

# Studying QCD and Beyond with Electron Scattering

## QCD Lagrangian

$$\mathcal{L} = \frac{1}{4g^2} G_{\mu\nu}^a G_{\mu\nu}^a + \sum_j \bar{q}_j (i\gamma_\mu D_\mu + m_j) q_j$$

where

$$G_{\mu\nu}^a \equiv \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + i f_{bc}^a A_\mu^b A_\nu^c$$

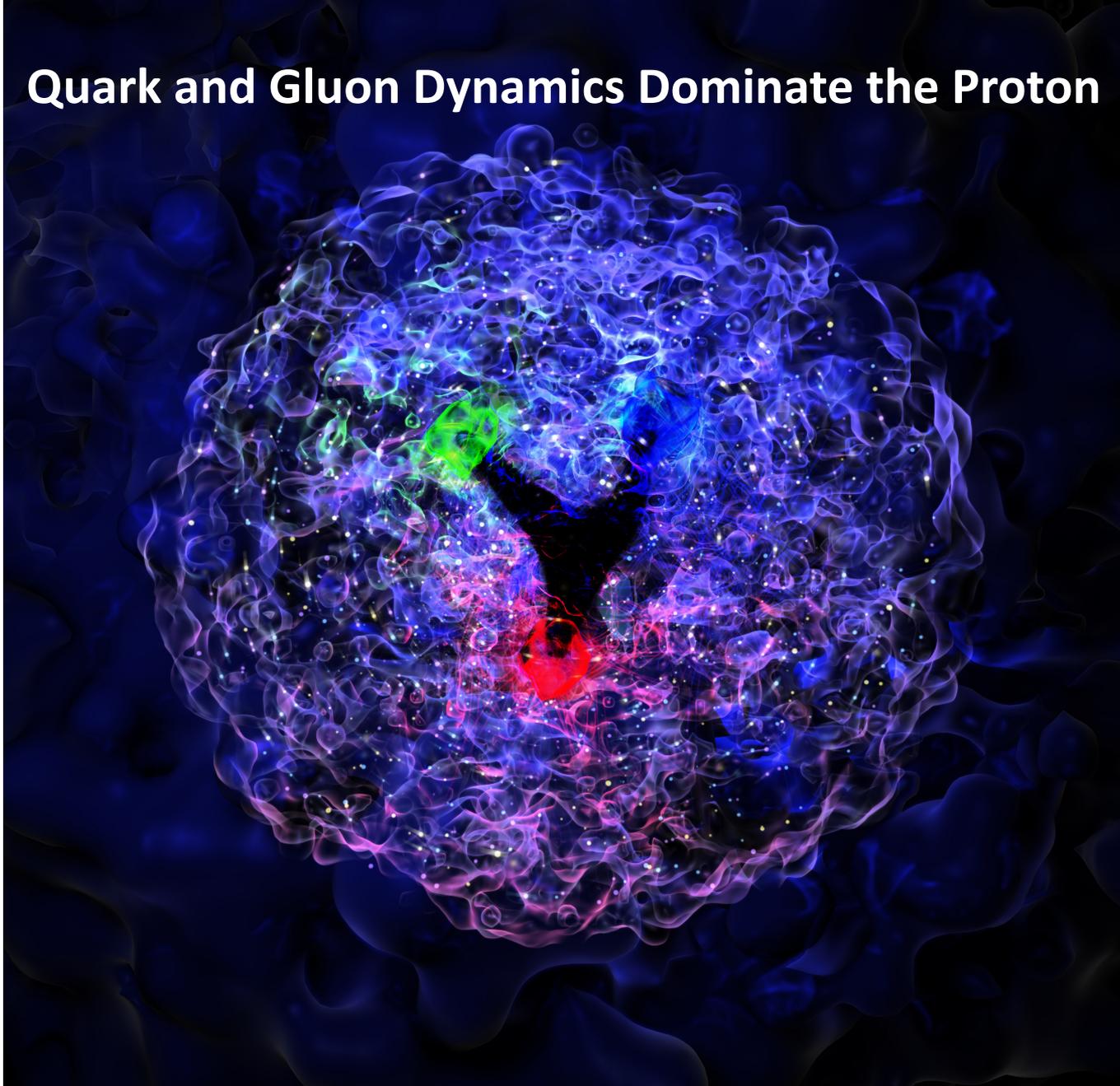
and

$$D_\mu \equiv \partial_\mu + i t^a A_\mu^a$$

That's all!

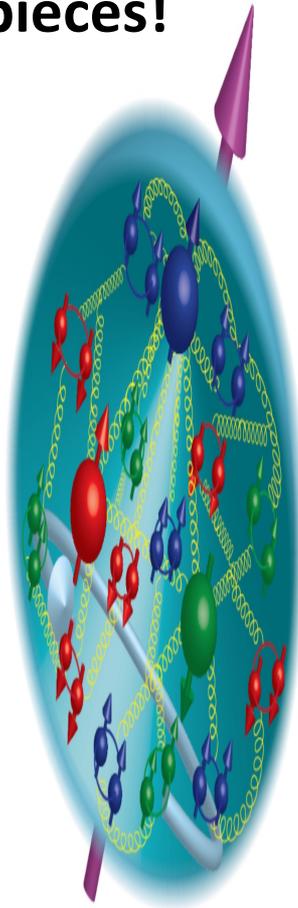
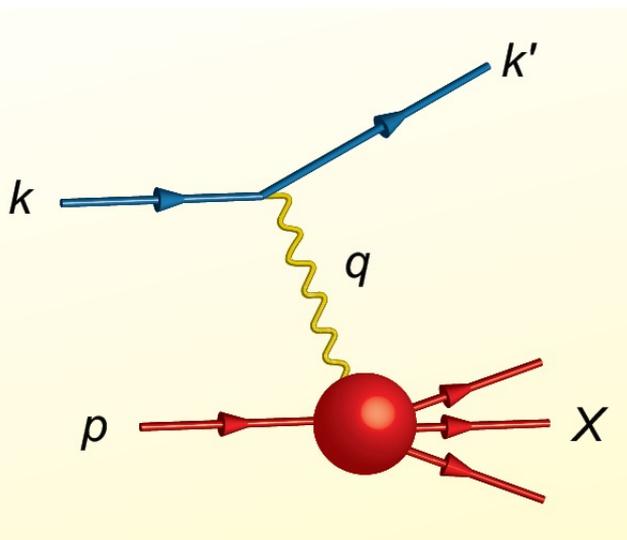
**How does the spin-1/2 proton with mass 938 MeV/c<sup>2</sup> arise?**

# Quark and Gluon Dynamics Dominate the Proton



# Proton Viewed in High Energy Electron Scattering: 1 Longitudinal Dimension

Proton is smashed into pieces!



- Viewed from boosted frame, length contracted by

$$\gamma_{Breit} = \sqrt{1 + \frac{Q^2}{4M^2}}$$

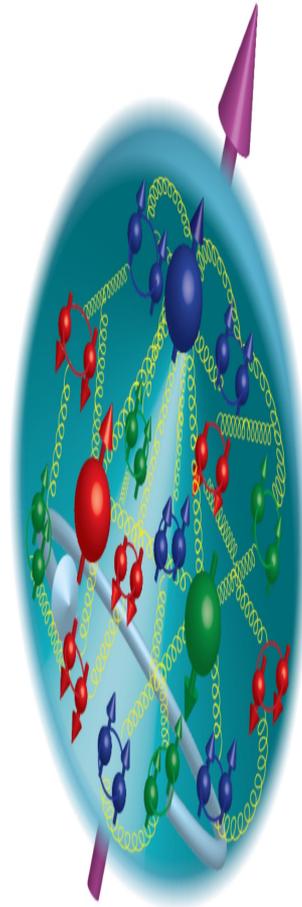
- Internal motion of the proton's constituents is slowed down by time dilation – the instantaneous charge distribution of the proton is seen.
- In boosted frame  $x$  is understood as the longitudinal momentum fraction  
*valence* quarks:  $0.1 < x < 1$   
*sea* quarks:  $x < 0.1$

## Lorentz Invariants

- $E_{CM}^2 = (p+k)^2$
- $Q^2 = -(k-k')^2$
- $x = Q^2/(2p \cdot q)$

J. Bjorken, SLAC-PUB-0571  
March 1969

# Proton Viewed in High Energy Electron Scattering: 1 Longitudinal Dimension

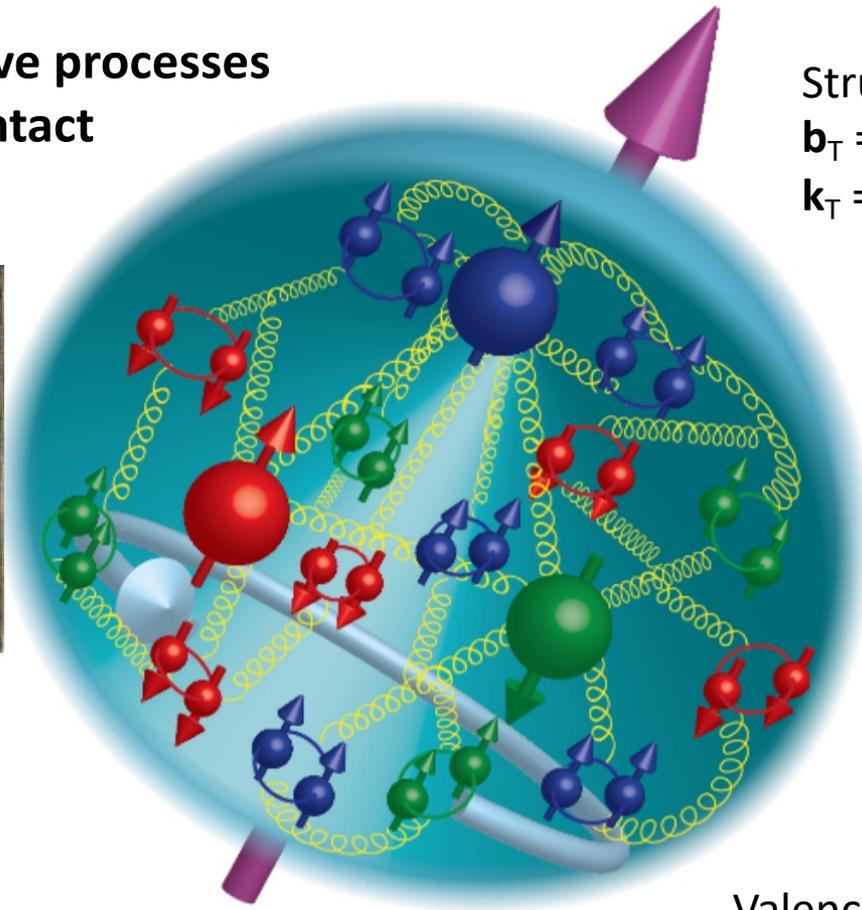


# Proton Tomography: 2 New Dimensions Transverse to Longitudinal Momentum

Deeply virtual exclusive processes  
where proton is left intact



Direction of longitudinal  
momentum normal to  
plane of slide



Structure mapped in terms of  
 $\mathbf{b}_T$  = transverse position  
 $\mathbf{k}_T$  = transverse momentum

**Nuclei!**

**Goal:  
Unprecedented  
21<sup>st</sup> Century Imaging  
of Hadronic Matter**

Valence Quarks: JLab 12 GeV  
Sea Quarks and Gluons: EIC

# Charting the Inner Structure of the Proton

<https://www.youtube.com/watch?v=G-9I0buDi4s>



**Christopher Boebel**  
**Rolf Ent**  
**James LaPlante**  
**Joseph McMaster**  
**Richard Milner**

**Jefferson Lab**

Richard Milner

**SPUTNIK  
ANIMATION**

LNS Welcome

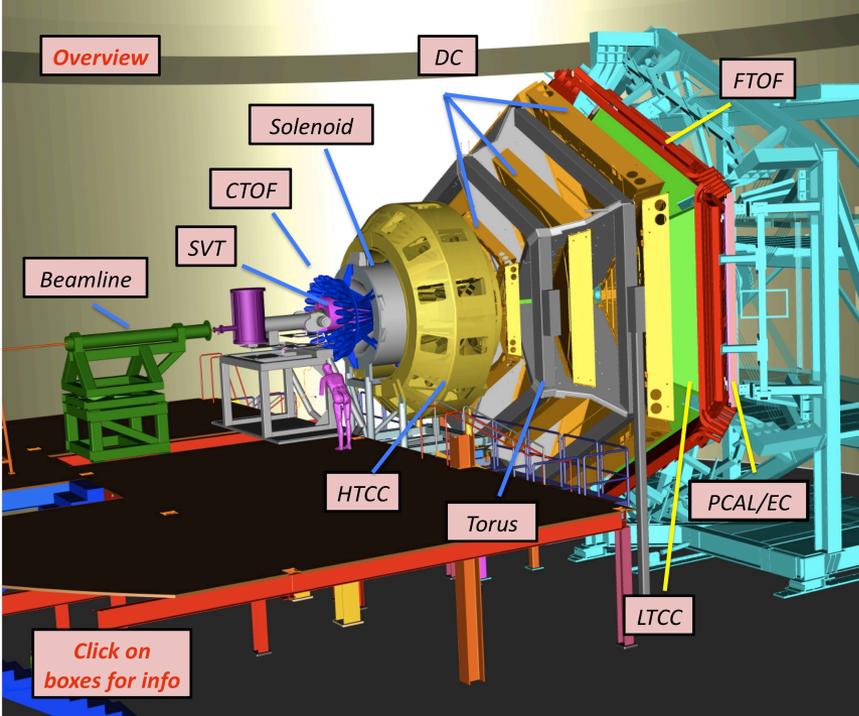
September 6, 2022

**ARTS**  
CENTER FOR ART,  
SCIENCE & TECHNOLOGY  
AT MIT

# Jefferson Lab

Thomas Jefferson National Accelerator Facility



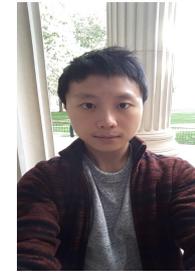


# CLAS12

## Deeply Virtual Processes



Bobby  
Johnston



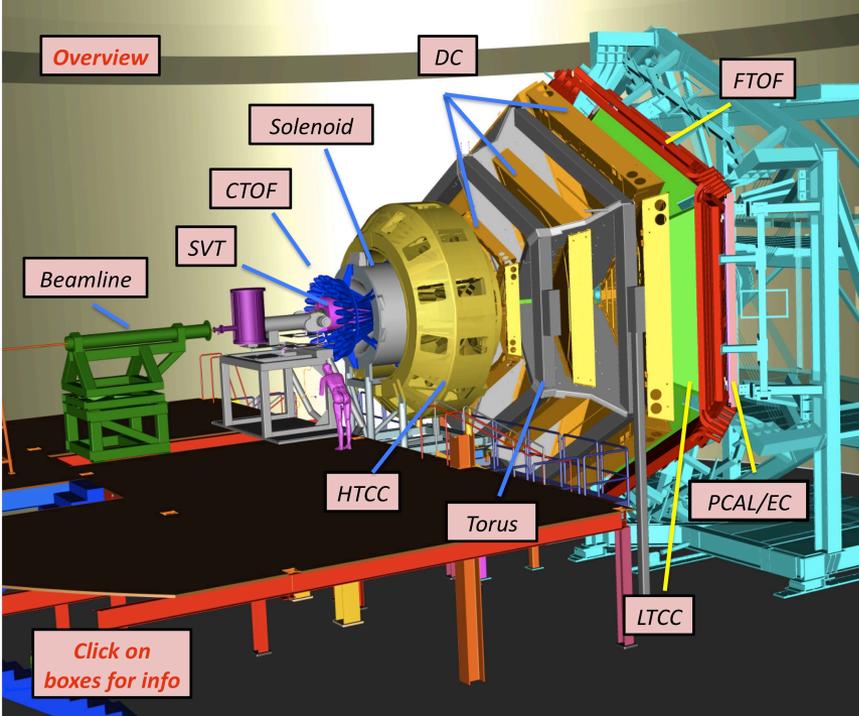
Sangbaek  
Lee



Patrick  
Moran

- Our group is a member of the CLAS12 collaboration at Jefferson Lab, VA
- Have developed with MIT-LNS high performance computing group (computers located at Bates) the capability to run the CLAS12 Monte-Carlo code by collaborators worldwide
- Working on analysis of CLAS12 data.
 

Bobby:	$\rho(e, e' \pi^0) p$
Sangbaek:	$\rho(e, e' \gamma) p$
Patrick:	$\rho(e, e' \varphi) p$
- Seek new insights into the quark and gluon structure of the proton



# CLAS12

## Deeply Virtual Processes



Bobby  
Johnston



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Lee



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Moran

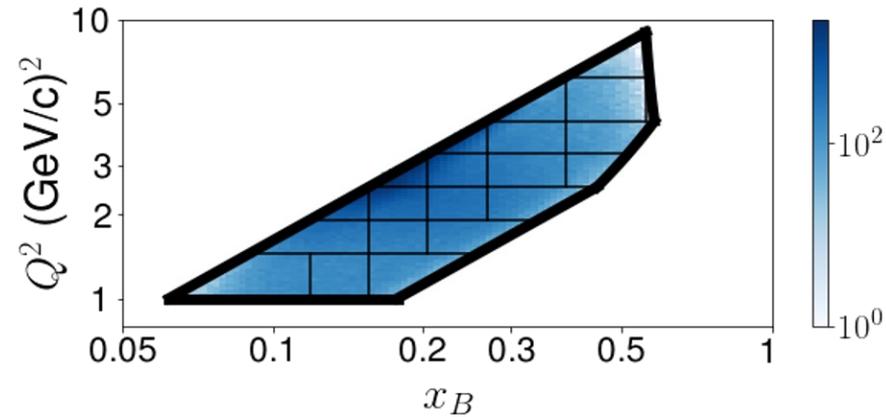
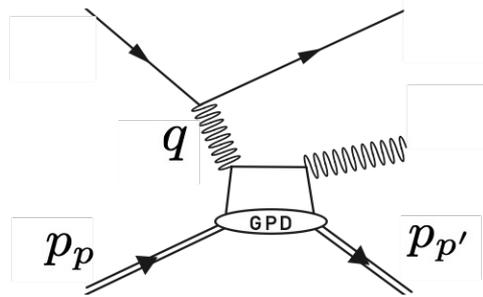
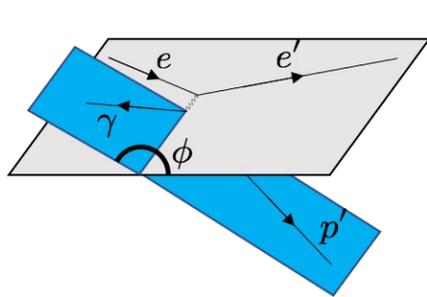
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# DVCS cross section measurement at CLAS12



Sangbaek Lee



Bjorken x

$$0 < x_B \equiv \frac{Q^2}{2p_p \cdot q} < 1$$

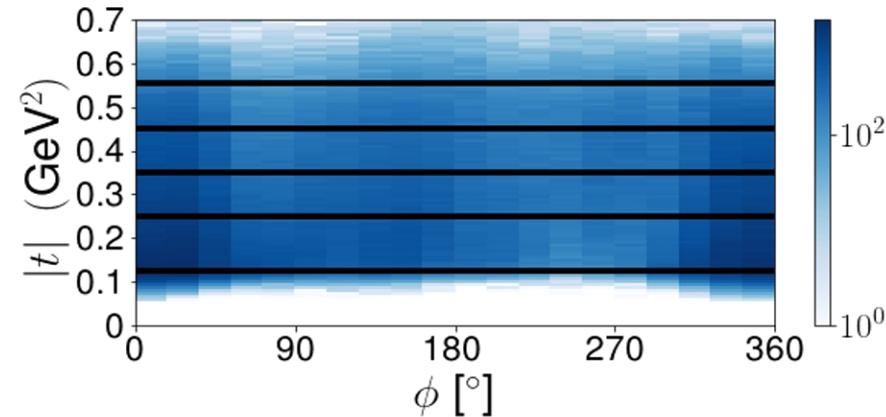
4-momentum transfer

$$Q^2 \equiv -q^2 > 1$$

Mandelstam variable

$$t \equiv (p_{p'} - p_p)^2$$

angle between scattering planes  $\phi$



$$\frac{d\sigma}{dx_B dQ^2 d(-t) d\phi} = \frac{N_{\text{DVCS+BH}}}{L \times \text{Vol}_{\text{bin}}} \frac{1}{F_{\text{correction}}}$$

# DVCS Cross Section Results

Measurement of the Deeply Virtual Compton Scattering Cross Section from the Proton at 10.6 GeV using the CLAS12 Detector

by

Sangbaek Lee

B.S., Seoul National University (2016)

Submitted to the Department of Physics in partial fulfillment of the requirements for the degree of

Doctor of Philosophy in Physics

at the

MASSACHUSETTS INSTITUTE OF TECHNOLOGY

September 2022

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 Department of Physics  
 August 22, 2022

Certified by .....  
 Richard G. Milner  
 Professor of Physics  
 Thesis Supervisor

Accepted by .....  
 Deeptho Chakrabarty  
 Associate Department Head of Physics

0.150 GeV<sup>2</sup> < |t| < 0.250 GeV<sup>2</sup>  
 + Experimental Data  
 — Theory (BH)  
 — Theory (KM15)

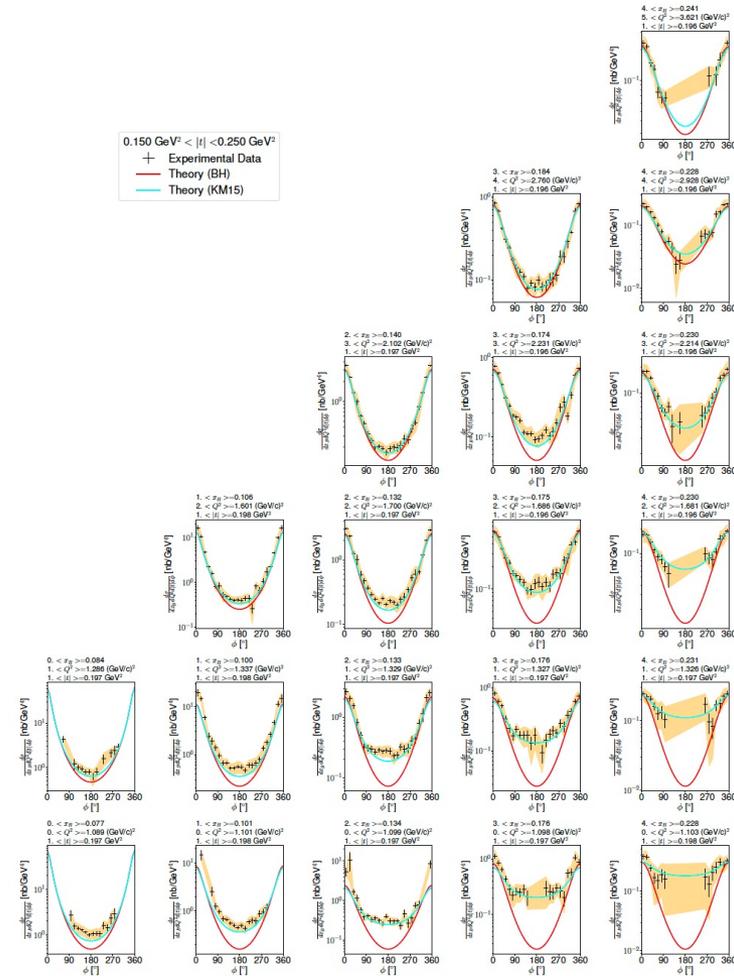
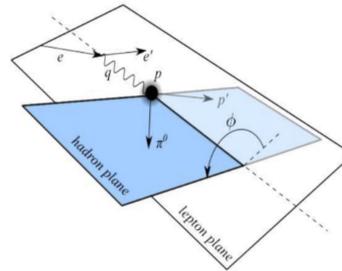
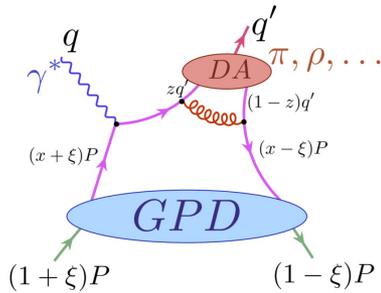


Figure 5-25: The unpolarized cross section in  $x_B < 0.268$ ,  $Q^2 < 4.326$  (GeV/c)<sup>2</sup>,  $0.150$  GeV<sup>2</sup> < |t| < 0.250 GeV<sup>2</sup> bins.

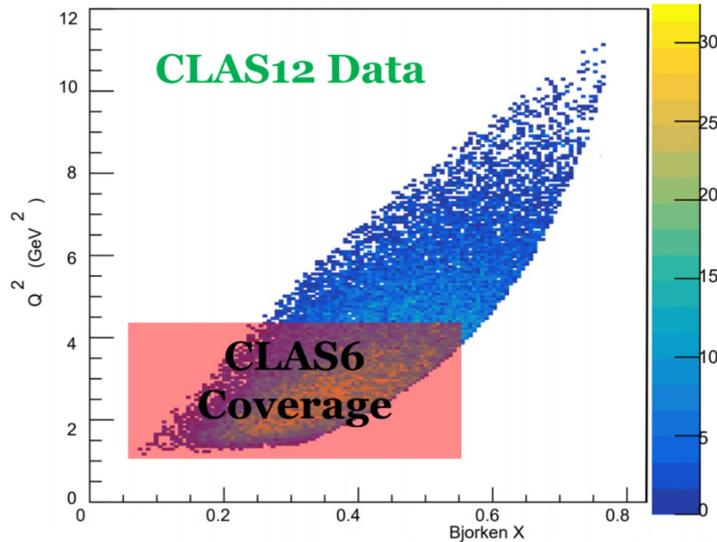
# Deeply Virtual $\pi^0$ cross section measurement at CLAS12



**Bobby Johnston**



$Q^2$  vs.  $x_B$  - CLAS12



$$\frac{d^4\sigma}{dQ^2 dx_B dt d\phi_\pi}$$

$$= \Gamma(Q^2, x_B, E) \frac{1}{2\pi} \left[ \left( \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_\pi \frac{d\sigma_{LT}}{dt} \right]$$

$$\frac{d\sigma_L}{dt} = \frac{4\pi\alpha}{k'} \frac{1}{Q^6} \left\{ (1-\xi^2) |\langle \tilde{H} \rangle|^2 - 2\xi^2 \text{Re}[\langle \tilde{H} \rangle^* \langle \tilde{E} \rangle] - \frac{t'}{4m^2} \xi^2 |\langle \tilde{E} \rangle|^2 \right\},$$

$$\frac{d\sigma_T}{dt} = \frac{4\pi\alpha}{2k'} \frac{\mu_\pi^2}{Q^8} \left[ (1-\xi^2) |\langle H_T \rangle|^2 - \frac{t'}{8m^2} |\langle \tilde{E}_T \rangle|^2 \right],$$

$$\frac{d\sigma_{LT}}{dt} = \frac{4\pi\alpha}{\sqrt{2}k'} \frac{\mu_\pi}{Q^7} \xi \sqrt{1-\xi^2} \frac{\sqrt{-t'}}{2m} \text{Re}[\langle H_T \rangle^* \langle \tilde{E} \rangle],$$

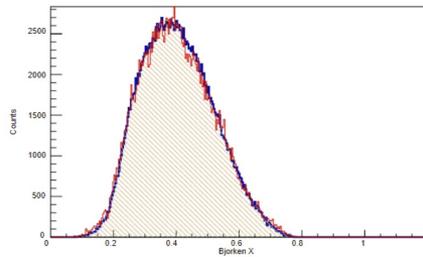
$$\frac{d\sigma_{TT}}{dt} = \frac{4\pi\alpha}{k'} \frac{\mu_\pi^2}{Q^8} \frac{t'}{16m^2} |\langle \tilde{E}_T \rangle|^2.$$

# Deeply virtual $\pi^0$ cross section measurement at CLAS12

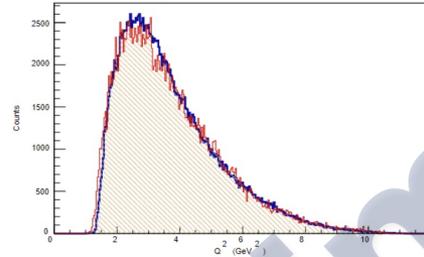
## Simulation-Data Comparison

Simulation (red) vs. Data (blue)

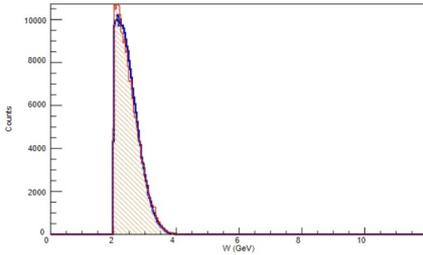
Bjorken X



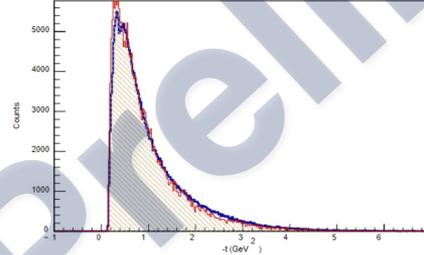
$Q^2$



W

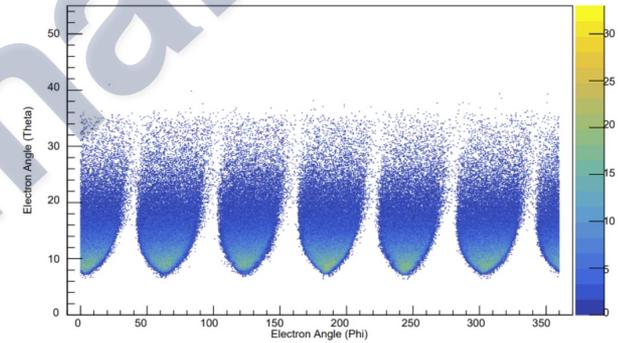


Mom. Transfer t

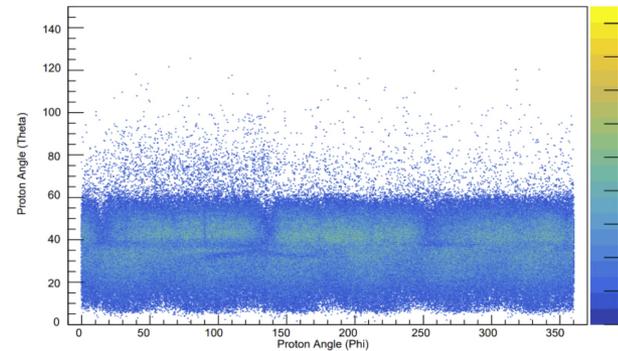


## Particle Kinematics

Electron Theta vs. Phi, After Excl. Cuts, FD & CD



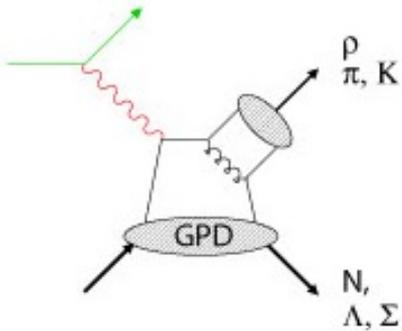
Proton Theta vs. Phi, After Excl. Cuts, FD & CD



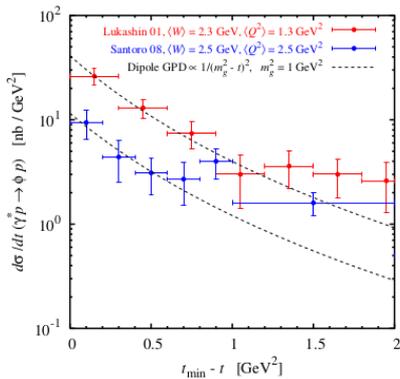
# Deeply Virtual Phi Production (DVφP) at CLAS12, JLab Hall B



Patrick Moran

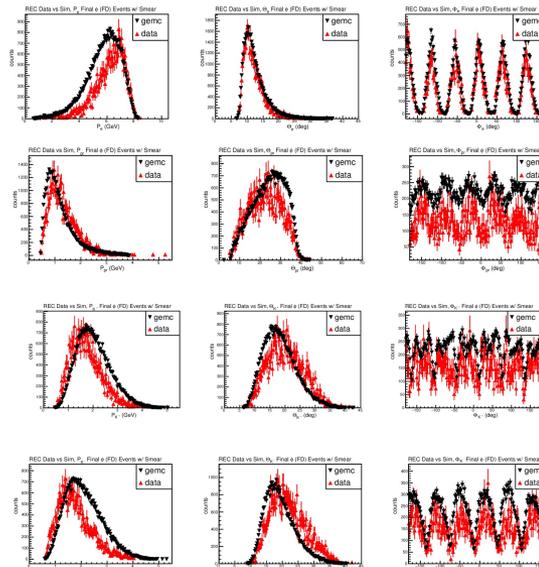


- Goal: to measure the exclusive phi electroproduction cross section
- Signal event:  $(e, e'p'K^+K^-)$
- DVφP accesses gluon GPDs, information about gluonic radius of the proton

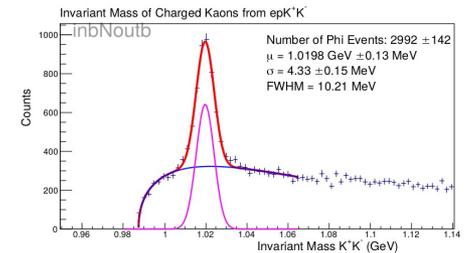


Previous diff. cross section measurements from CLAS

## Simulation vs. data for final state particle kinematics



## Total number of phi events in the final state

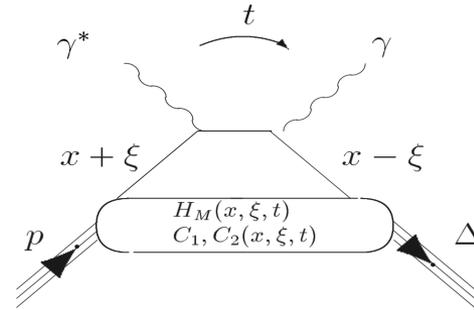
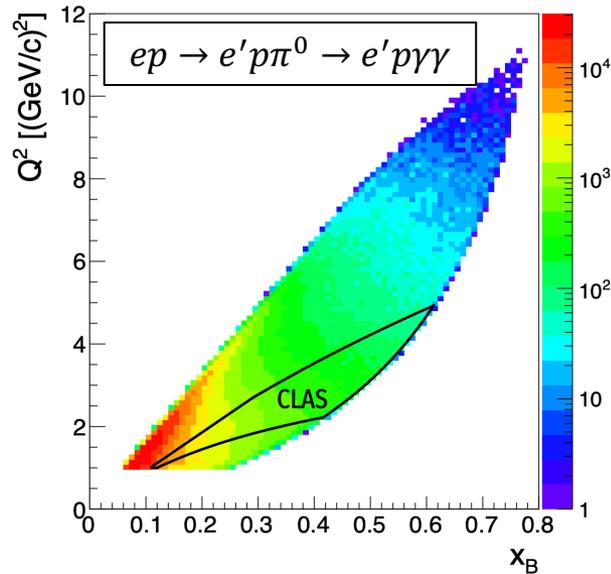


# Transition GPDs $ep \rightarrow \gamma N^* \rightarrow \gamma p \text{ Meson}$

## Reaction Mechanism: Factorization



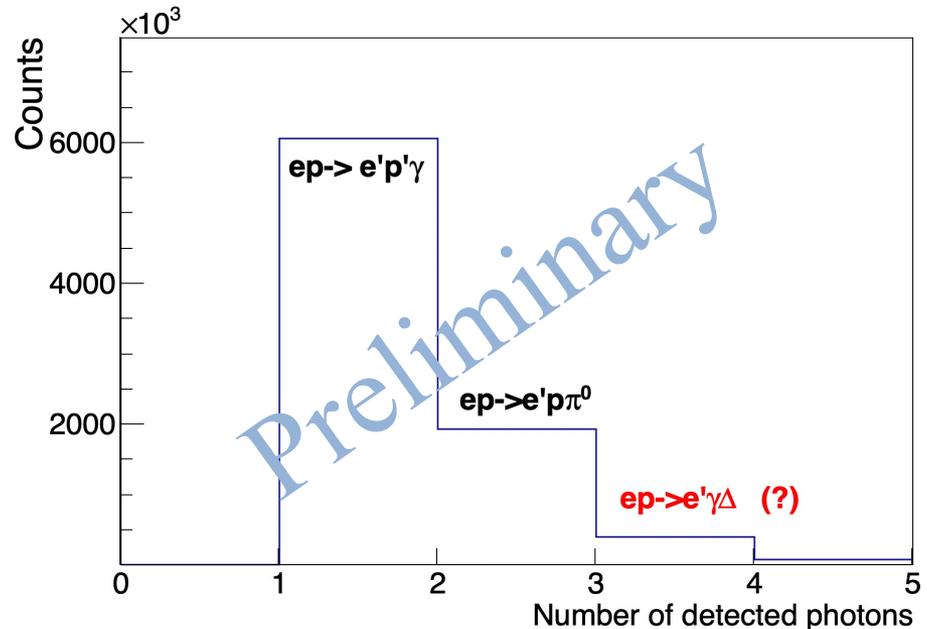
Dr. Igor Korover



$$\frac{d^2\sigma}{dt d\phi_\pi} = \frac{1}{2\pi} \left[ \left( \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_\pi \frac{d\sigma_{LT}}{dt} \right]$$

Two beam energies: 5.75 GeV and 10.6 GeV

$\sigma_L/\sigma_T$  separation over wide ( $x_B, Q^2$ ) range



April, 2021

S2134

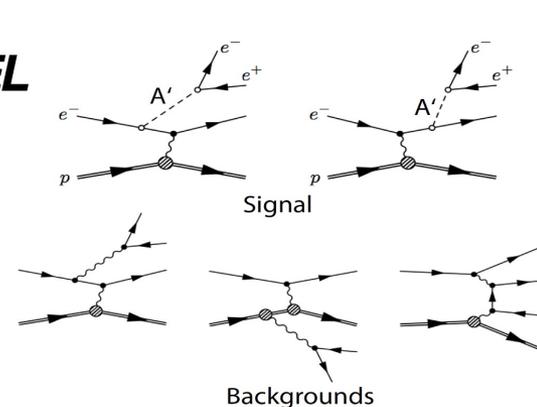
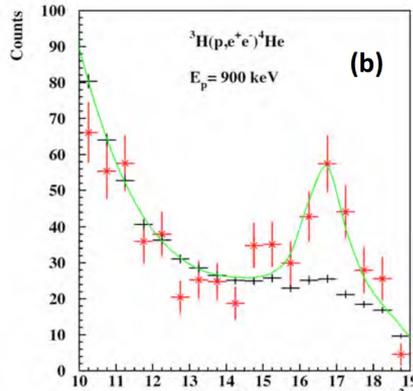
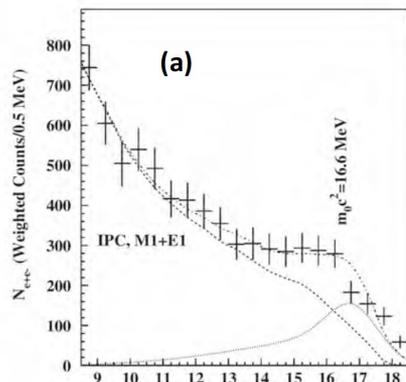
Search for New Physics  
in  $e^+e^-$  Final States  
With an Invariant Mass  
of 13-17 MeV using the  
ARIEL Electron  
Accelerator

J. C. Bernauer,  
R.C. Corliss,  
R.G. Milner

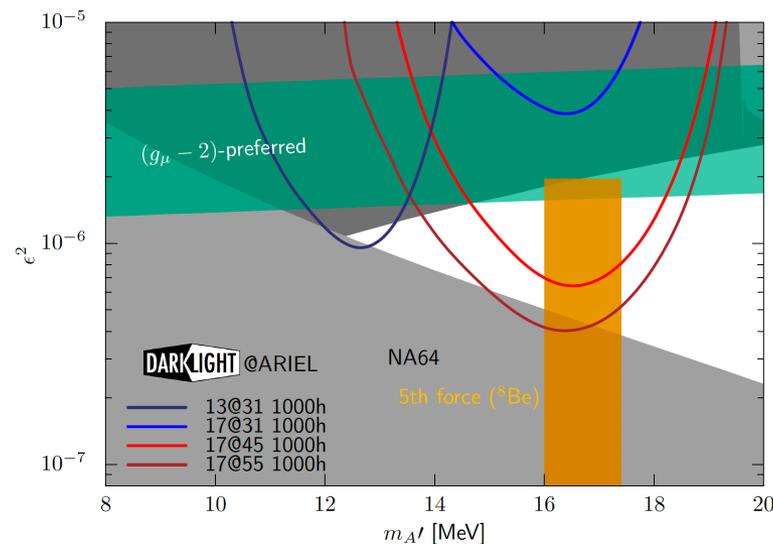
Approved for 1300  
hours with high  
priority

**DARKLIGHT**

@ **ARIEL**



Arizona State University, Tempe, AZ, USA  
 University of British Columbia, Canada  
 Hampton University, Hampton, VA, USA  
 TJNAF, Newport News, VA, USA  
 Massachusetts Institute of Technology, Cambridge, MA, USA  
 St. Mary's University, Halifax, Nova Scotia, Canada  
 Stony Brook University, NY, USA  
 TRIUMF, Vancouver, British Columbia, Canada  
 University of Manitoba, Canada  
 University of Winnipeg, Manitoba, Canada



# Realization

Funding secured in FY2022 and construction will take place in FY2023

Data taking in 2024

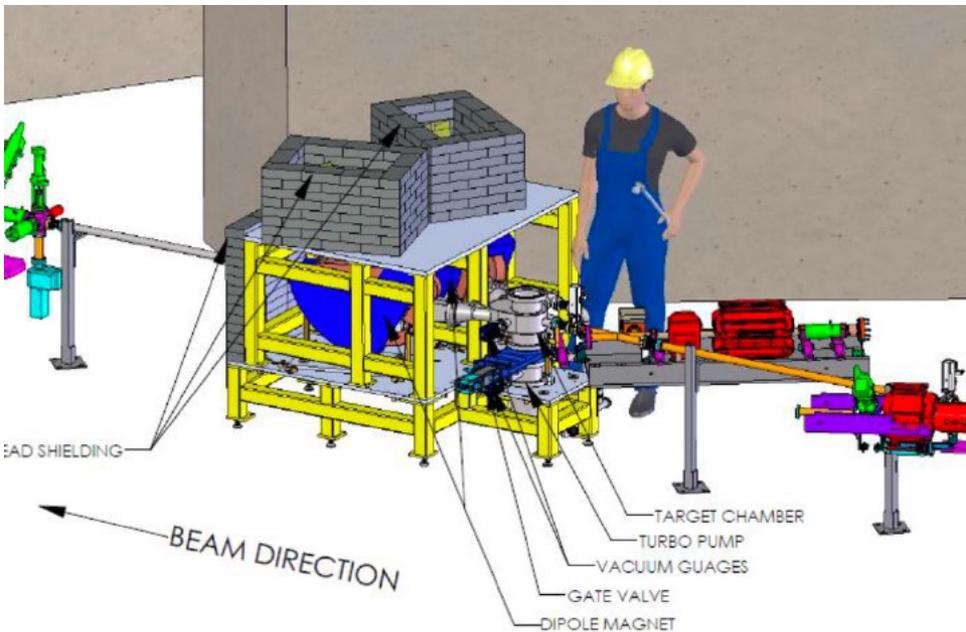
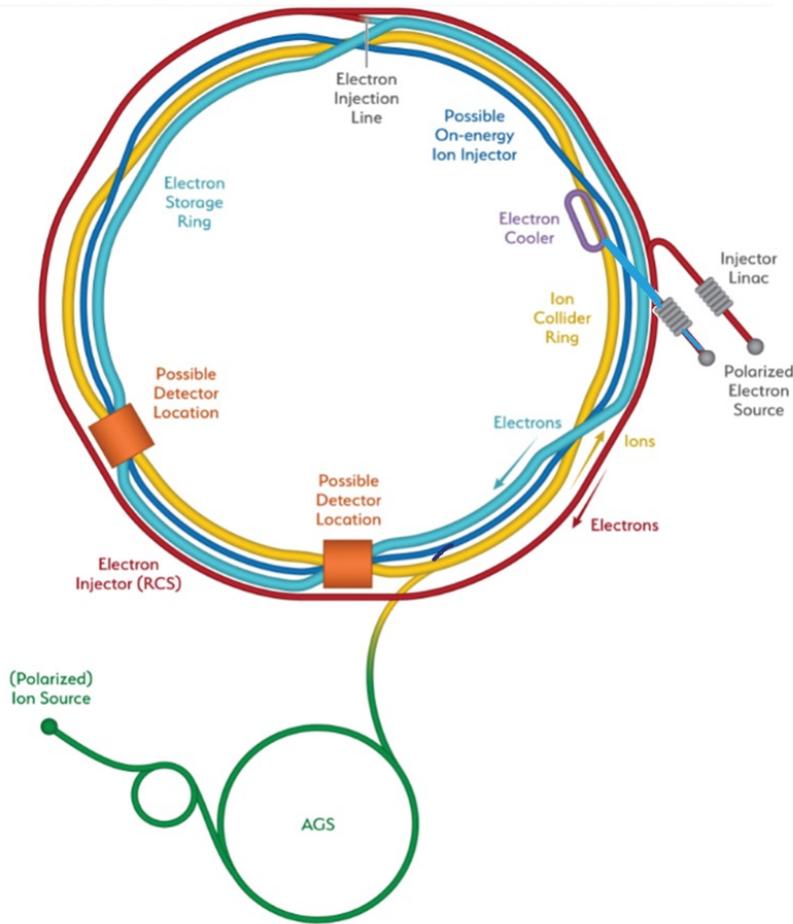


Table 2: Major tasks and responsibilities for the proposed experiment.

Task	Lead Group	\$ 165 k
Magnetic spectrometers	MIT	\$ 50 K
Target and Scattering Chamber	MIT	
GEM detectors	Hampton U	
Data Acquisition	Stony Brook U.	
Trigger hodoscopes	TRIUMF, UW, and SMU	
Integration with ARIEL	TRIUMF, UofM	

MIT-Bates lab is coordinating design and construction of the experiment.

# Electron-Ion Collider (EIC)



- New high luminosity collider **to study QCD** to be constructed using RHIC at BNL and expected to come online in early 2030s.
- MIT-LNS has played a leadership role in making the case for EIC over two decades: Bates Lab one of the points of origin
- Prof. Hen leader of EPIC (detector 1)
- EIC R&D: Polarized  $^3\text{He}$  ion source, EM calorimeter and streaming readout development
- Beginning graduate students in 2022 will be young faculty who will drive the scientific program at EIC.

# Seeking New Students

To work on

- the design and construction of the DarkLight experiment at TRIUMF, Vancouver, Canada
- the data taking and analysis of deeply virtual exclusive processes using CLAS12 at Jefferson Lab
- the design and construction of the EPIC detector for EIC

**Contact info: Email: [milner@mit.edu](mailto:milner@mit.edu) Office 26-411**