

USQCD All Hands Meeting  
April 22, 2022

# Nuclear Physics from the Standard Model

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# Recent work

## Spectroscopy

Baryon-baryon  
interactions

[PRD 103 \(2021\), 054508](#)

$m_\pi \sim 450$  MeV

Variational  
nucleon-nucleon

[arXiv:2108.10835 \[hep-lat\]](#)

$m_\pi \sim 806$  MeV

## Matrix elements

Triton axial  
charge

[PRD 103 \(2021\), 074511](#)

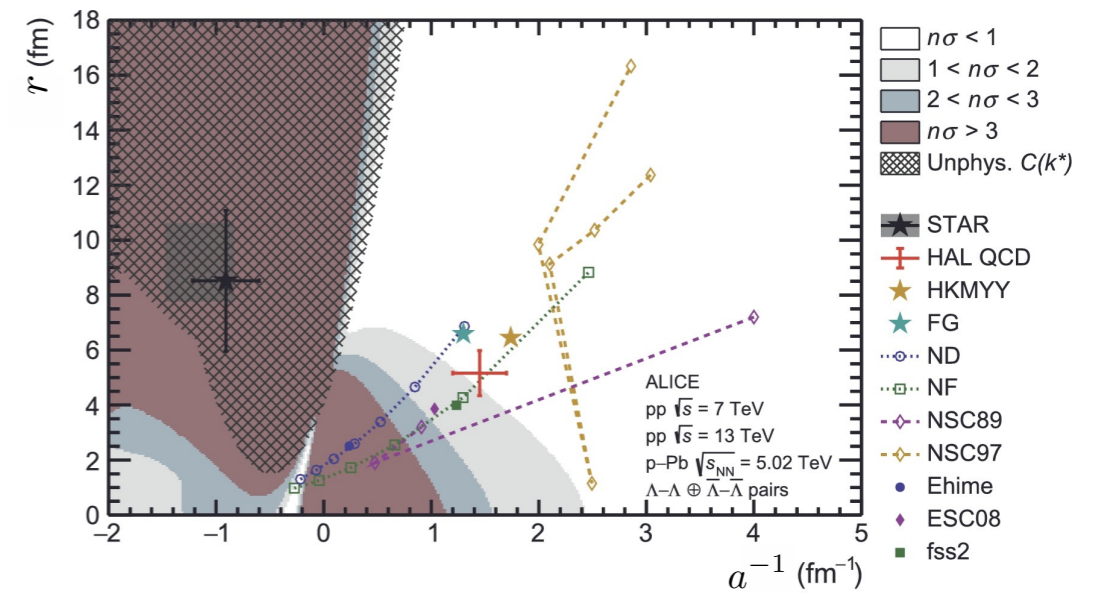
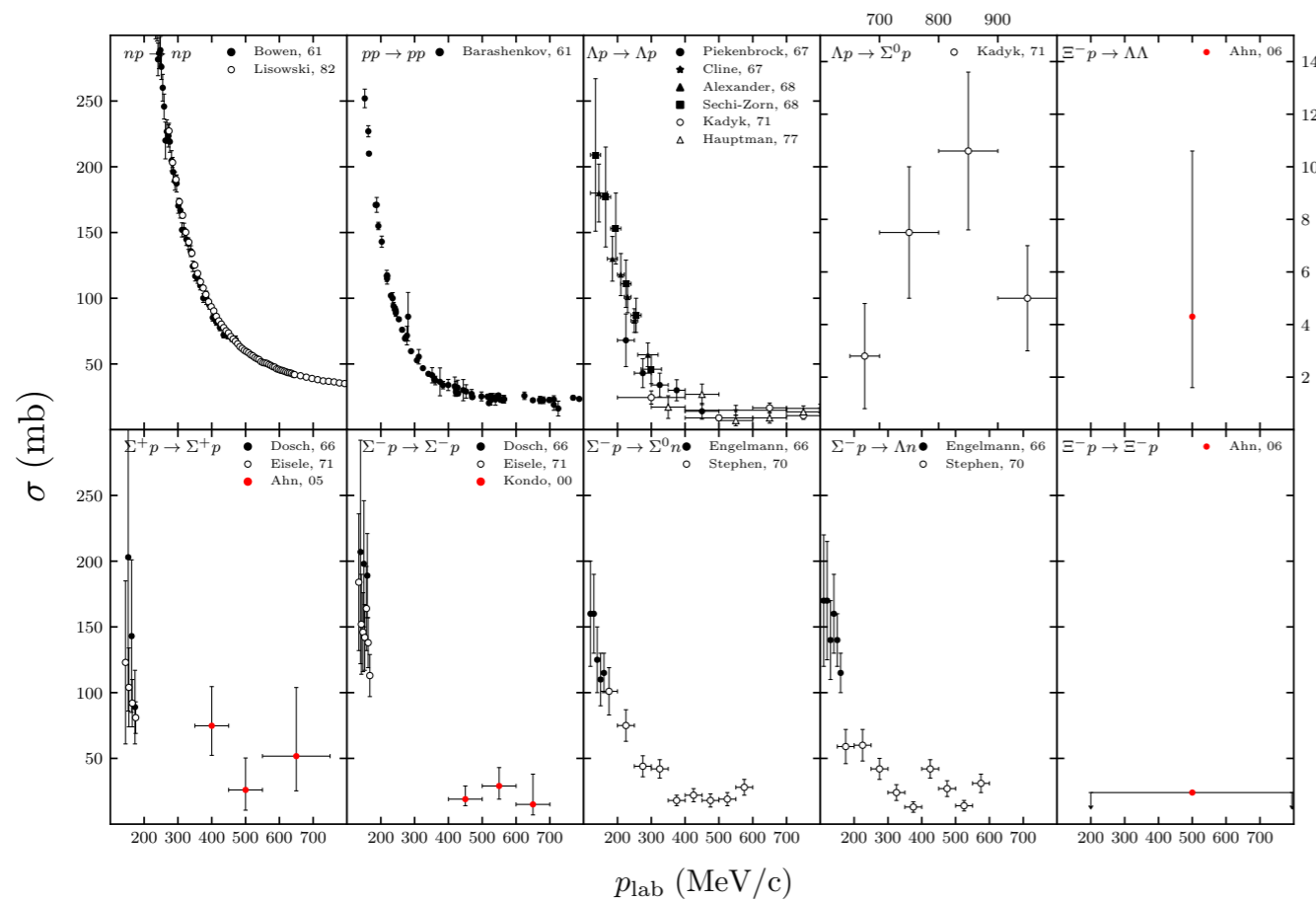
$m_\pi \sim 450$  MeV

Momentum  
fraction of  $^3\text{He}$

[PRL 126 \(2021\), 202001](#)

$m_\pi \sim 806$  MeV

# Baryon-baryon interactions



ALICE Collaboration, [PLB 797 \(2019\)](#)

updated from Dover and Feshbach, [Ann. Phys. 198 \(1990\)](#)

$$\mathbf{8} \otimes \mathbf{8} = \mathbf{27} \oplus \mathbf{8}_s \oplus \mathbf{1} \oplus \overline{\mathbf{10}} \oplus \mathbf{10} \oplus \mathbf{8}_a$$

Wagman et al. [NPLQCD], [PRD 96 \(2017\)](#)

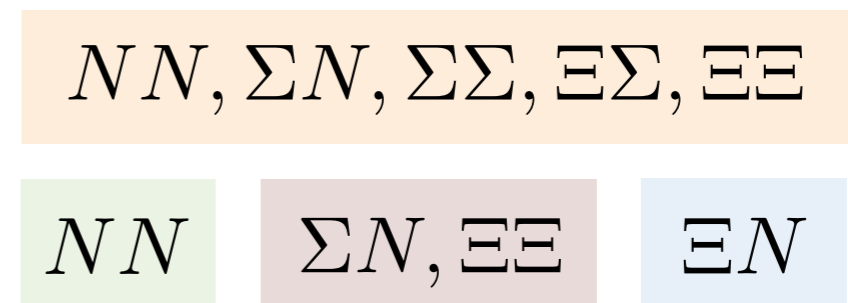
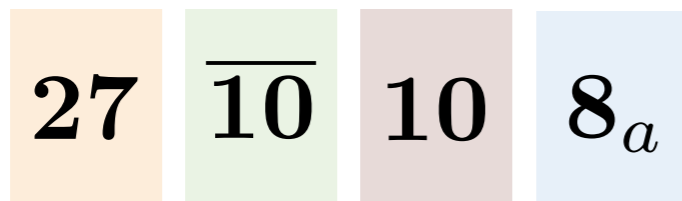
$$m_u = m_d = m_s$$

$$m_\pi = m_K \sim 806 \text{ MeV}$$

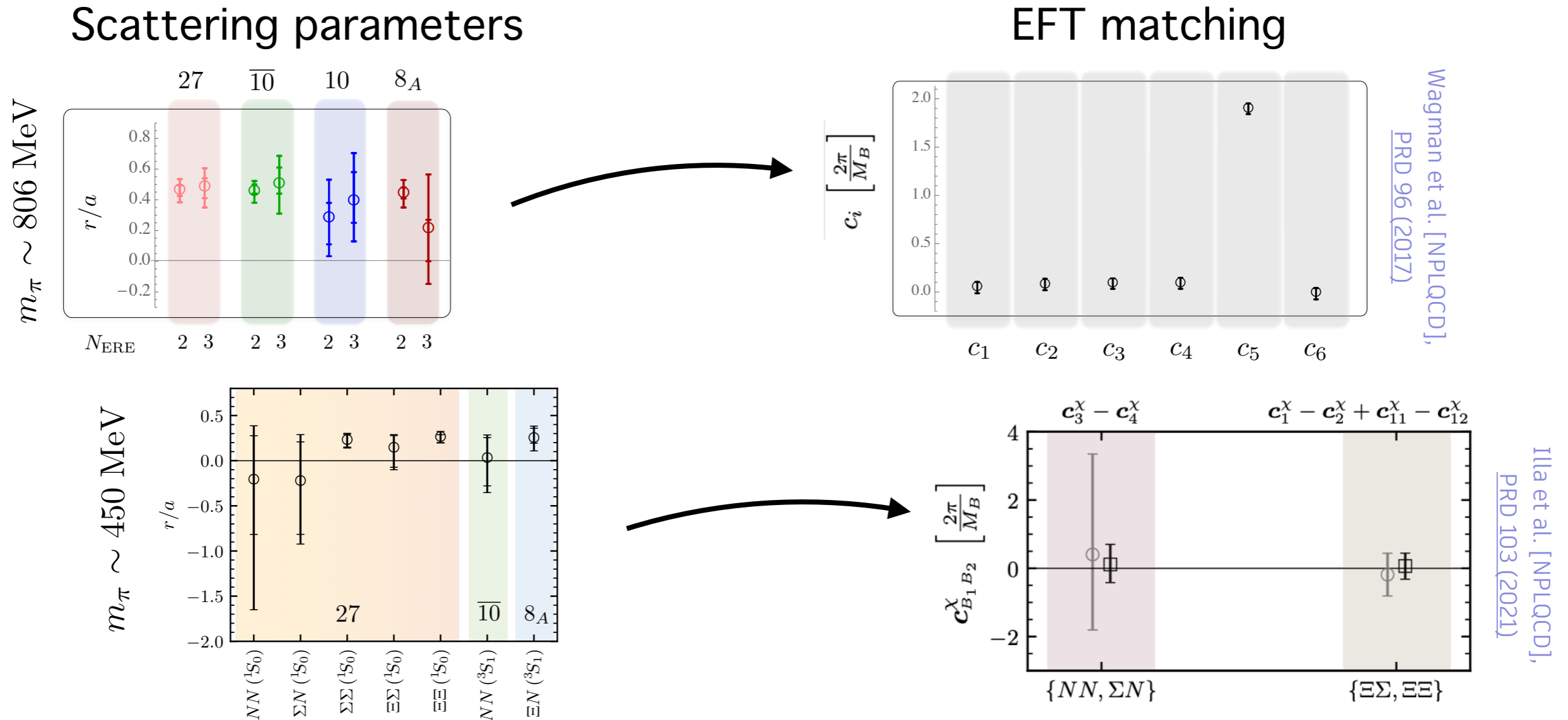
Illa et al. [NPLQCD], [PRD 103 \(2021\)](#)

$$m_u = m_d \neq m_s$$

$$m_\pi \sim 450 \text{ MeV}, m_K \sim 600 \text{ MeV}$$



# Baryon-baryon interactions



Heavier-than-physical quark masses

Only one lattice spacing  $\rightarrow$  possible discretization effects? [Green et al., PRL 127 \(2021\)](#)

Asymmetrical correlation functions  $\rightarrow$  excited state contamination?

# Baryon-baryon interactions

First steps towards a variational study of the baryon-baryon interaction

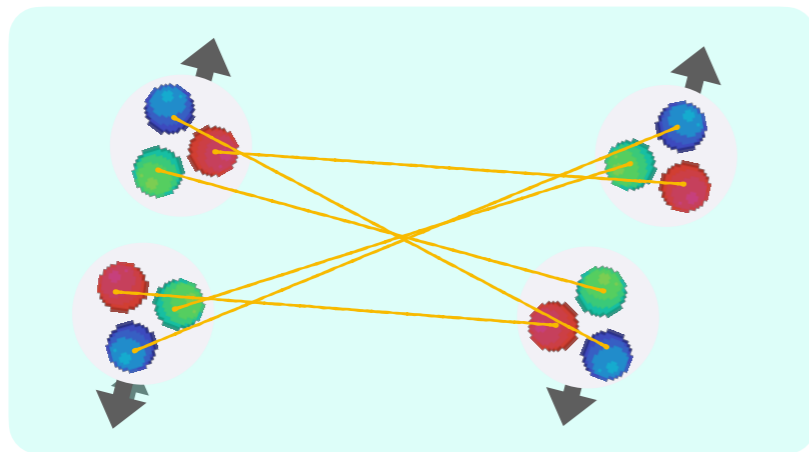
Francis et al., [PRD 99 \(2019\)](#)

Green et al., [PRL 127 \(2021\)](#)

H dibaryon

Hörz et al., [PRC 103 \(2021\)](#)

NN systems



Matrix of dibaryon-like operators with different boost and back-to-back momenta



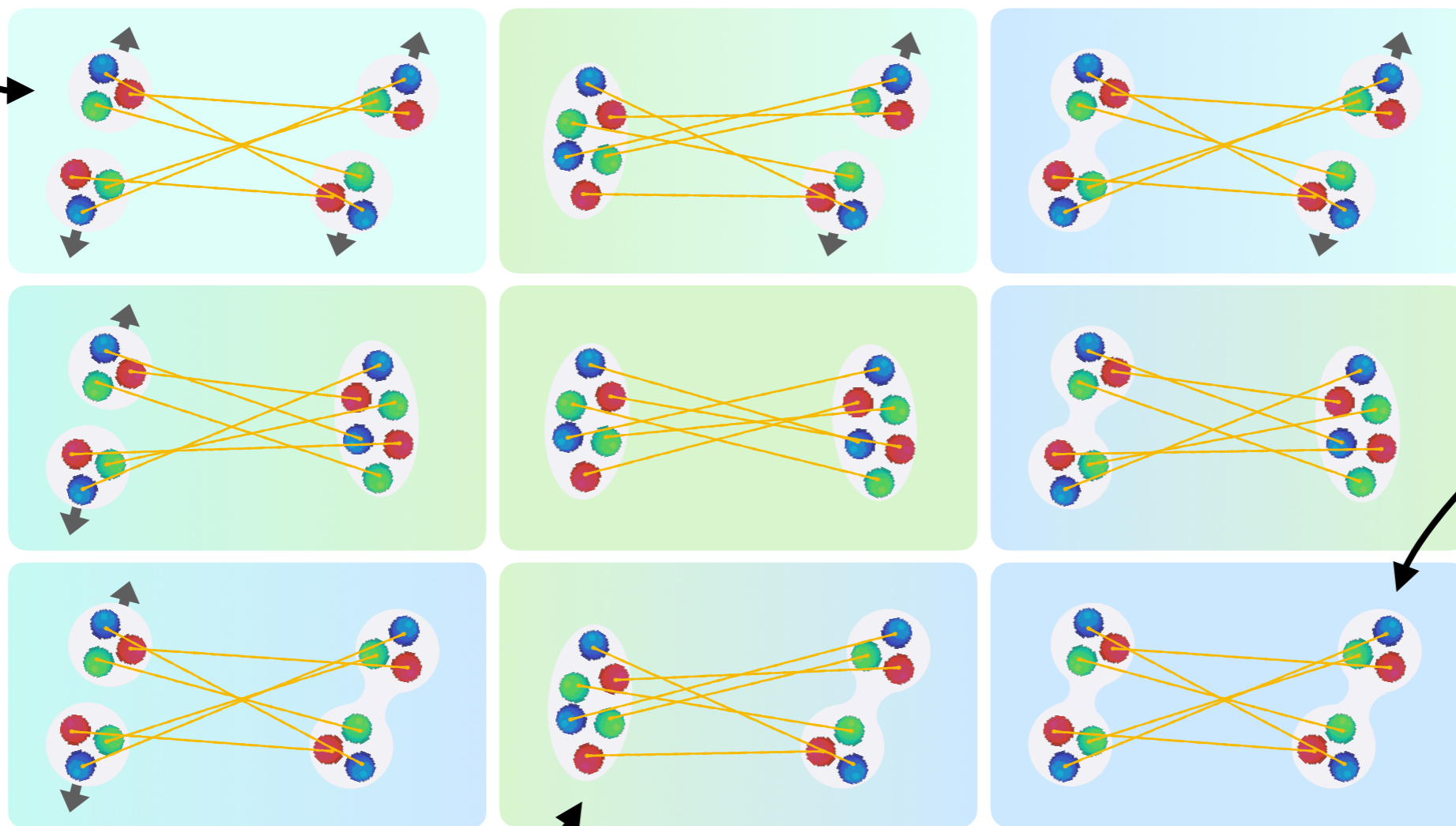
Discrepancies with previous results

Maybe dibaryon operators have small overlap with deeply-bound states?

# Baryon-baryon interactions

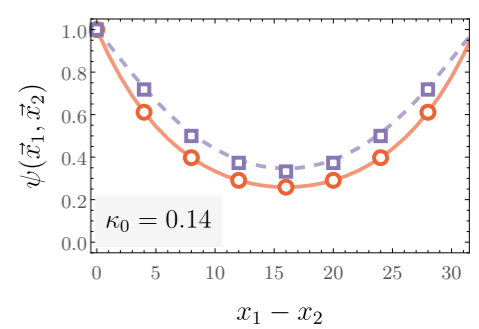
Extend previous variational studies by including hexaquark and quasi-local operators [Amarasinghe et al. \[NPLQCD\], arXiv:2108.10835 \[hep-lat\]](#)

Dibaryon  $\psi(\vec{x}_1, \vec{x}_2) = e^{i\vec{k}\cdot(\vec{x}_1 - \vec{x}_2)}$



Quasi-local

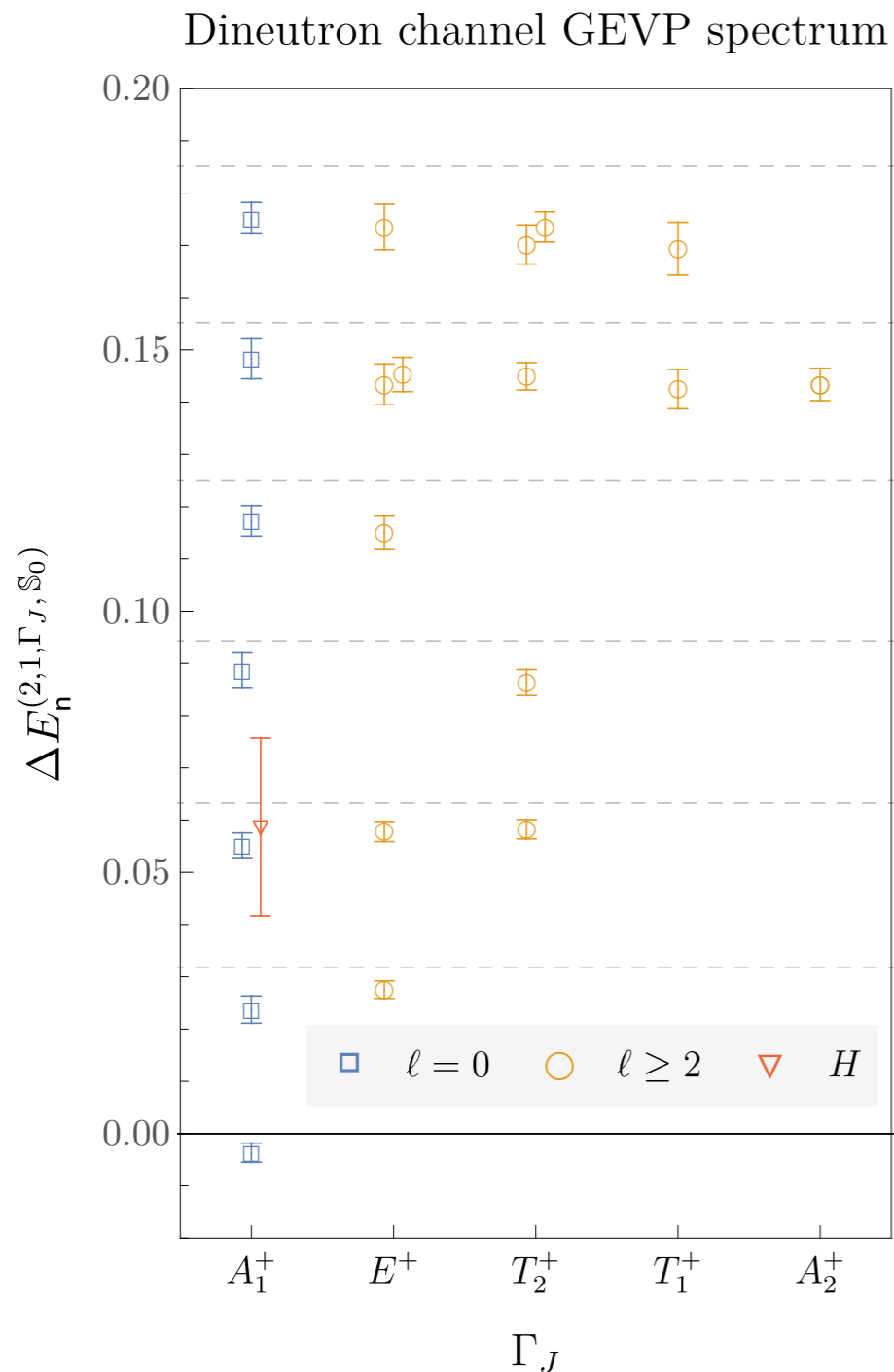
$$\psi(\vec{x}_1, \vec{x}_2) = \sum_n e^{-\kappa_d |\vec{x}_1 - \vec{x}_2 + nL|}$$



Hexaquark

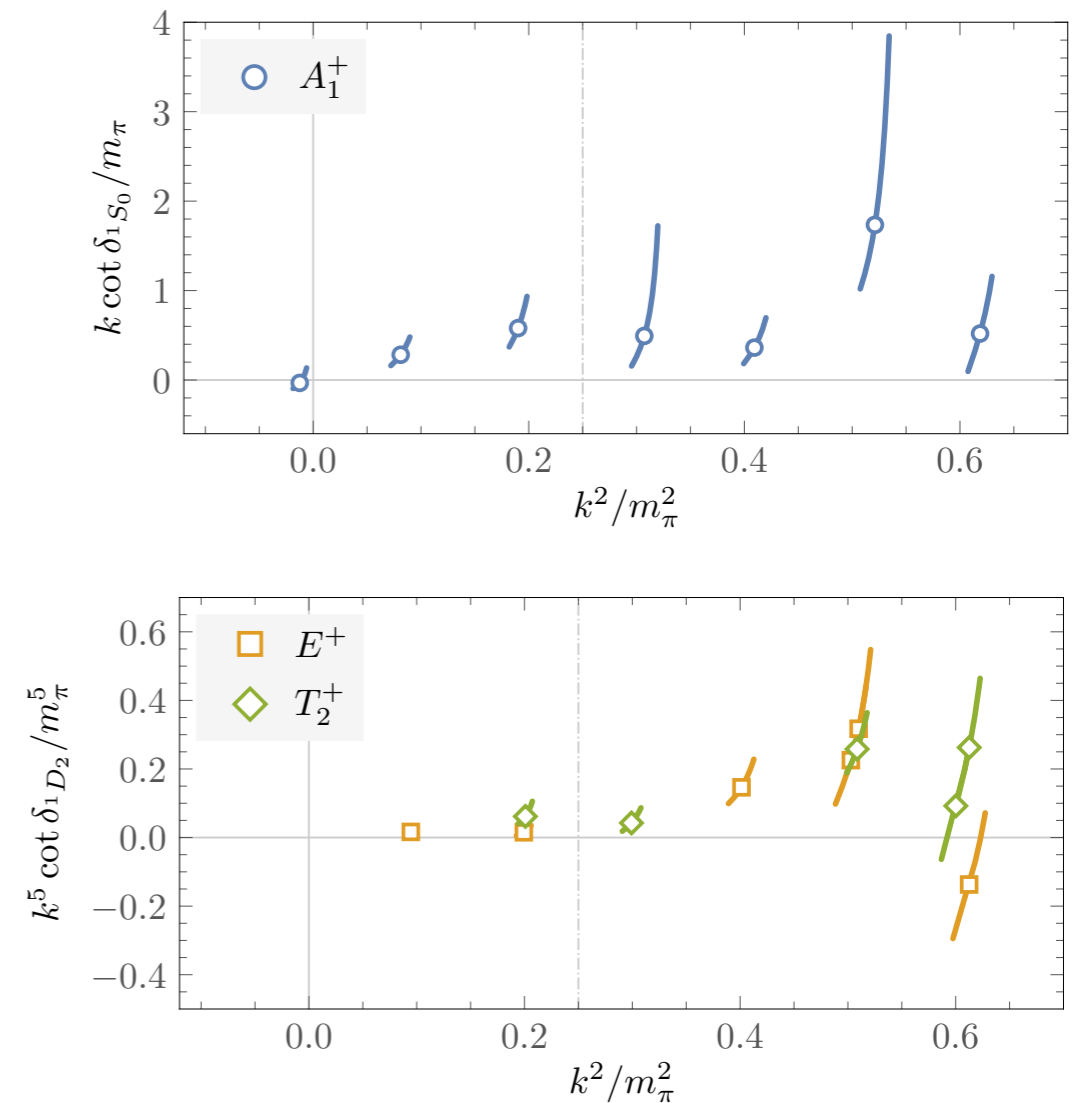
# Baryon-baryon interactions

Extend previous variational studies by including hexaquark and quasi-local operators [Amarasinghe et al. \[NPLQCD\], arXiv:2108.10835 \[hep-lat\]](#)

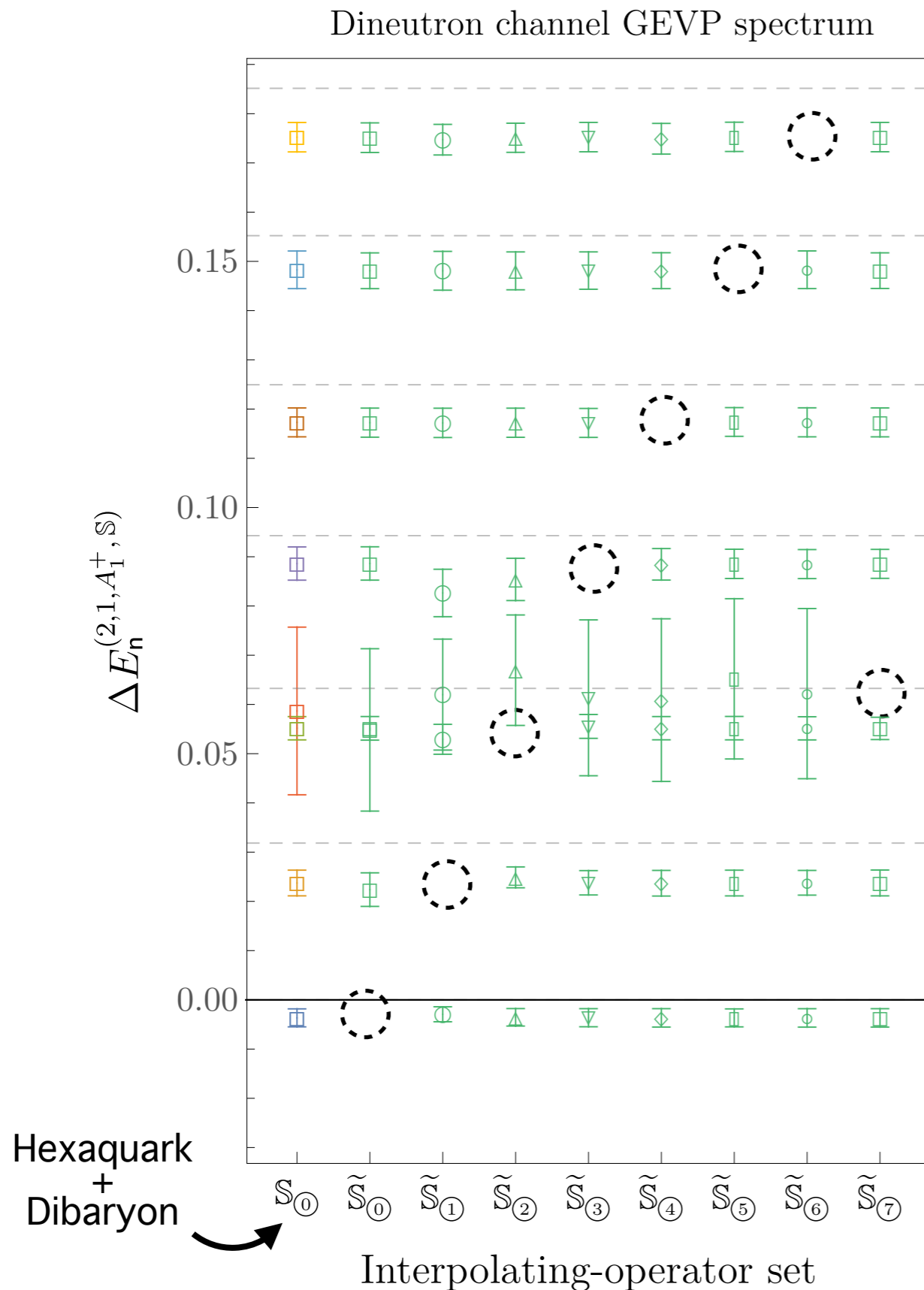


Lüscher's QC  
 $\longrightarrow$   
 Higher partial waves

[Luu, Savage, PRD 83 \(2011\)](#)  
[Briceño, Davoudi, Luu, PRD 88 \(2013\)](#)



# Baryon-baryon interactions



Large interpolating-operator dependence is observed

[Amarasinghe et al. \[NPLQCD\], arXiv:2108.10835 \[hep-lat\]](#)

Energy levels disappear when the operator with the corresponding larger overlap is removed

$\pi\pi$

[Dudek et al. \[HadSpec\], PRD 87 \(2013\)](#)

[Wislon et al. \[HadSpec\], PRD 92 \(2015\)](#)

$N\pi$

[Lang, Verduci, PRD 87 \(2013\)](#)

[Kiratidis et al., PRD 91 \(2015\)](#)

Are we still missing operators?

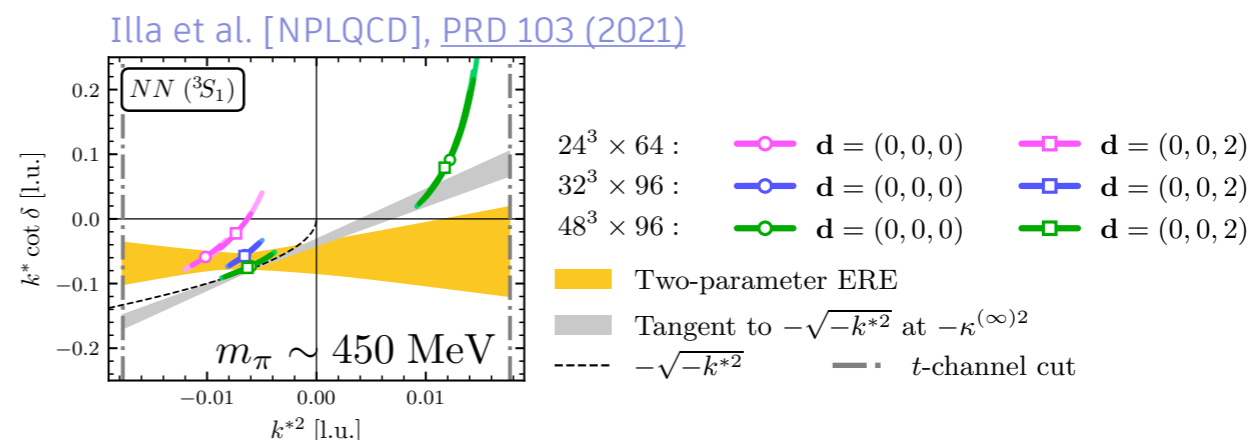
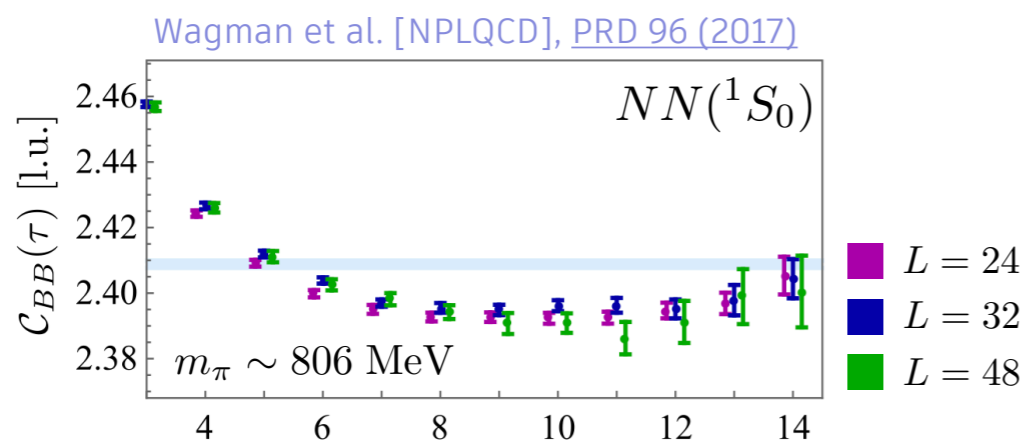


# Baryon-baryon interactions

Are we still missing operators?

Coincidence?

Option a) There is no deep-bound state, however...



Volume independence of the ground state

Analysis of the phase-shifts and checks on scattering parameters

Figure from Davoudi et al., Phys. Rep. 900 (2020)  
Data from Beane et al. [NPLQCD], PRD 87 (2013)  
Barnea et al., PRL 114 (2015)



$$\sigma_{B;\pi A} = \sigma_{\pi A} - A\sigma_{\pi p}$$

Chang et al. [NPLQCD], PRL 120 (2018)  
Beane et al., PRD 89 (2014)

	Direct calculation	Feynman-Hellmann approach
$d$	$-7(14)$	$-9.1(6.0)$
${}^3\text{He}$	$-40(22)$	$-50.8(11.8)$

$m_\pi \sim 806$  MeV

Agreement between LQCD and EFT calculations (fitted with B=2 and 3 systems)

Consistency in scalar ME extraction

# Baryon-baryon interactions

Are we still missing operators?

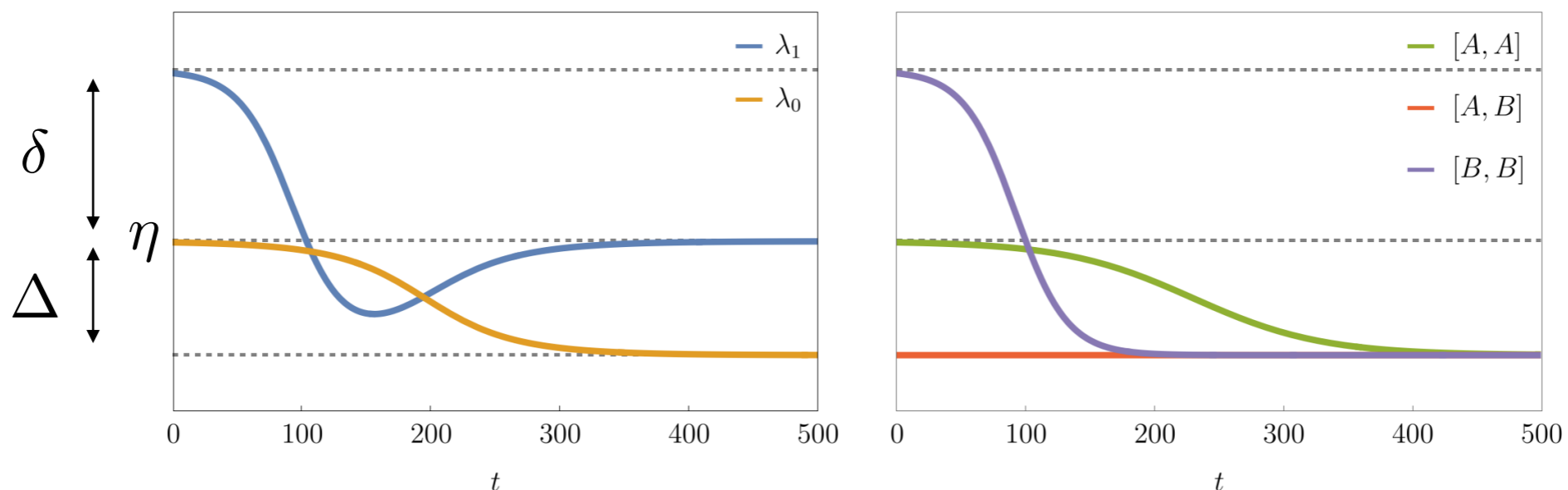
Option b) There is a deep-bound state, but the current operators have a small overlap

Toy model:  $Z_n^{(A)} = (\epsilon, \sqrt{1 - \epsilon^2}, 0)$   $Z_n^{(B)} = (\epsilon, 0, \sqrt{1 - \epsilon^2})$

$$E_0^{(AB)} = \eta - \Delta \quad E_1^{(AB)} = \eta \quad E_2^{(AB)} = \eta + \delta$$

$$\lambda_0^{(AB)} = e^{-(t-t_0)\eta} [1 + \epsilon^2 (e^{t\Delta} - e^{t_0\Delta}) + \mathcal{O}(\epsilon^4)]$$

$$\lambda_1^{(AB)} = e^{-(t-t_0)(\eta+\delta)} [1 + \epsilon^2 (e^{t(\Delta+\delta)} - e^{t_0(\Delta+\delta)}) + \mathcal{O}(\epsilon^4)]$$



# Summary

We can use LQCD to reach systems that are difficult for experimentalists (like strange systems)

It is still not clear what the best operators are to include in a variational analysis for two-baryon systems

Ongoing study with 15 additional hexaquark operators and a different volume at  $m_\pi \sim 806$  MeV

→ Compute contractions for different baryon-baryon systems closer to the physical point ( $m_\pi \sim 170$  MeV) at two different volumes (4.4 and 5.8 fm) (optimized tiramisu contraction code on GPUs)

## Thank you

