

# Semileptonic $B$ -decays with a vector final state

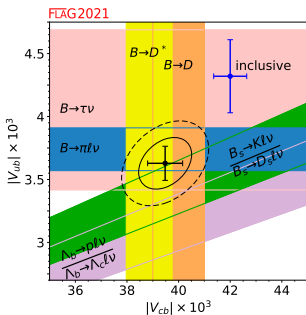
---

Andrew Lytle (FNAL-MILC collaboration)  
University of Illinois @ Urbana-Champaign

04.22.22  
USQCD All Hands Meeting  
Zoom@MIT

# Intro & Motivation

- Semileptonic decays are a rich source of information for determining CKM matrix elements.
- Lattice data a critical source of input for testing the CKM paradigm.



- With new experimental and theoretical data on the horizon, these are interesting times!

- Overall aim: Precision ( $\sim 1\%$ ) determination of a range of  $B_{(s)}$  (and  $D_{(s)}$ ) semileptonic form factors, of direct relevance for current and upcoming experimental programs.
- Here we discuss extending this program to decays with vector final states (specifically the processes  $B_{(s)} \rightarrow D_{(s)}^*$ ).
- Support/enhance physics of  $B \rightarrow D^*$  with FNAL heavy quarks on asqtad (and hisq) sea. 2105.14019

# Outline

---

- Intro & Motivation
- FNAL/MILC all-HISQ semileptonic decays
  - ▶ Calculation framework
  - ▶ Preliminary results w/ pseudoscalar final state
- Including vector final states
- Summary

# FNAL-MILC allhisq working group

---

Carleton DeTar

Elvira Gámiz

Steve Gottlieb

William Jay

Aida El-Khadra

Andreas Kronfeld

Jim Simone

Alejandro Vaquero

## Heavy quarks

---

Treatment of  $c$  and especially  $b$  quarks challenging in lattice simulation due to lattice artifacts which grow as  $(am_h)^n$

- May use an effective theory framework to handle the  $b$  quark.
  - ▶ Fermilab method, RHQ, OK, NRQCD
  - ▶ Pros: Solves problem w/  $am_h$  artifacts.
  - ▶ Cons: Requires matching, can still have  $ap$  artifacts.
- Also possible to use relativistic fermion provided  $a$  is sufficiently small  $am_c \ll 1$ ,  $am_b < 1$ .
  - ▶ Use improved actions e.g.  $\mathcal{O}(a^2) \rightarrow \mathcal{O}(\alpha_s a^2)$
  - ▶ Pros: Absolutely normalised current, straightforward continuum extrap.
  - ▶ Cons: Numerically expensive, extrapolate  $m_h \rightarrow m_b$ .

## allhisq simulations

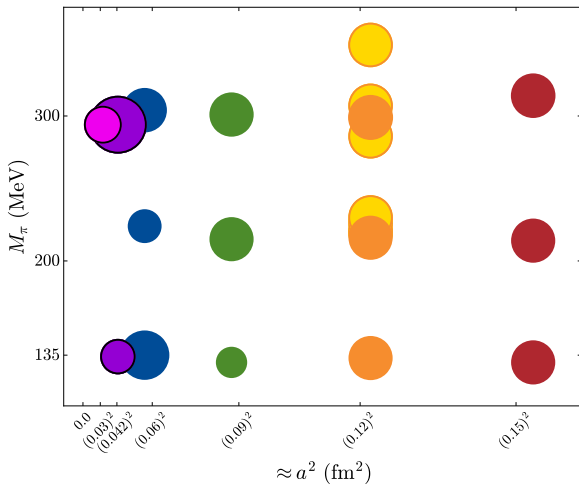
---

- Here we simulate *all* quarks with the HISQ action.
- Unified treatment for wide range of  $B_{(s)}$  (and  $D_{(s)}$ ) to pseudoscalar transitions
  - ▶  $B_{(s)} \rightarrow D_{(s)}$
  - ▶  $B_{(s)} \rightarrow K$
  - ▶  $B \rightarrow \pi$
- Ensembles with (HISQ) sea quarks down to physical at each lattice spacing.
- Enables correlated studies of ff *ratios*.

See our 2021 Lattice proceeding for more details! 2111.05184

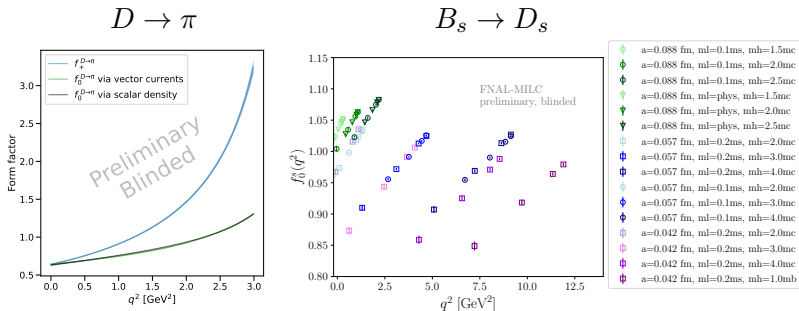
- HISQ fermion action.
  - ▶ Discretization errors begin at  $\mathcal{O}(\alpha_s a^2)$ .
  - ▶ Designed for simulating heavy quarks ( $m_c$  and higher at current lattice spacings).
- Symanzik-improved gauge action, takes into account  $\mathcal{O}(N_f \alpha_s a^2)$  effects of HISQ quarks in sea. [0812.0503]
- Multiple lattice spacings down to  $\sim 0.042$  (now 0.03) fm.
- Effects of  $u/d$ ,  $s$ , and  $c$  quarks in the sea.
- Multiple light-quark input parameters down to physical pion mass.
  - ▶ Chiral fits.
  - ▶ Reduce statistical errors.





- Use a heavy valence mass  $h$  as a proxy for the  $b$  quark.
- Work at a range of  $m_h$ , with  $am_c < am_h \lesssim 1$  on each ensemble. On sufficiently fine ensembles,  $m_h$  is near to  $m_b$  (e.g.  $m_b$  at  $am_h \approx 0.65$  on  $a = 0.03$  fm).
- Map out physical dependence on  $m_h$ , remove discretisation effects  $\sim (am_h)^{2n}$  using information from several ensembles. Extrapolate results  $a^2 \rightarrow 0, m_h \rightarrow m_b$ .

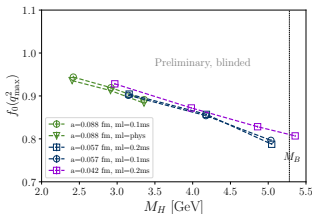
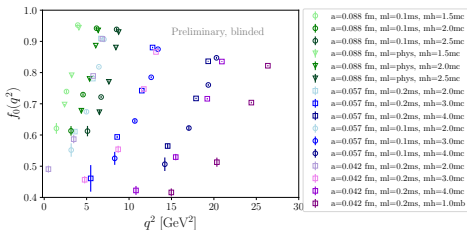
# Update on allHISQ $P \rightarrow P$



- Will Jay's  $D$ -decay analysis ( $D \rightarrow \pi, K$   $D_s \rightarrow K$ ) at an advanced stage. Percent-level targets achieved.
- For  $B$  decays, vector operator renorm. and chiral/continuum extrapolations remain.

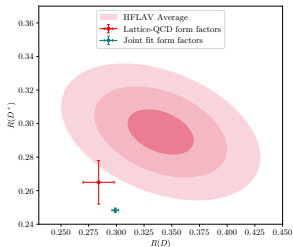
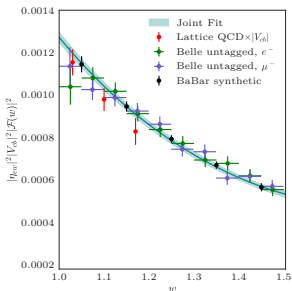
# Update on allHISQ $P \rightarrow P$

$$B_s \rightarrow K$$



- Good statistical precision out to  $p=300$ .
- Tree-level disc. artifacts removed in right-hand figure.

- Pioneering FNAL-MILC calculation beyond zero-recoil using FNAL  $b$  and  $c$  quarks.

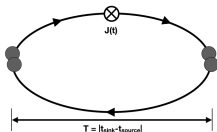


Figs. courtesy A. Vaquero

- FNAL-HISQ analysis in progress (Vaquero).
- all-HISQ approach normalizes currents exactly (Ward identities), reducing an important source of uncertainty.

## Extending allHISQ to vector final states

Structurally, calculation is similar to  $P \rightarrow P$  – need to modify spin-taste at source/sink/current.



	$\mathcal{O}_{H(s)}$	$\mathcal{O}_{P/V}$	$\mathcal{O}_J$
$f_+$	$\gamma_5 \otimes \gamma_5$	$\gamma_5 \otimes \gamma_5$	$\gamma_i \otimes 1$
$f_0$	$\gamma_0 \gamma_5 \otimes \gamma_0 \gamma_5$	$\gamma_5 \otimes \gamma_5$	$\gamma_0 \otimes \gamma_0$
$V$	$\gamma_5 \otimes \gamma_1$	$\gamma_1 \otimes \gamma_1$	$\gamma_3 \otimes 1$
$A_0$	$\gamma_5 \otimes \gamma_5 \gamma_1$	$\gamma_1 \otimes \gamma_1$	$\gamma_5 \otimes \gamma_5$
$A_1$	$\gamma_5 \otimes \gamma_5 \gamma_3$	$\gamma_3 \otimes \gamma_3$	$\gamma_3 \gamma_5 \otimes \gamma_5$
$A_2$	$\gamma_5 \otimes \gamma_5 \gamma_1$	$\gamma_1 \otimes \gamma_1$	$\gamma_1 \gamma_5 \otimes \gamma_5$

Normalize vector (axial vector) current using PCVC (PCAC).

## Summary & Conclusion

---

- Semileptonic decays are crucial sources of information for fundamental physics, e.g.  $|V_{ub}|$  and  $|V_{cb}|$ . Lattice results needed to support experimental physics programs at LHCb and Belle II.
  - ▶ Understand inclusive/exclusive discrepancies.
  - ▶ Pure SM predictions for  $R$ -ratios.
- The FNAL-MILC allHISQ- $b$  program aims to produce high quality form factor data for a range of phenomenologically important channels.
- Propose to extend these calculations to vector final states, to obtain  $B_{(s)} \rightarrow D_{(s)}^*$  form factors over the full kinematic range.

Thank you!