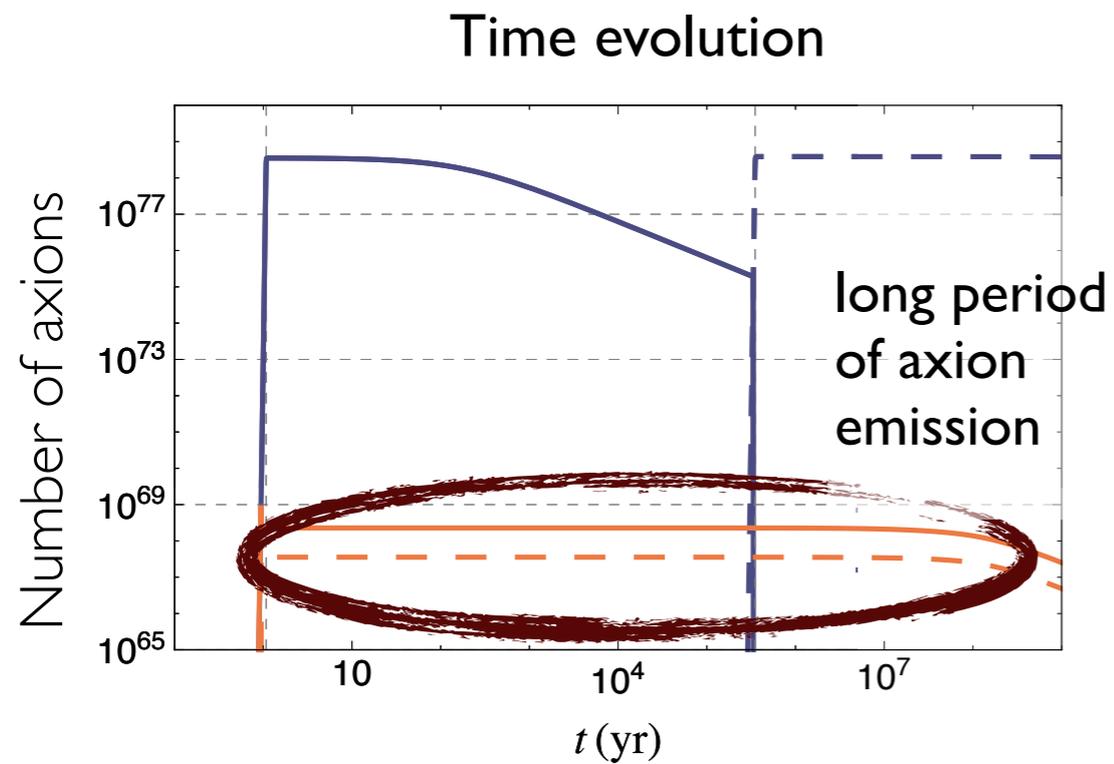
- Black Hole spins down slowly, emitting axion waves



Axion Wave Emission

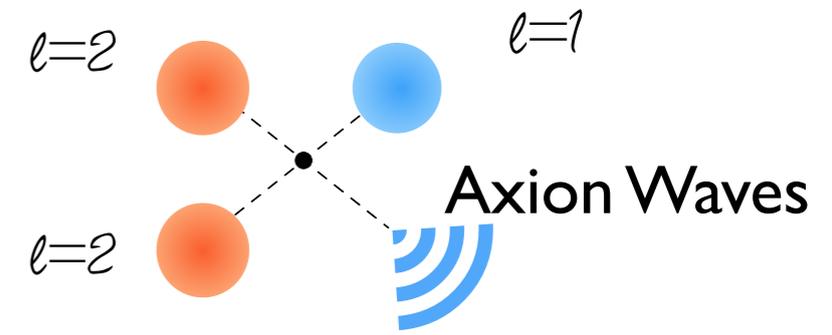


- Black Hole spins down slowly, emitting axion waves



- Directly detectable if coupled to the SM

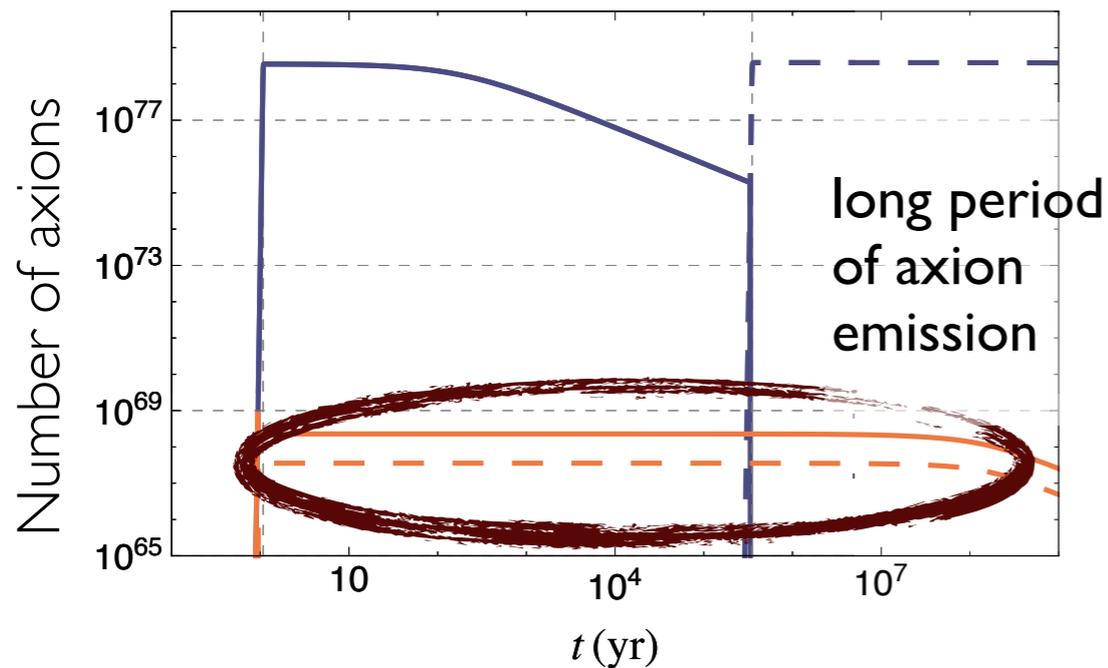
Axion Wave Emission



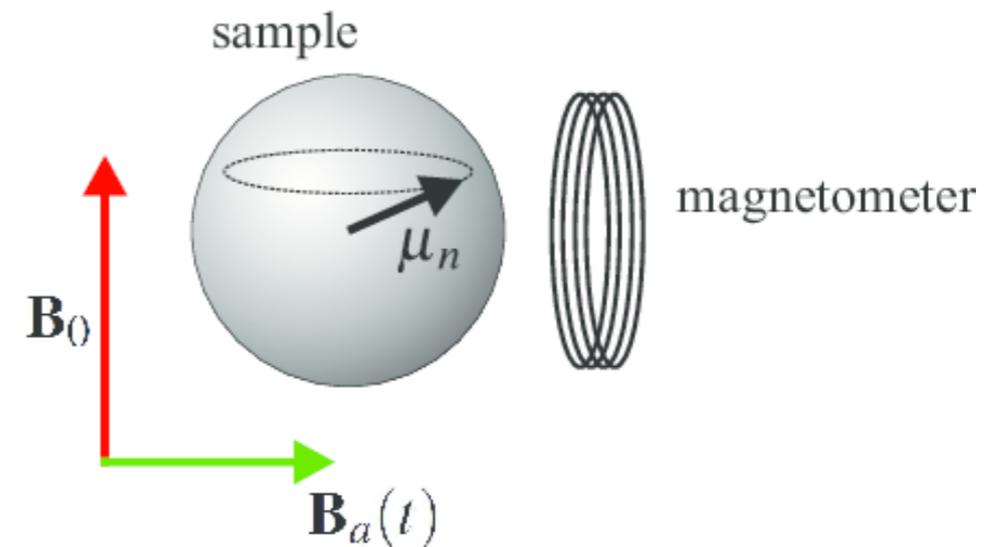
- Black Hole spins down slowly, emitting axion waves

- Axion field gradient acts like a magnetic field on particle spins

Time evolution



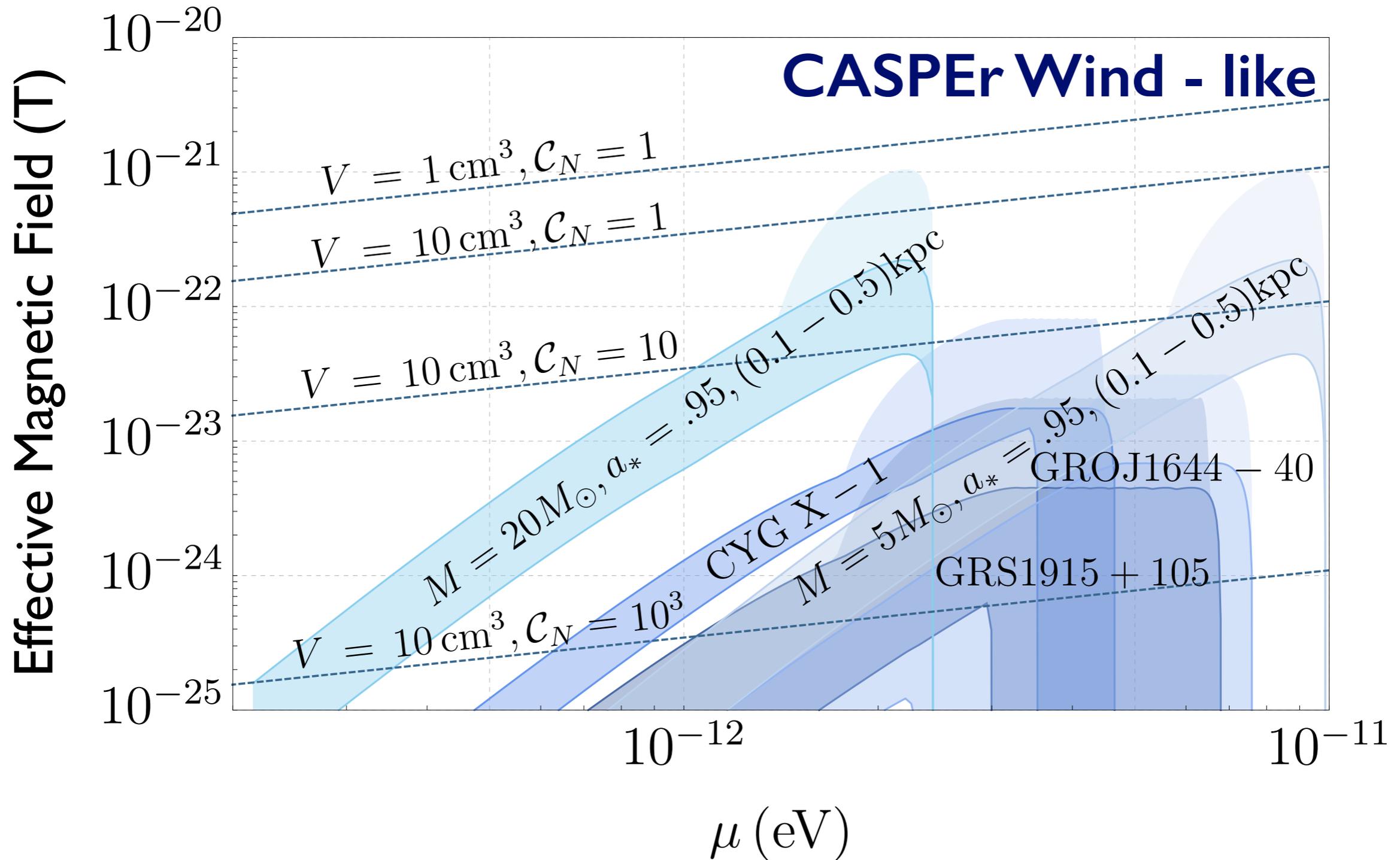
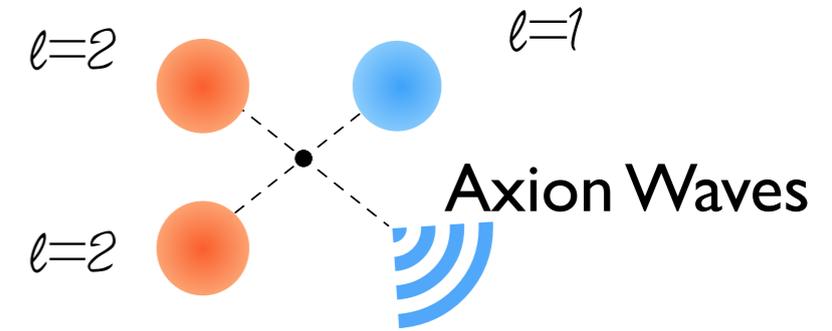
$$H_n \supset C \frac{\vec{\nabla} a}{f_a} \cdot \vec{\sigma}_N$$



- Directly detectable if coupled to the SM

CASPER Wind Experiment (2014)
Kimball et al (2017)

Axion Wave Emission

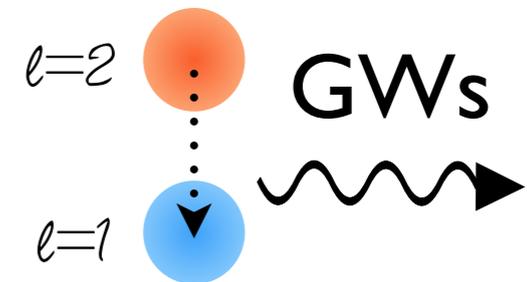


Conclusions

- Self-Interactions **dramatically affect** the evolution of the cloud

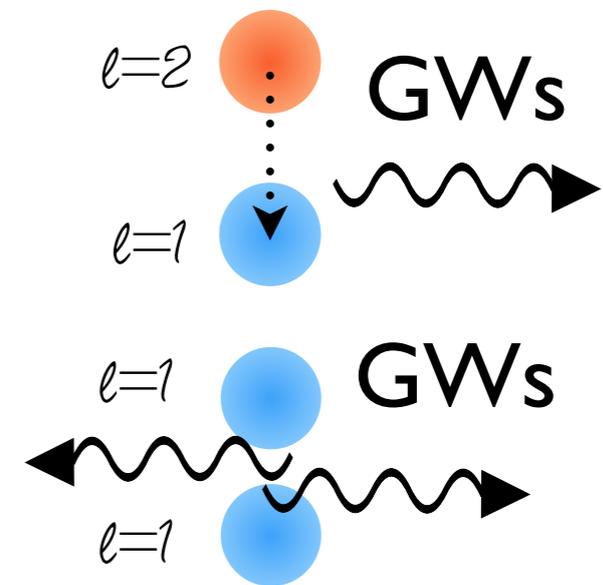
Conclusions

- Self-Interactions **dramatically affect** the evolution of the cloud
- Novel **GW transition signatures**: can be probed by **aLIGO + future observatories**



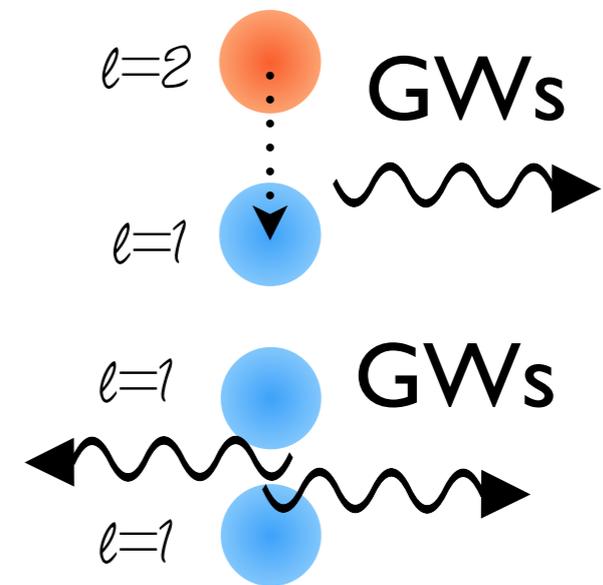
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- **GW annihilation signatures** are suppressed but still observable by **aLIGO**



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- **Constraints** from spin measurements are **modified** and do not apply for appreciable self-interactions



Conclusions

- Self-Interactions **dramatically affect** the evolution of the cloud
- Novel **GW transition signatures**: can be probed by **aLIGO + future observatories**
- **GW annihilation signatures** are suppressed but still observable by **aLIGO**
- **Constraints** from spin measurements are **modified** and do not apply for appreciable self-interactions
- Instead Black Holes emit **axion radiation** which can be detected by upcoming experiments, such as **CASPEr-Wind**

