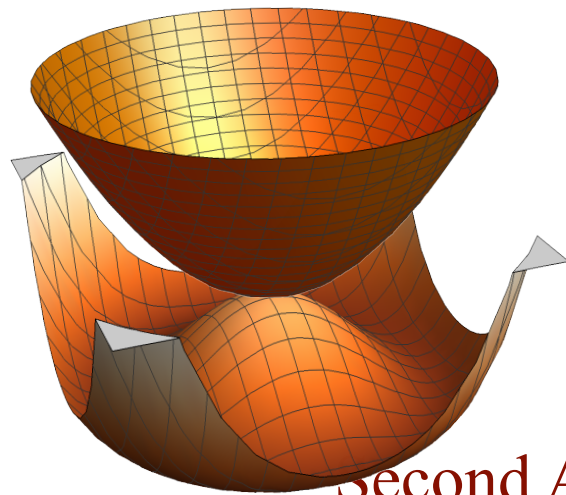
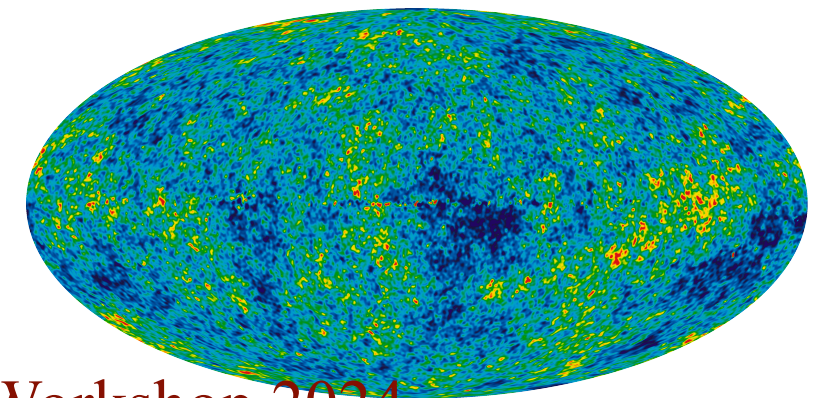


Electroweak Phase Transition and Higgs Exotic Decays



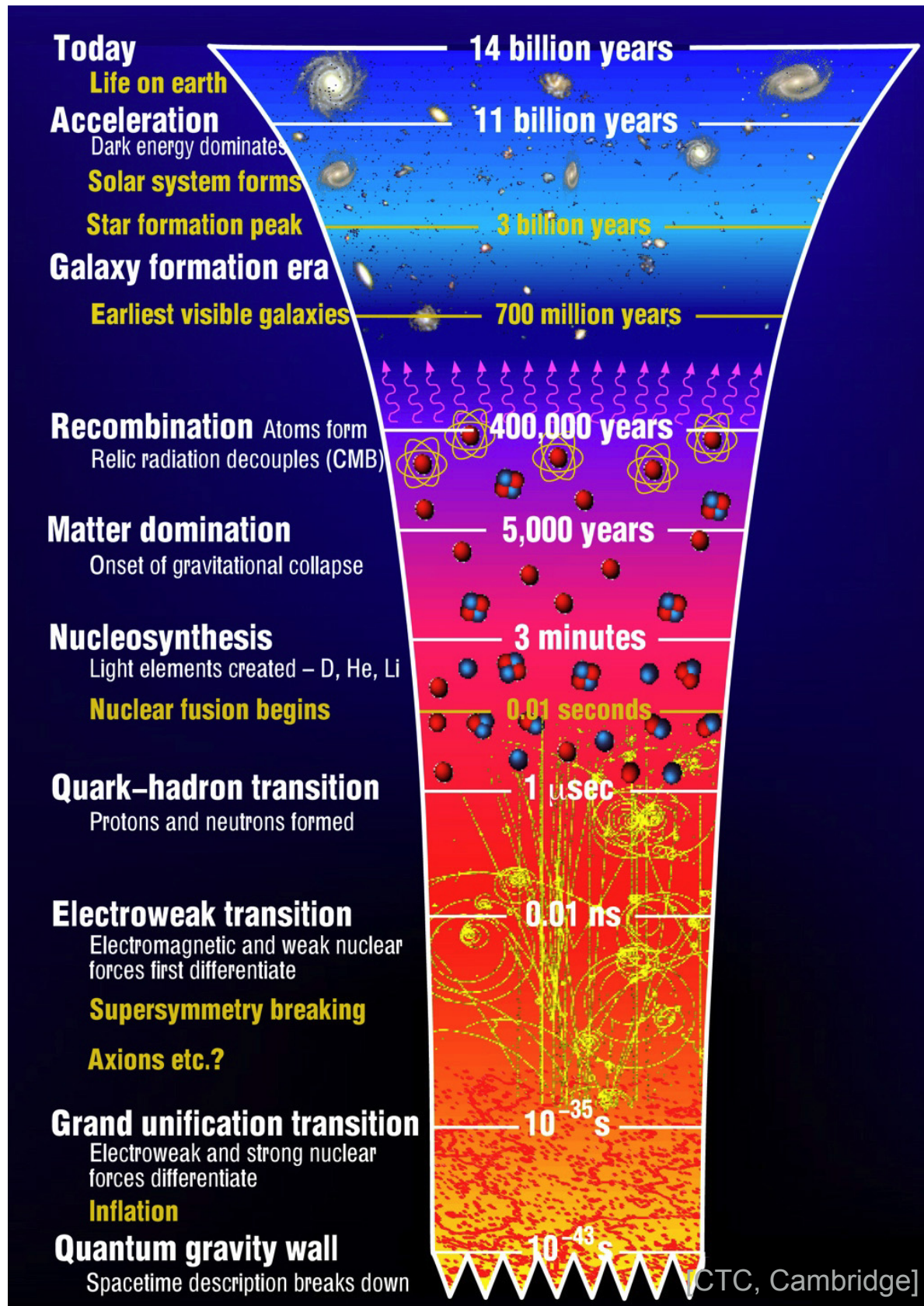
Yikun Wang
California Institute of Technology

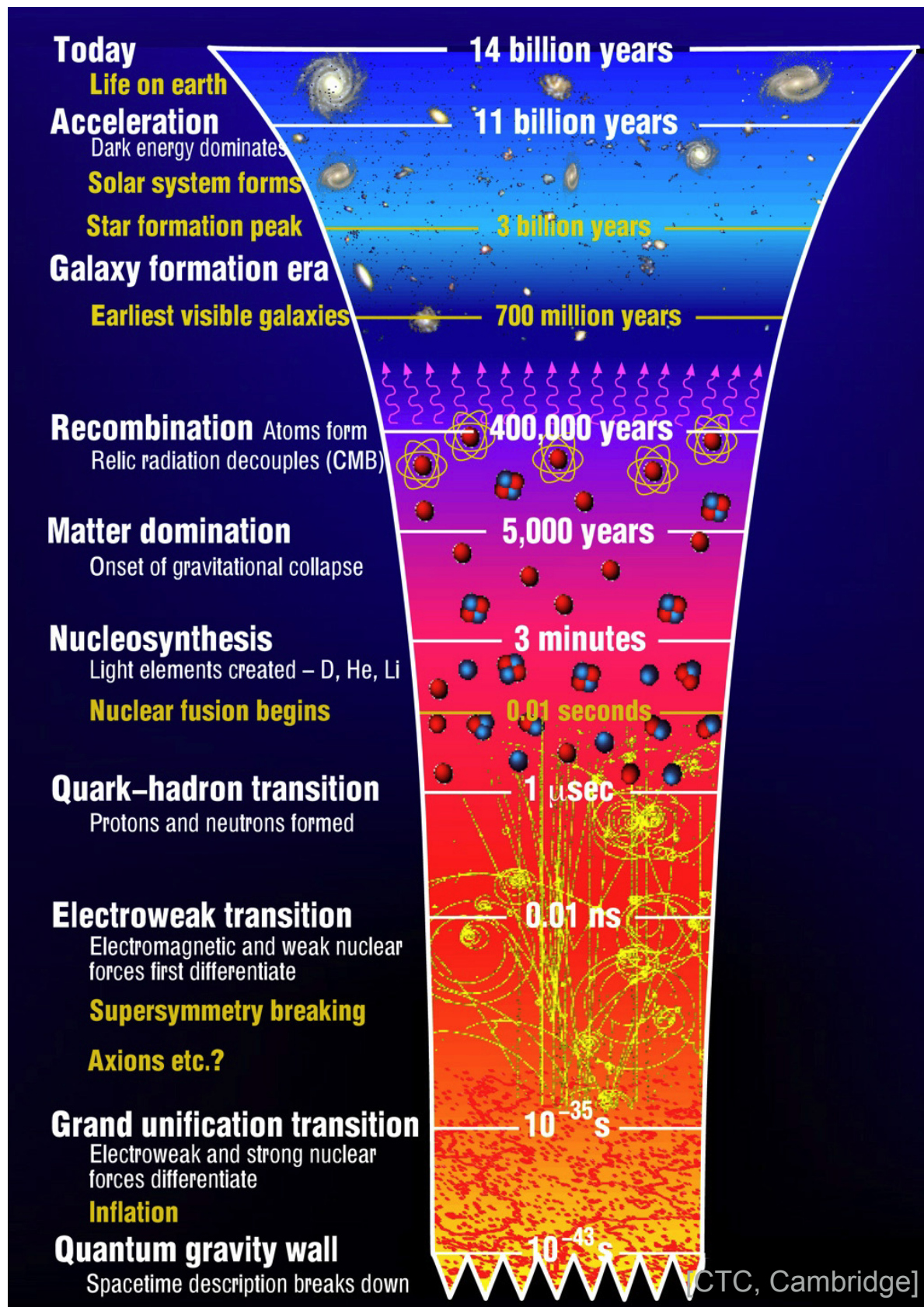


Second Annual U.S. Future Circular Collider (FCC) Workshop 2024

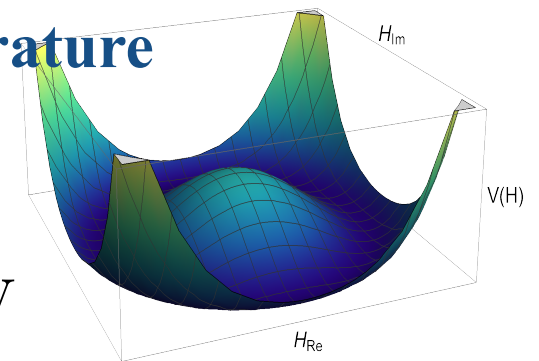
March 26th, 2024, MIT, Boston

*with Marcela Carena, Zhen Liu based on arXiv:1911.10206;
with Marcela Carena, Jonathan Kozaczuk, Zhen Liu, Tong Ou, Michael J. Ramsey-
Musolf, Jessie Shelton, and Ke-Pan Xie based on arXiv:2203.08206.*





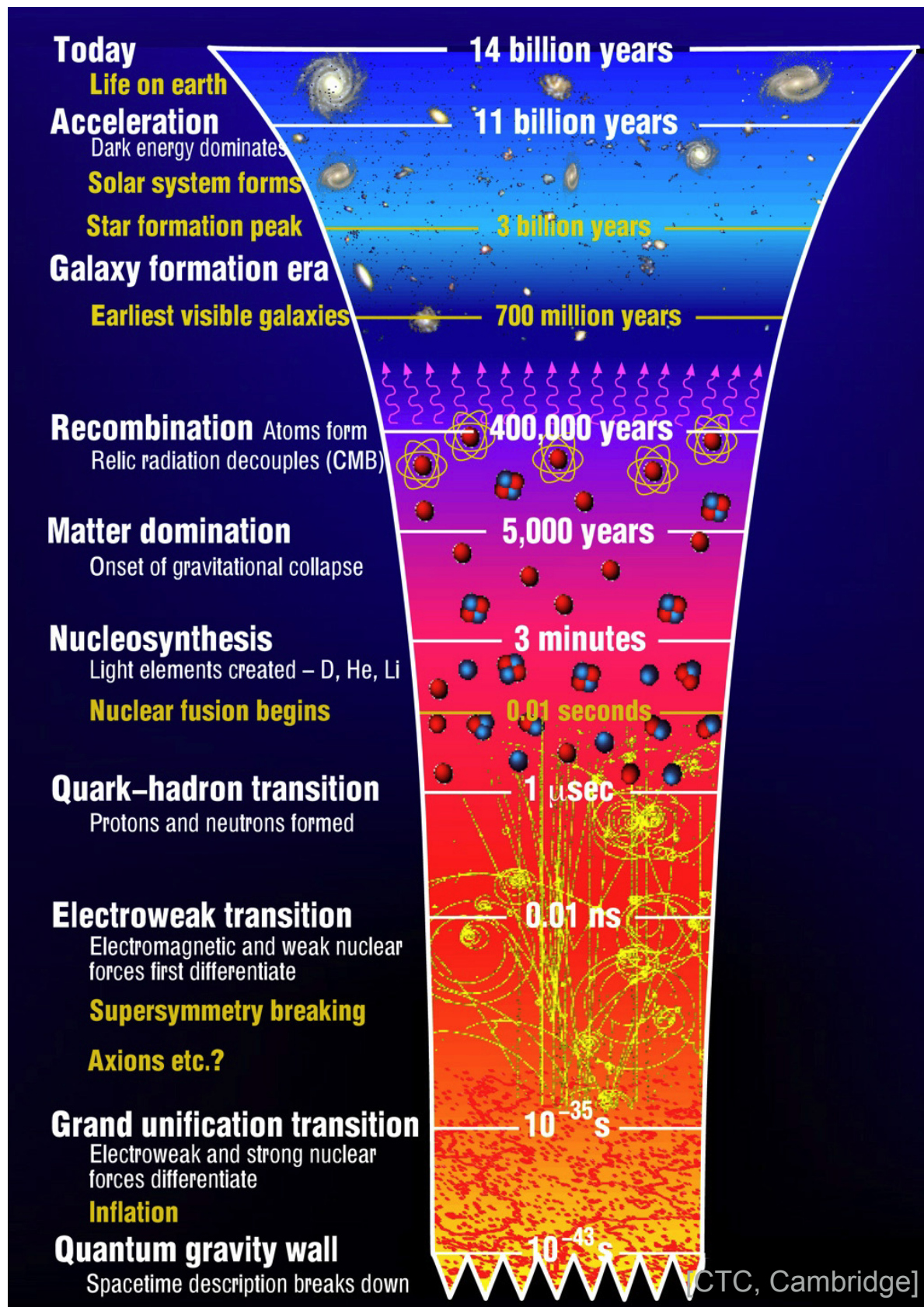
Zero Temperature



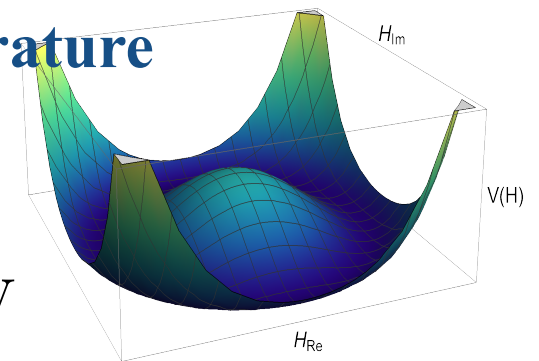
$$\langle h \rangle = 246 \text{ GeV}$$

$$V(H) = -\mu_H^2 |H|^2 + \lambda_H |H|^4$$

Electroweak Symmetry Breaking



Zero Temperature



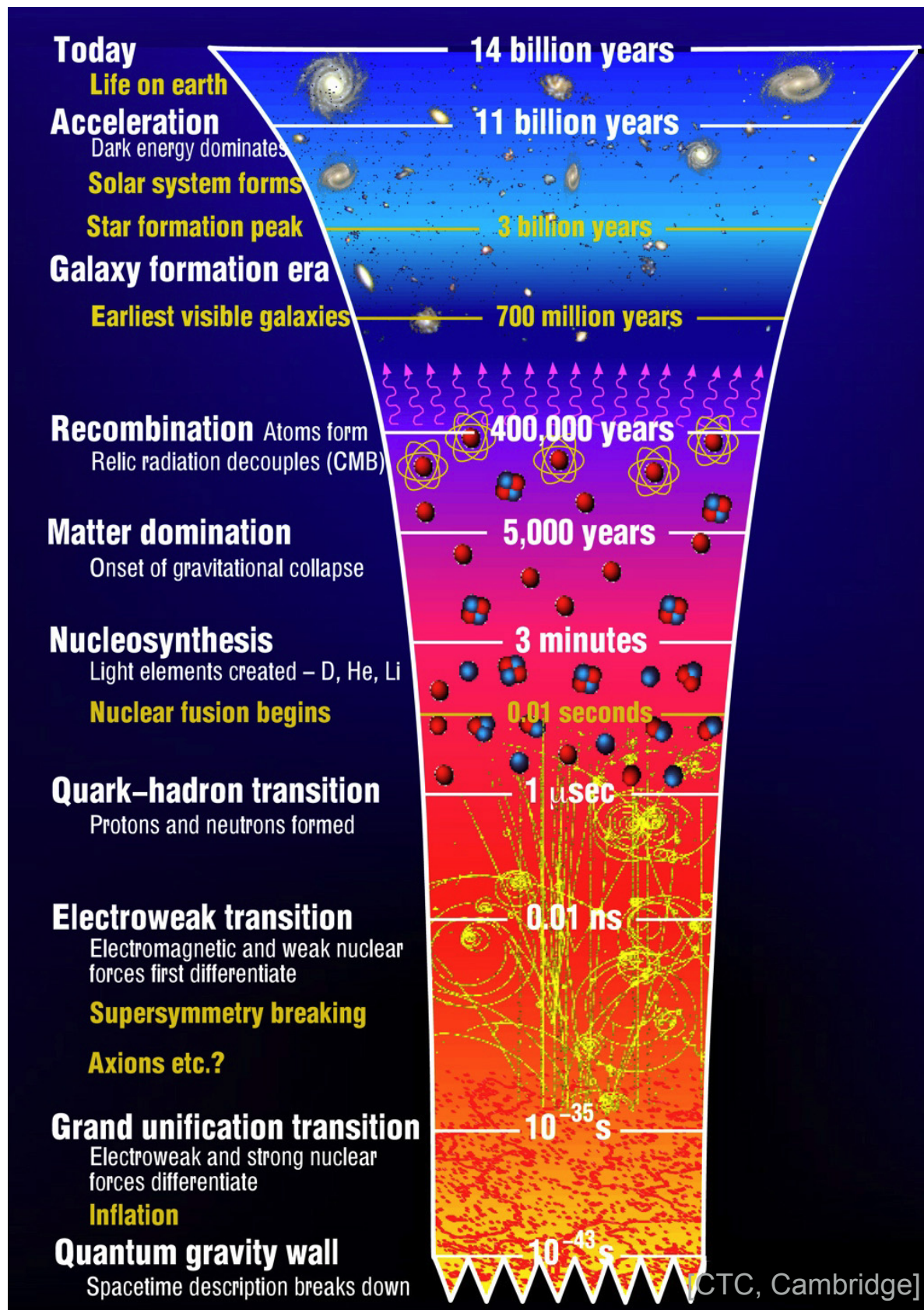
$$\langle h \rangle = 246 \text{ GeV}$$

$$V(H) = -\mu_H^2 |H|^2 + \lambda_H |H|^4$$

Electroweak Symmetry Breaking

Temperature increases





Temperature increases

Zero Temperature

$\langle h \rangle = 246 \text{ GeV}$

$$V(H) = -\mu_H^2 |H|^2 + \lambda_H |H|^4$$

Electroweak Symmetry Breaking

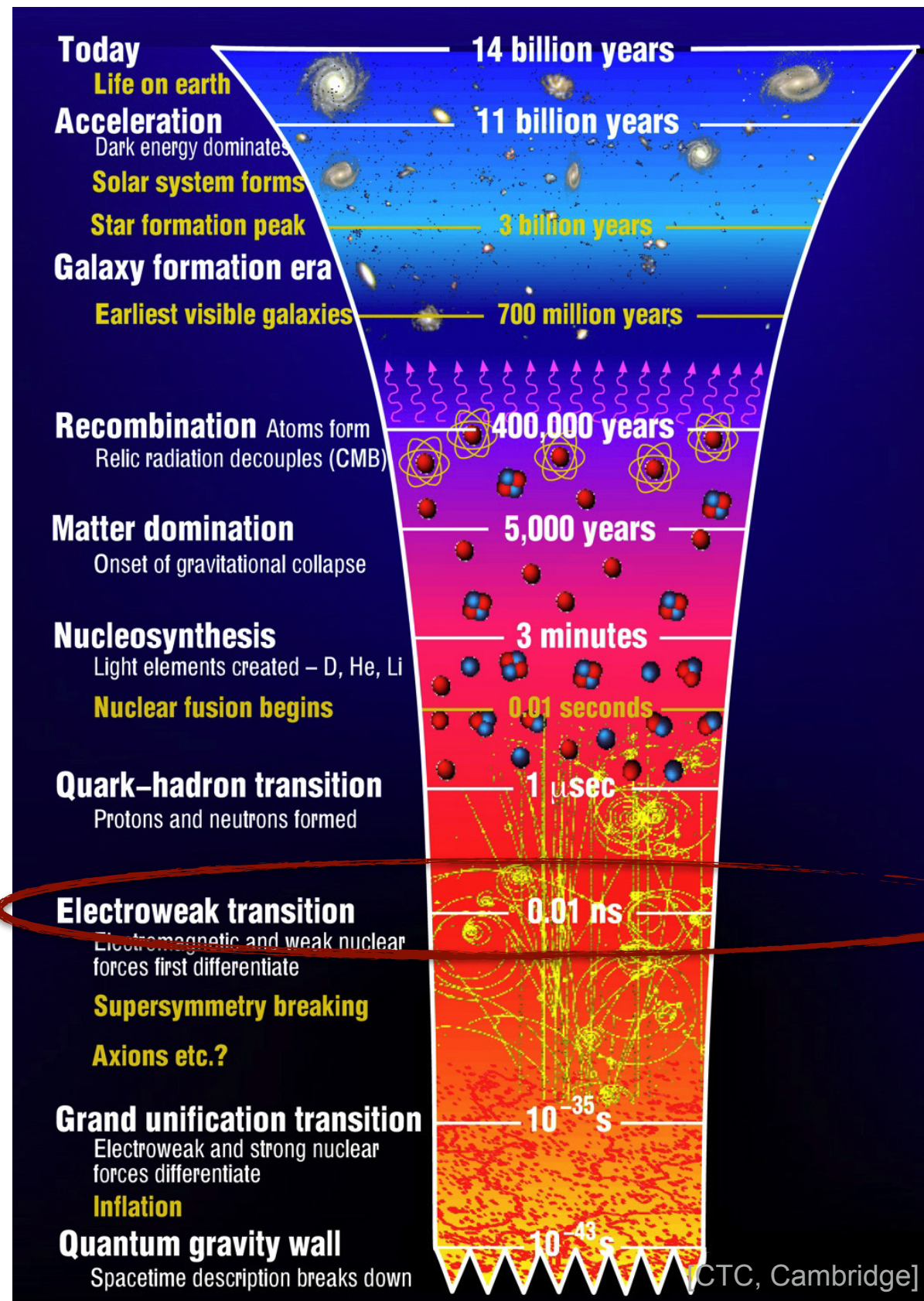
High Temperature

$\langle h \rangle = 0$

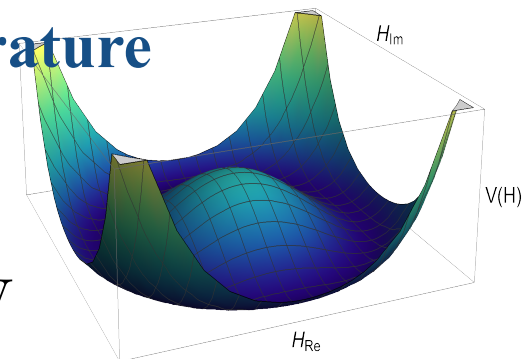
$$V(H) = (c_H T^2 - \mu_H^2) |H|^2 + \tilde{\lambda}_H |H|^4$$

Electroweak Symmetry Preserved

The Standard Model



Zero Temperature



$$\langle h \rangle = 246 \text{ GeV}$$

$$V(H) = -\mu_H^2 |H|^2 + \lambda_H |H|^4$$

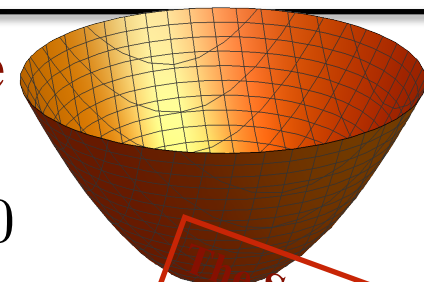
Electroweak Symmetry Breaking



Electroweak Phase Transition



High Temperature



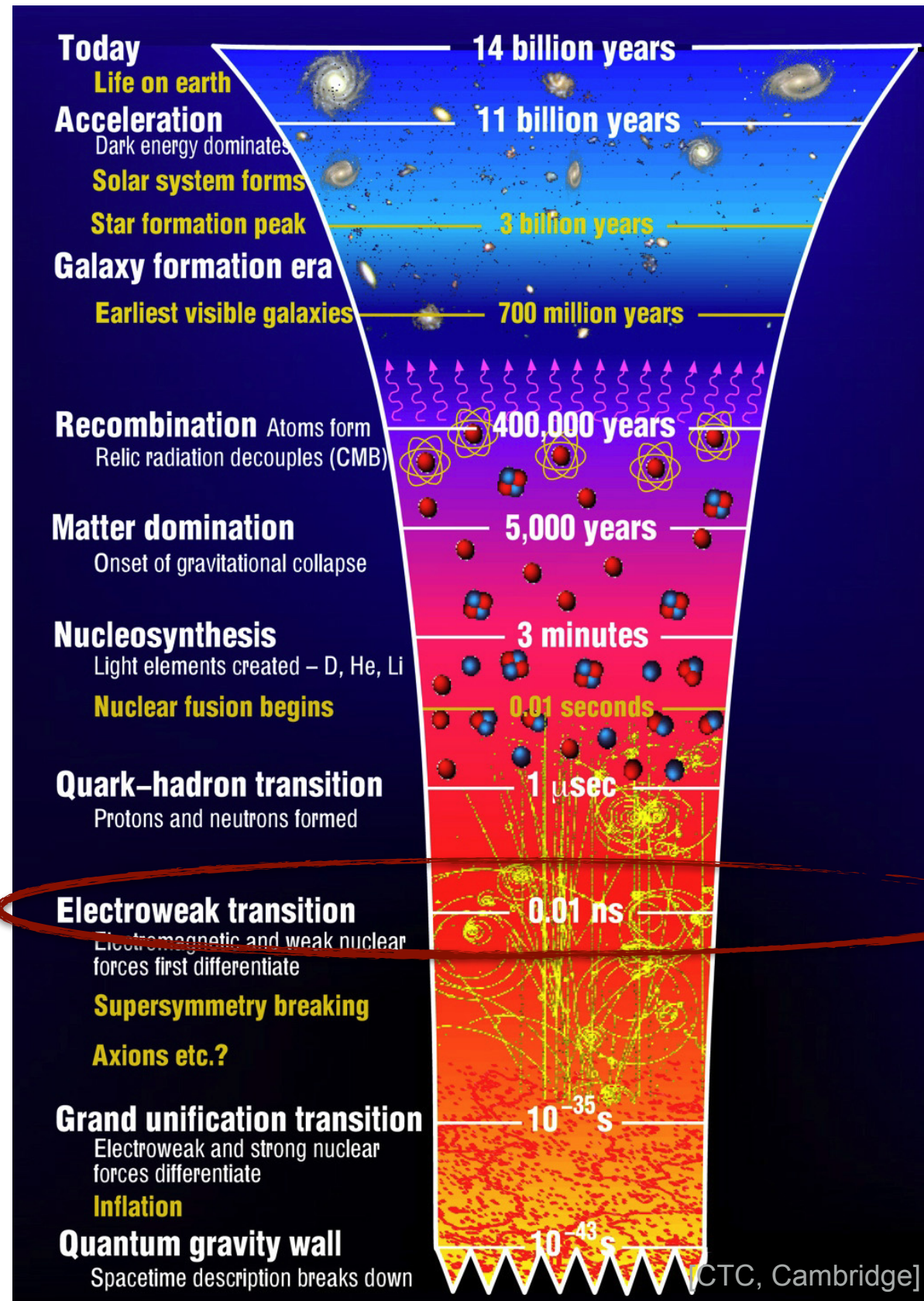
$$\langle h \rangle = 0$$

$$V(H) = (c_H T^2 - \mu_H^2) |H|^2 + \tilde{\lambda}_H |H|^4$$

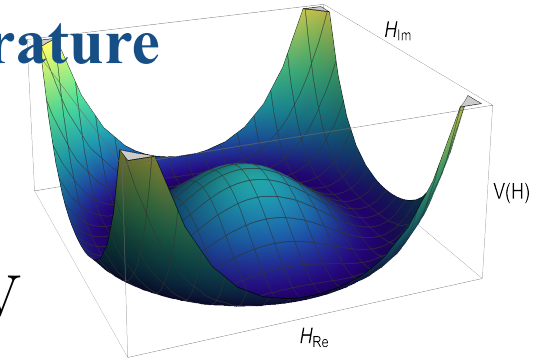
Electroweak Symmetry Preserved

The Standard Model

Nature of the phase transition



Zero Temperature



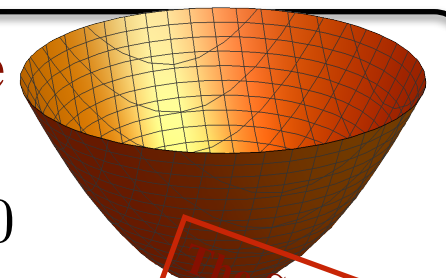
$$\langle h \rangle = 246 \text{ GeV}$$

$$V(H) = -\mu_H^2 |H|^2 + \lambda_H |H|^4$$

Electroweak Symmetry Breaking

Electroweak Phase Transition

High Temperature



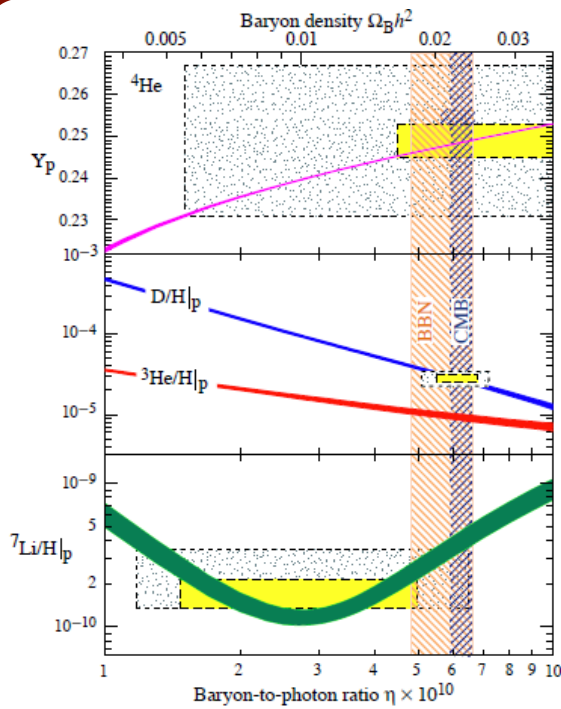
$$\langle h \rangle = 0$$

$$V(H) = (c_H T^2 - \mu_H^2) |H|^2 + \tilde{\lambda}_H |H|^4$$

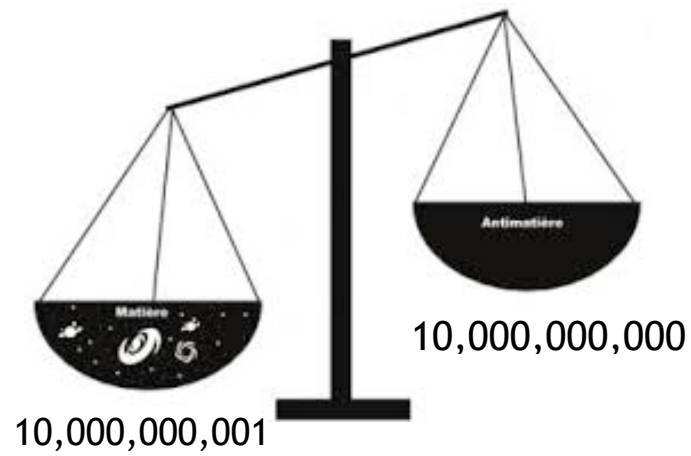
Electroweak Symmetry Preserved



A bonus for answering the question

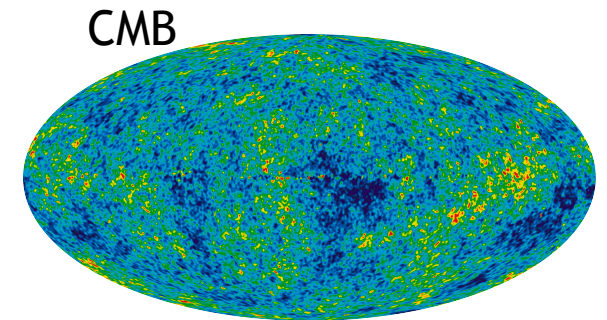
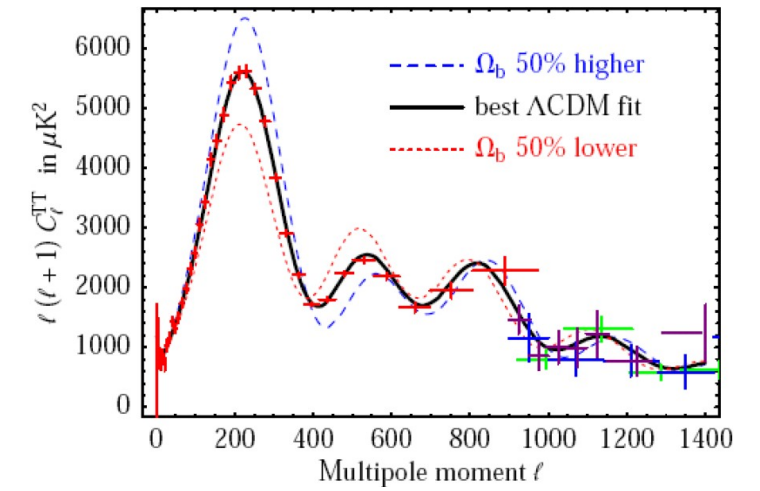


Big Bang Nucleosynthesis

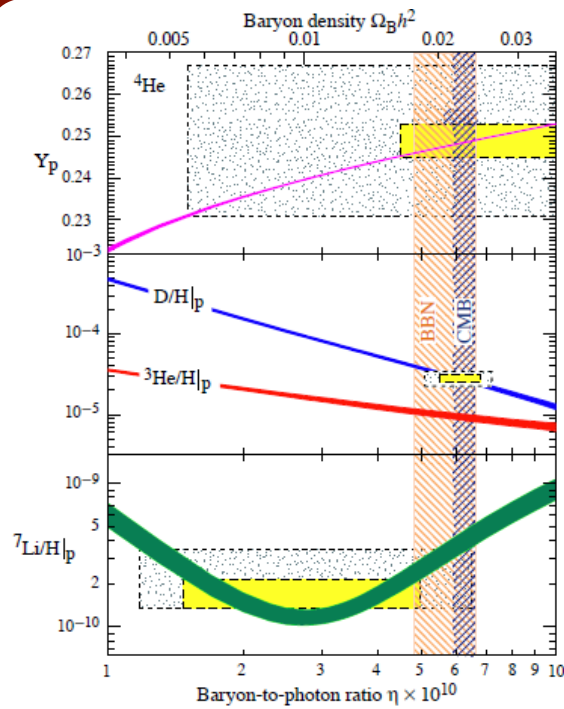


Baryon Asymmetry of the Universe

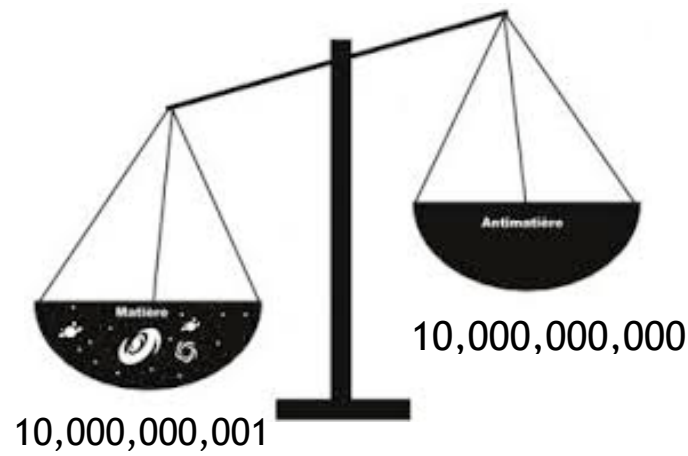
$$\eta = \frac{n_B}{n_\gamma} = (6.11 \pm 0.19) \times 10^{-10}$$



A bonus for answering the question

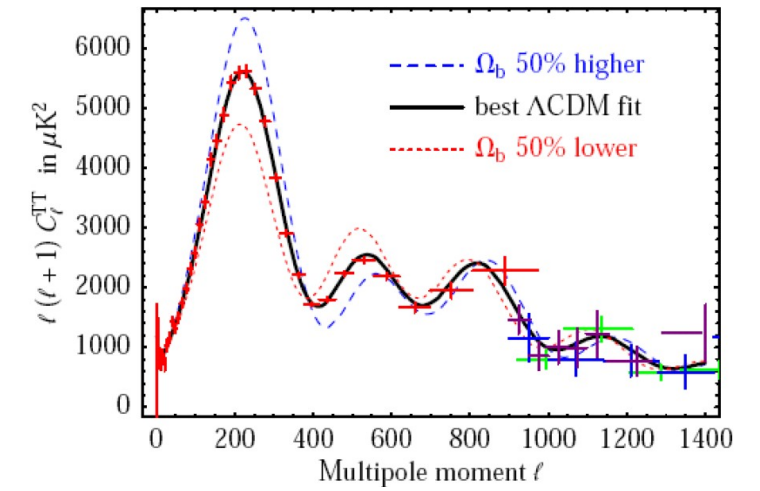


Big Bang Nucleosynthesis

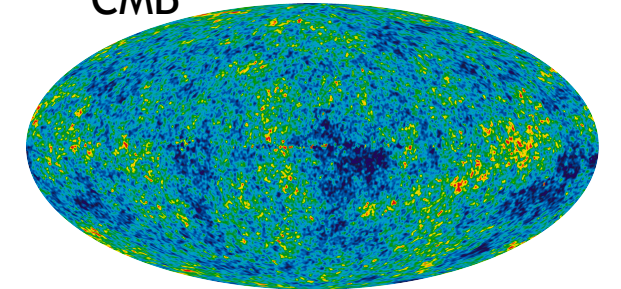


Baryon Asymmetry of the Universe

$$\eta = \frac{n_B}{n_\gamma} = (6.11 \pm 0.19) \times 10^{-10}$$

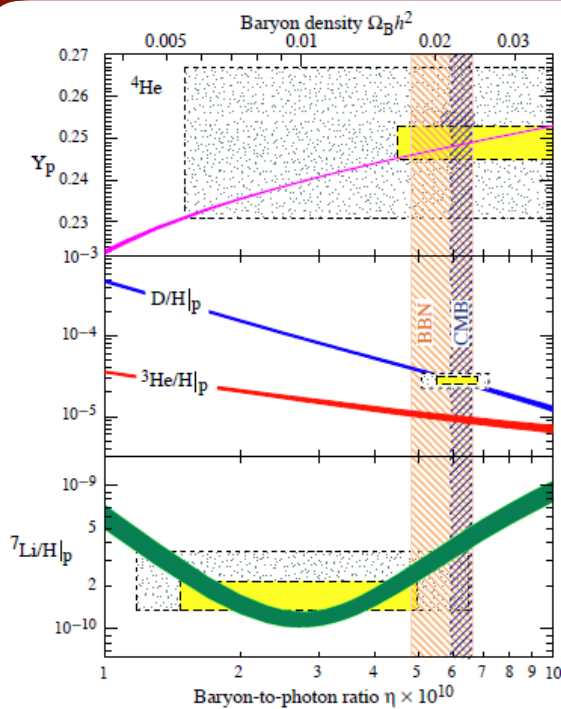


CMB

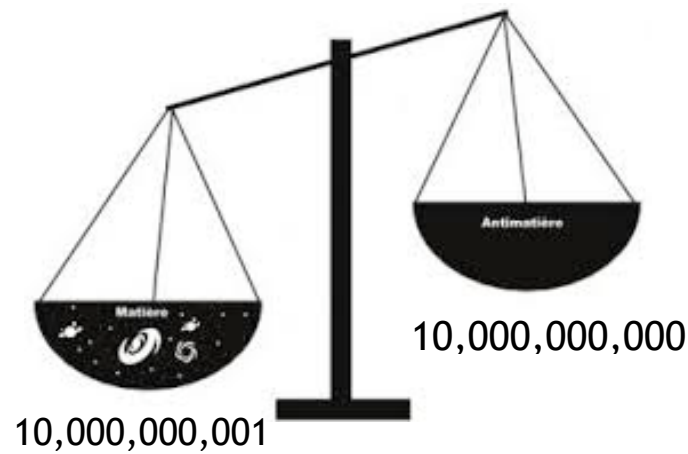


The Standard Model of particle physics could not explain the generation of BAU

A bonus for answering the question

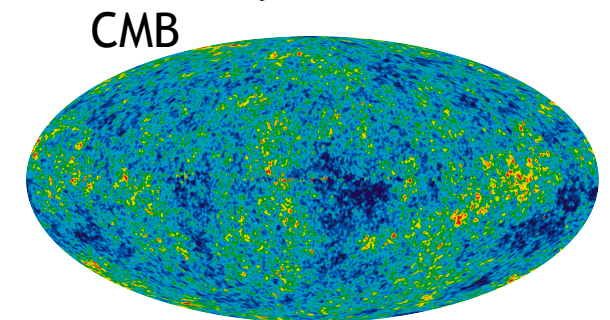
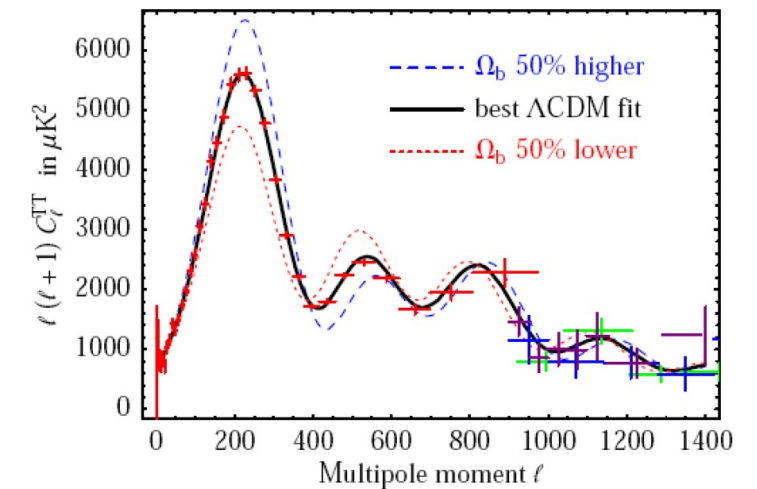


Big Bang Nucleosynthesis



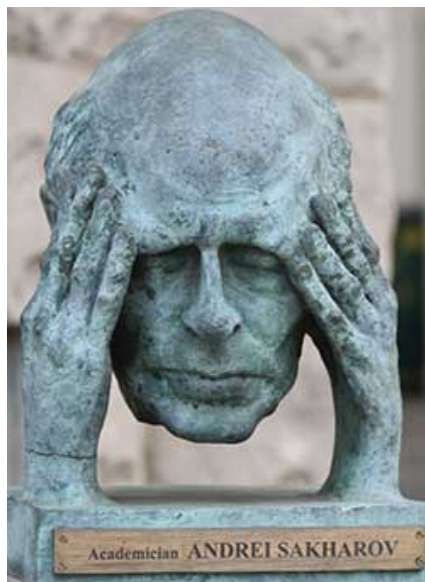
Baryon Asymmetry of the Universe

$$\eta = \frac{n_B}{n_\gamma} = (6.11 \pm 0.19) \times 10^{-10}$$



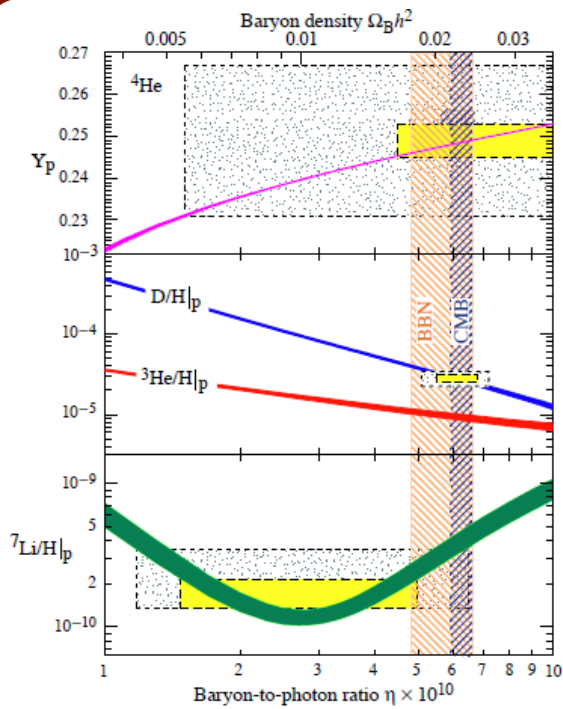
The Standard Model of particle physics could not explain the generation of BAU

Sakharov's conditions for BAU creation

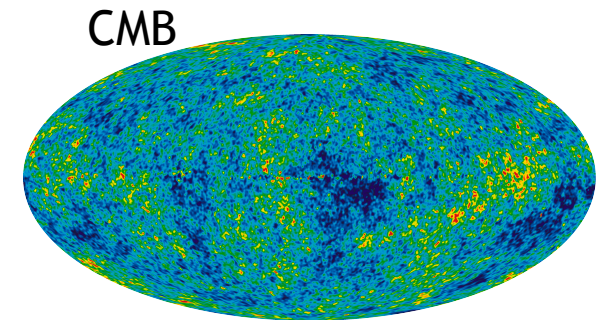
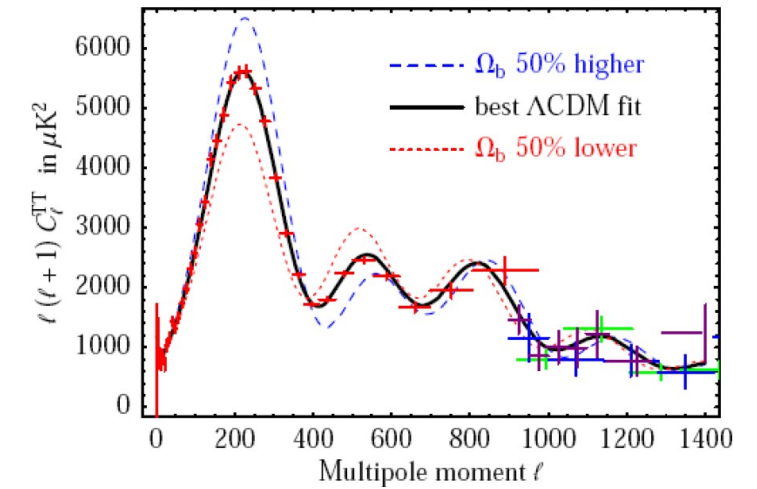
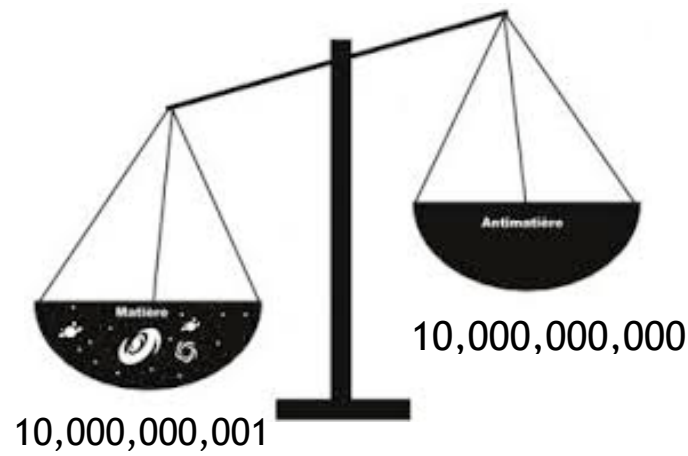


- Baryon number violation
- C and CP violation
- Out-of-equilibrium

A bonus for answering the question



Big Bang Nucleosynthesis

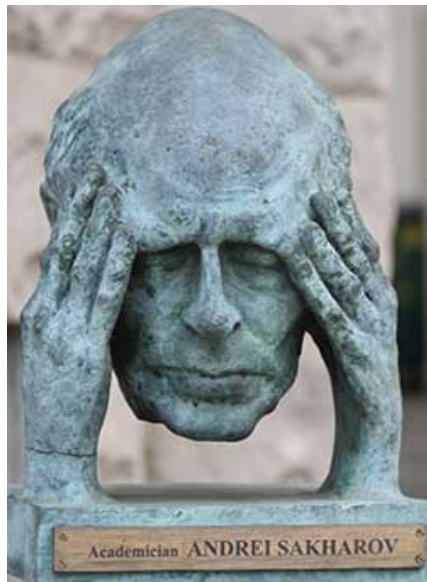


Baryon Asymmetry of the Universe

$$\eta = \frac{n_B}{n_\gamma} = (6.11 \pm 0.19) \times 10^{-10}$$

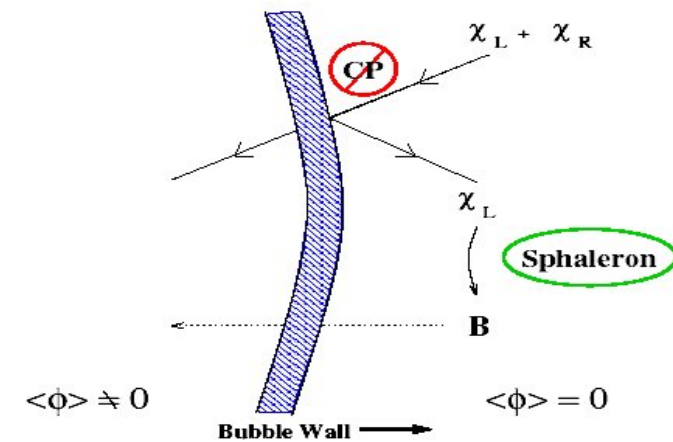
The Standard Model of particle physics could not explain the generation of BAU

Sakharov's conditions for BAU creation

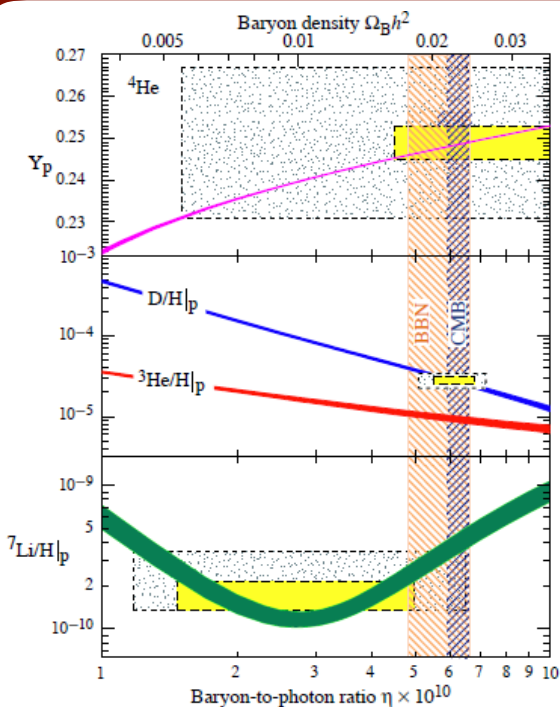


- Baryon number violation
- C and CP violation
- Out-of-equilibrium

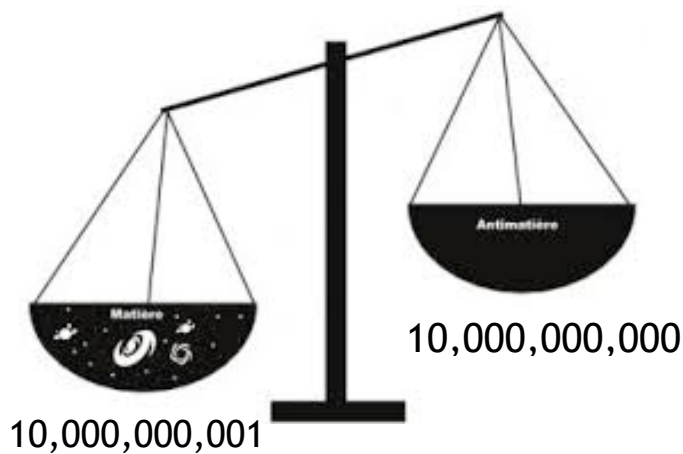
Electroweak Baryogenesis



A bonus for answering the question

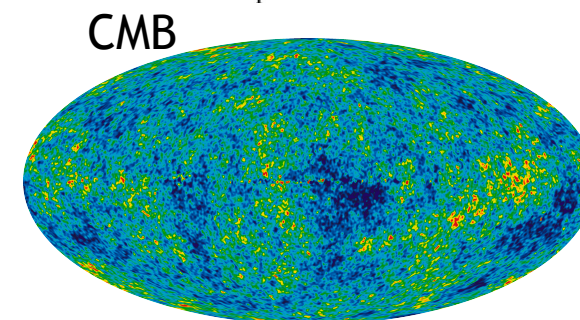
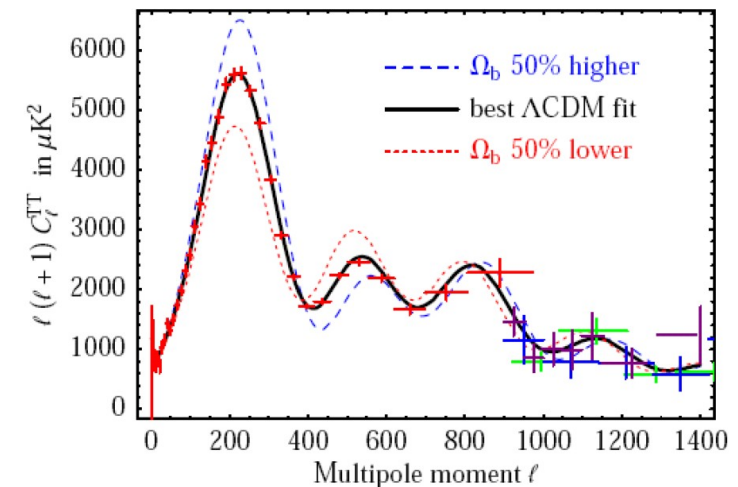


Big Bang Nucleosynthesis



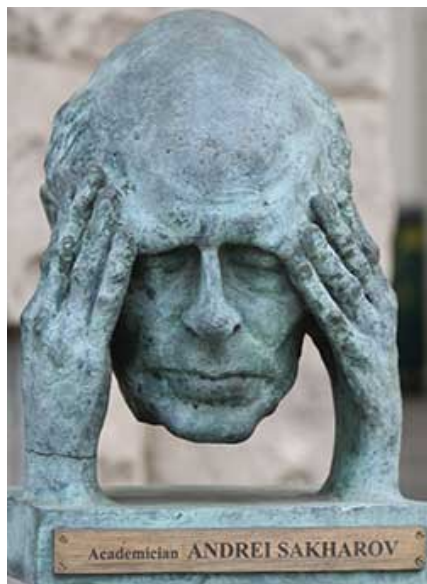
Baryon Asymmetry of the Universe

$$\eta = \frac{n_B}{n_\gamma} = (6.11 \pm 0.19) \times 10^{-10}$$



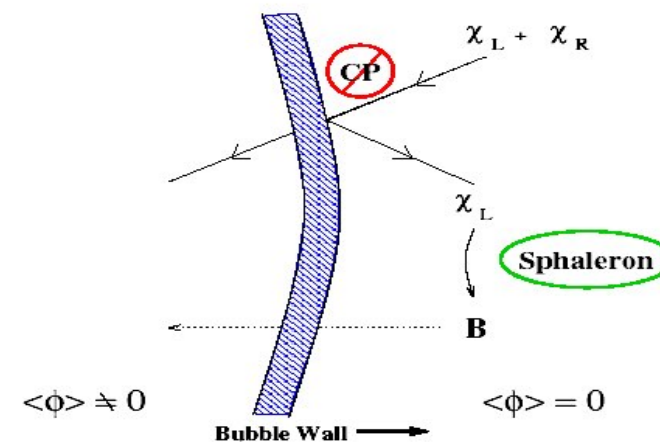
The Standard Model of particle physics could not explain the generation of BAU

Sakharov's conditions for BAU creation



- Baryon number violation
- C and CP violation
- **Out-of-equilibrium**

Electroweak Baryogenesis



Strongly First Order
Electroweak Phase Transition

Electroweak phase transition and Higgs properties (at zero T)

$$V_{\text{EFF}}(h, T) = c_H(T^2 - T_0^2)h^2 - (ET + e)h^3 + \frac{\widetilde{\lambda}_H}{2}h^4 + \dots$$

$$\text{Order of the Phase Transition} \propto \frac{E + e/T}{\widetilde{\lambda}_H} \gtrsim 1$$

Electroweak phase transition and Higgs properties (at zero T)

$$V_{\text{EFF}}(h, T) = c_H(T^2 - T_0^2)h^2 - (ET + e)h^3 + \frac{\widetilde{\lambda}_H}{2}h^4 + \dots$$

$$\text{Order of the Phase Transition} \propto \frac{E + e/T}{\widetilde{\lambda}_H} \gtrsim 1$$

$$\widetilde{\lambda}_H \sim \lambda_H \left(1 + \alpha \log \frac{h^2}{M^2} \right)$$

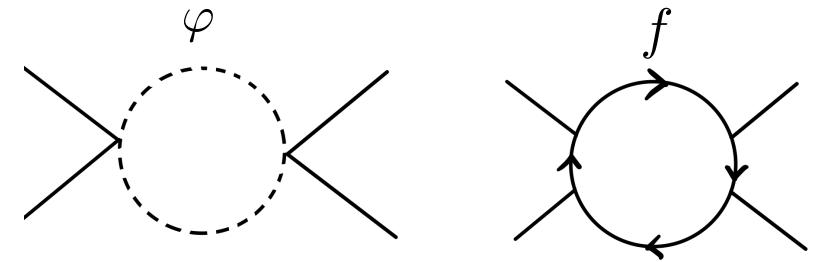
Electroweak phase transition and Higgs properties (at zero T)

$$V_{\text{EFF}}(h, T) = c_H(T^2 - T_0^2)h^2 - (ET + e)h^3 + \frac{\widetilde{\lambda}_H}{2}h^4 + \dots$$

$$\text{Order of the Phase Transition} \propto \frac{E + e/T}{\widetilde{\lambda}_H} \gtrsim 1$$

□ Zero Temperature loop effects

$$\widetilde{\lambda}_H \sim \lambda_H \left(1 + \alpha \log \frac{h^2}{M^2} \right)$$



E.g. [Espinosa, Quiros '07], [Kondo et al '91], [Cline, Lemieux '97], ...

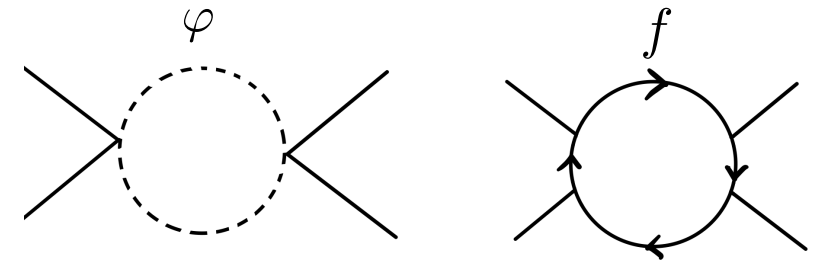
Electroweak phase transition and Higgs properties (at zero T)

$$V_{\text{EFF}}(h, T) = c_H(T^2 - T_0^2)h^2 - (ET + e)h^3 + \frac{\widetilde{\lambda}_H}{2}h^4 + \dots$$

$$\text{Order of the Phase Transition} \propto \frac{E + e/T}{\widetilde{\lambda}_H} \gtrsim 1$$

□ Zero Temperature loop effects

$$\widetilde{\lambda}_H \sim \lambda_H \left(1 + \alpha \log \frac{h^2}{M^2} \right)$$



E.g. [Espinosa, Quiros '07], [Kondo et al '91], [Cline, Lemieux '97], ...

$$Eh^3 \sim (m_{\text{eff}}(h, T_c))^{3/2} \sim \lambda^{3/2} h^3$$

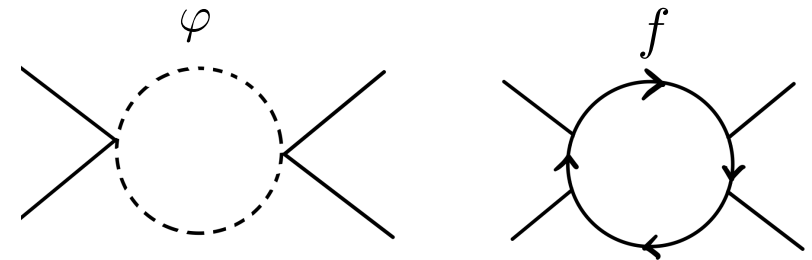
Electroweak phase transition and Higgs properties (at zero T)

$$V_{\text{EFF}}(h, T) = c_H(T^2 - T_0^2)h^2 - (ET + e)h^3 + \frac{\tilde{\lambda}_H}{2}h^4 + \dots$$

$$\text{Order of the Phase Transition} \propto \frac{E + e/T}{\tilde{\lambda}_H} \gtrsim 1$$

□ Zero Temperature loop effects

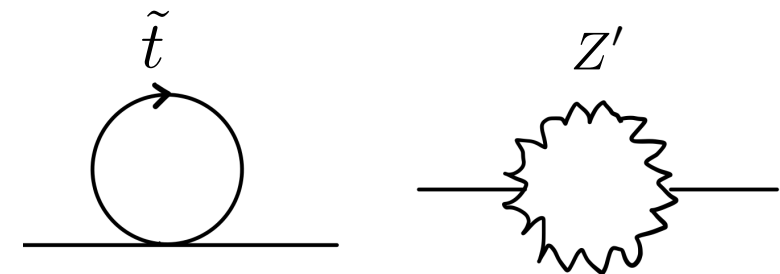
$$\tilde{\lambda}_H \sim \lambda_H \left(1 + \alpha \log \frac{h^2}{M^2} \right)$$



E.g. [Espinosa, Quiros '07], [Kondo et al '91], [Cline, Lemieux '97], ...

□ Thermal effects

$$Eh^3 \sim (m_{\text{eff}}(h, T_c))^{3/2} \sim \lambda^{3/2} h^3$$



E.g. [Anderson, Hall '92], [Cohen, Morrissey, Pierce '12], [Chowdhury et al '12] [Carena, Quiros, Wagner, '96], [Delepine, et al '96]

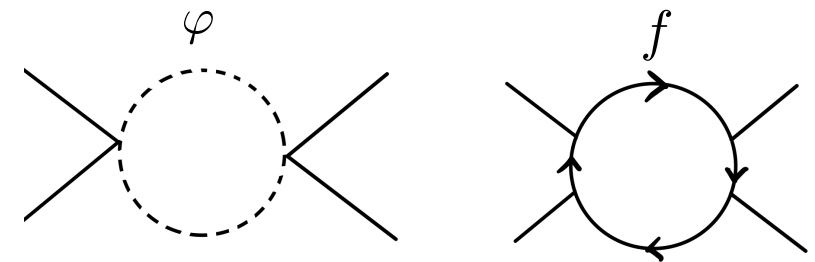
Electroweak phase transition and Higgs properties (at zero T)

$$V_{\text{EFF}}(h, T) = c_H(T^2 - T_0^2)h^2 - (ET + e)h^3 + \frac{\tilde{\lambda}_H}{2}h^4 + \dots$$

$$\text{Order of the Phase Transition} \propto \frac{E + e/T}{\tilde{\lambda}_H} \gtrsim 1$$

□ Zero Temperature loop effects

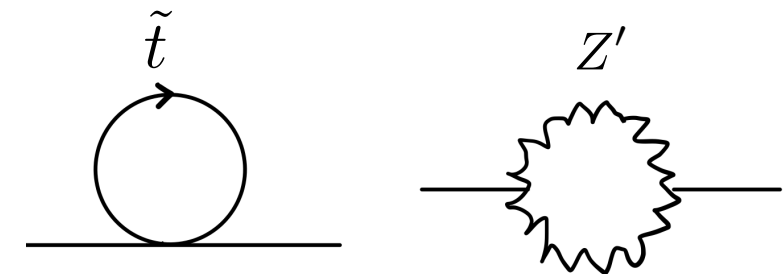
$$\tilde{\lambda}_H \sim \lambda_H \left(1 + \alpha \log \frac{h^2}{M^2} \right)$$



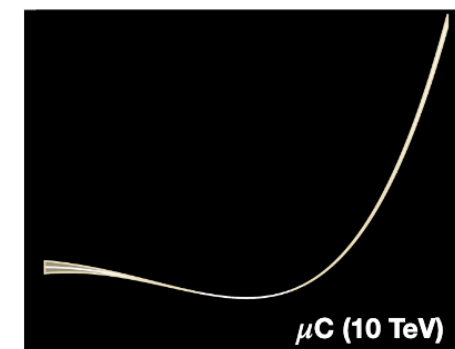
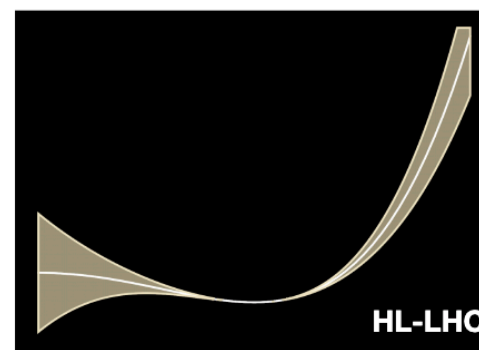
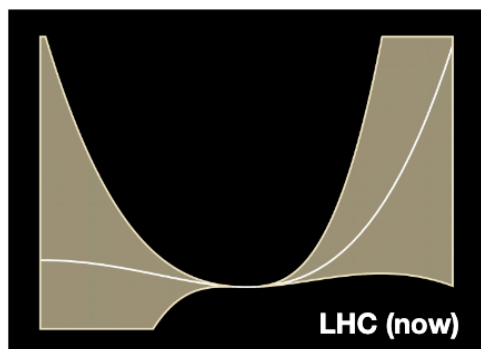
E.g. [Espinosa, Quiros '07], [Kondo et al '91], [Cline, Lemieux '97], ...

□ Thermal effects

$$Eh^3 \sim (m_{\text{eff}}(h, T_c))^{3/2} \sim \lambda^{3/2}h^3$$



E.g. [Anderson, Hall '92], [Cohen, Morrissey, Pierce '12], [Chowdhury et al '12] [Carena, Quiros, Wagner, '96], [Delepine, et al '96]



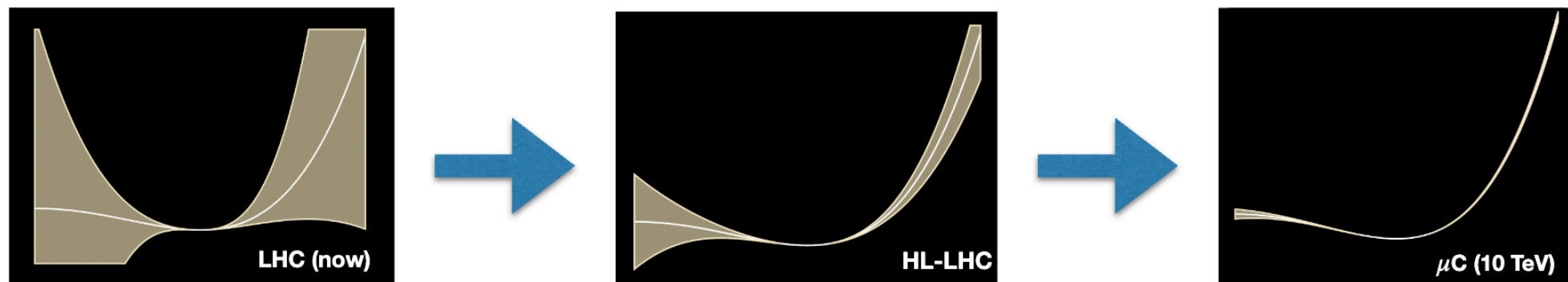
Courtesy of N. Craig

Electroweak phase transition and Higgs properties (at zero T)

$$V_{\text{EFF}}(h, T) = c_H(T^2 - T_0^2)h^2 - (ET + e)h^3 + \frac{\tilde{\lambda}_H}{2}h^4 + \dots$$

$$\text{Order of the Phase Transition} \propto \frac{E + e/T}{\tilde{\lambda}_H} \gtrsim 1$$

□ Tree-level Effects



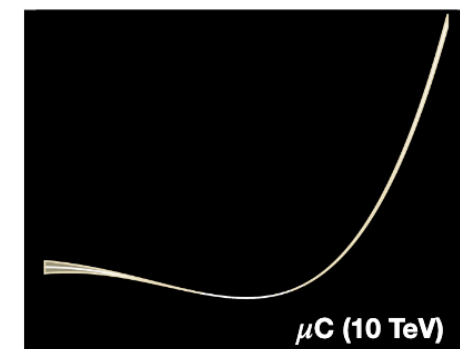
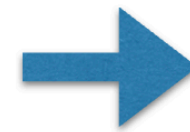
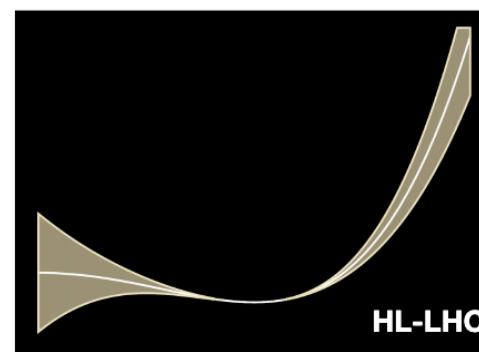
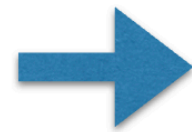
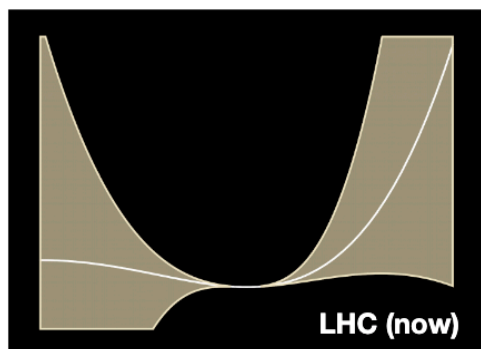
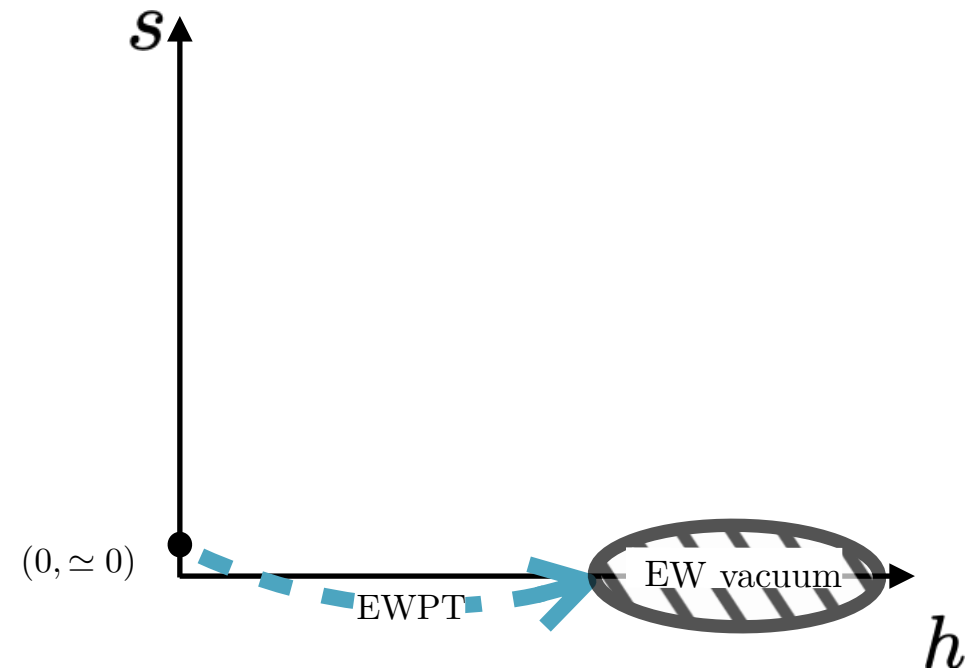
Courtesy of N. Craig

Electroweak phase transition and Higgs properties (at zero T)

$$V_{\text{EFF}}(h, T) = c_H(T^2 - T_0^2)h^2 - (ET + e)h^3 + \frac{\tilde{\lambda}_H}{2}h^4 + \dots$$

Order of the Phase Transition $\propto \frac{E + e/T}{\tilde{\lambda}_H} \gtrsim 1$

□ Tree-level Effects



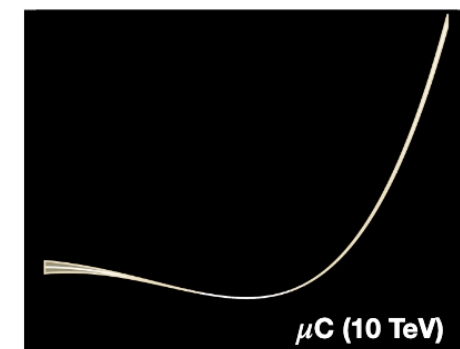
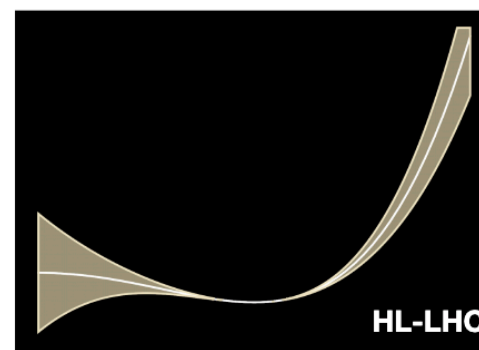
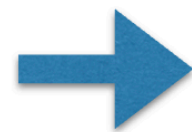
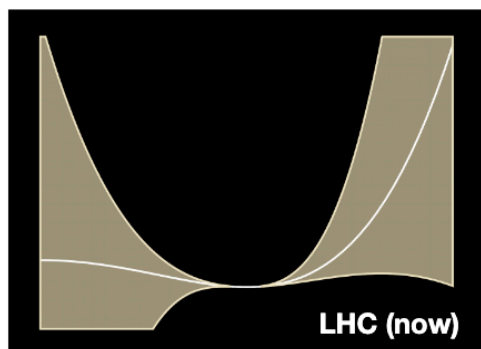
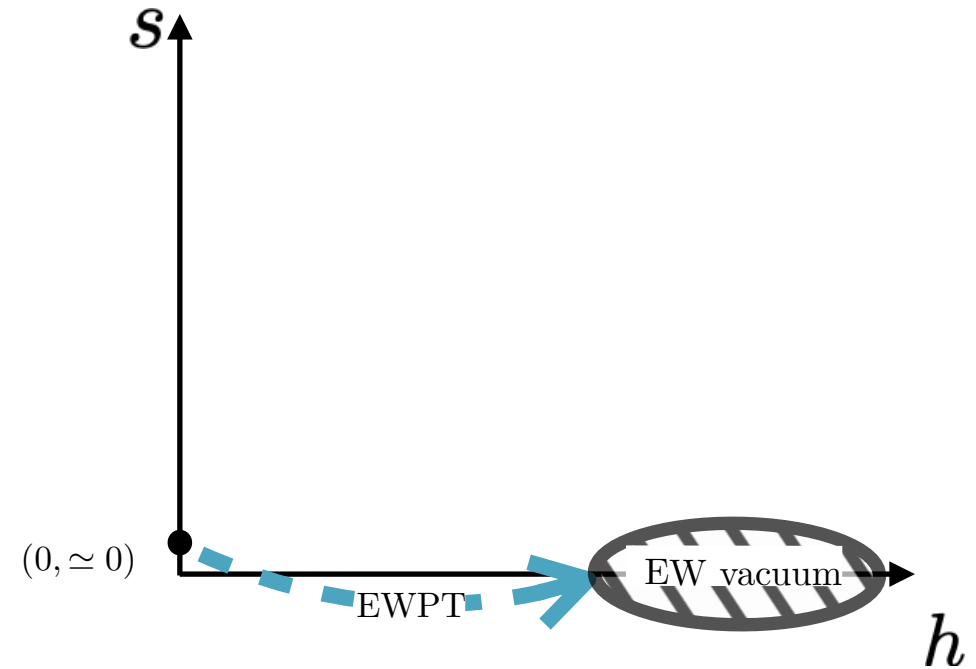
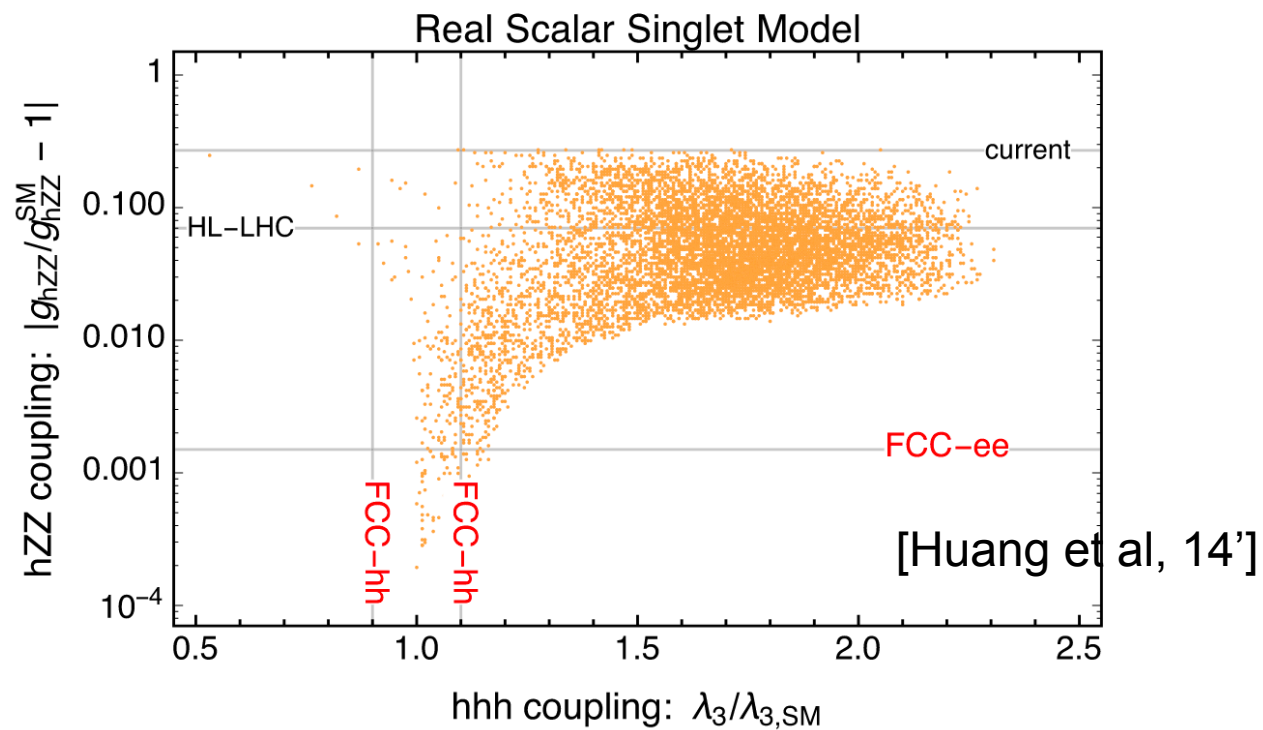
Courtesy of N. Craig

Electroweak phase transition and Higgs properties (at zero T)

$$V_{\text{EFF}}(h, T) = c_H(T^2 - T_0^2)h^2 - (ET + e)h^3 + \frac{\tilde{\lambda}_H}{2}h^4 + \dots$$

$$\text{Order of the Phase Transition} \propto \frac{E + e/T}{\tilde{\lambda}_H} \gtrsim 1$$

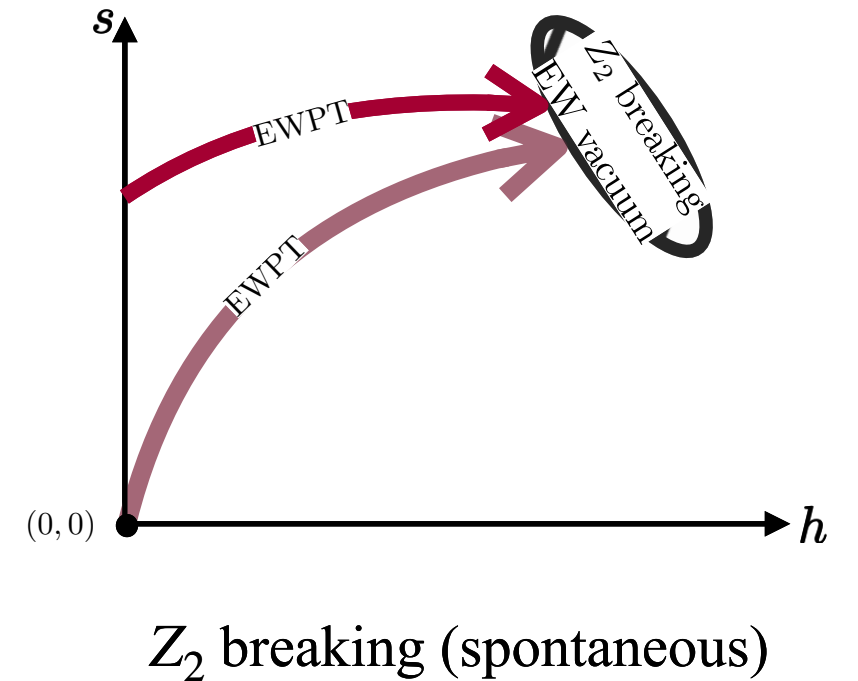
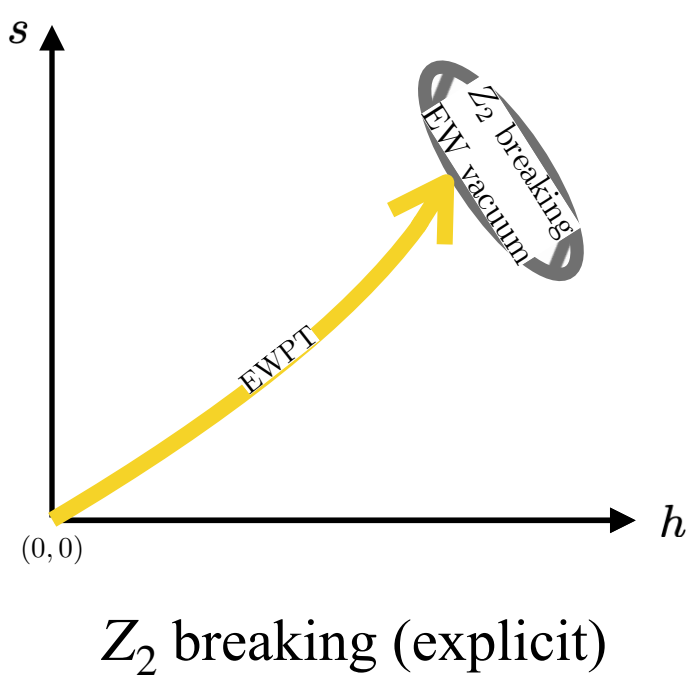
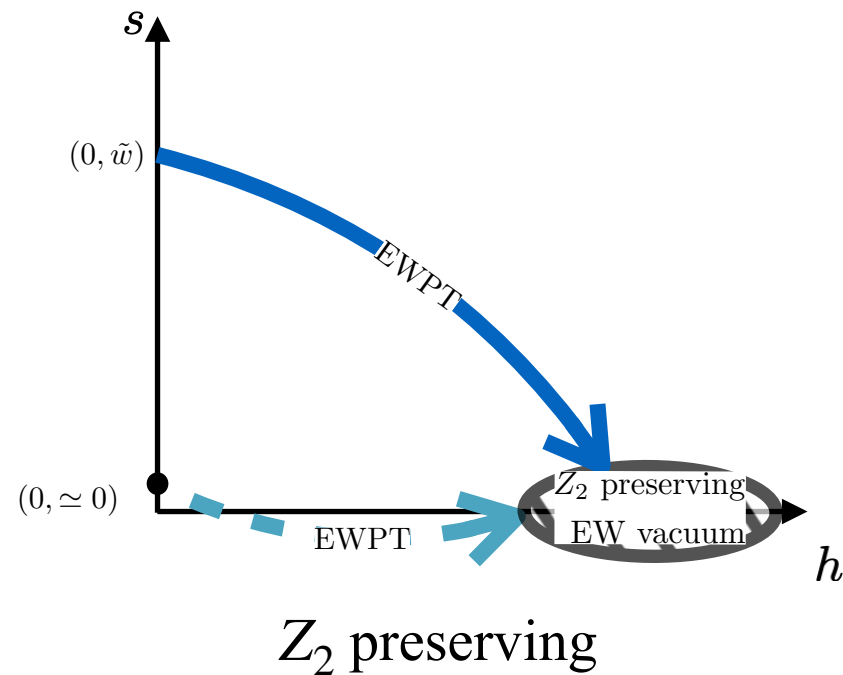
□ Tree-level Effects



Courtesy of N. Craig

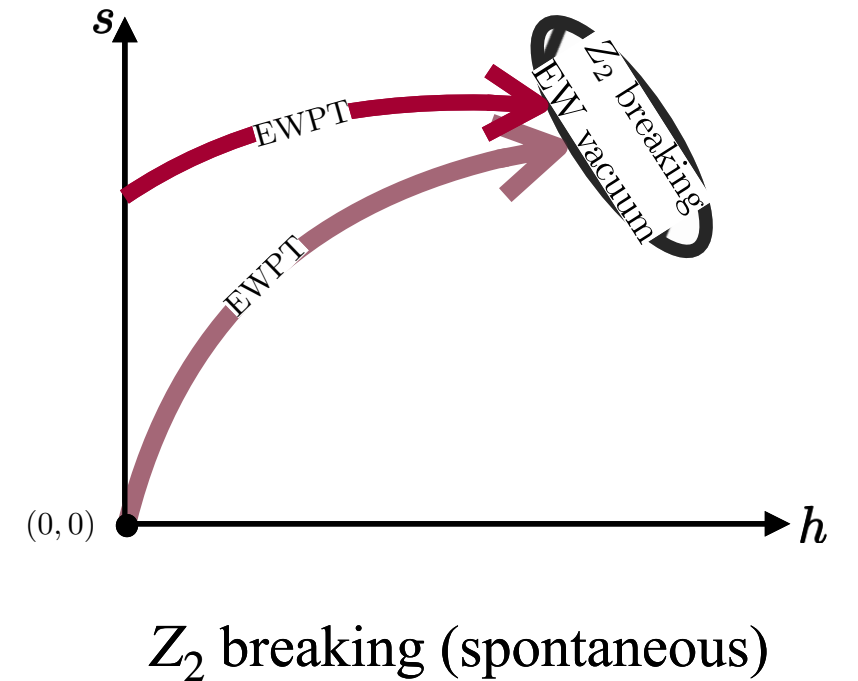
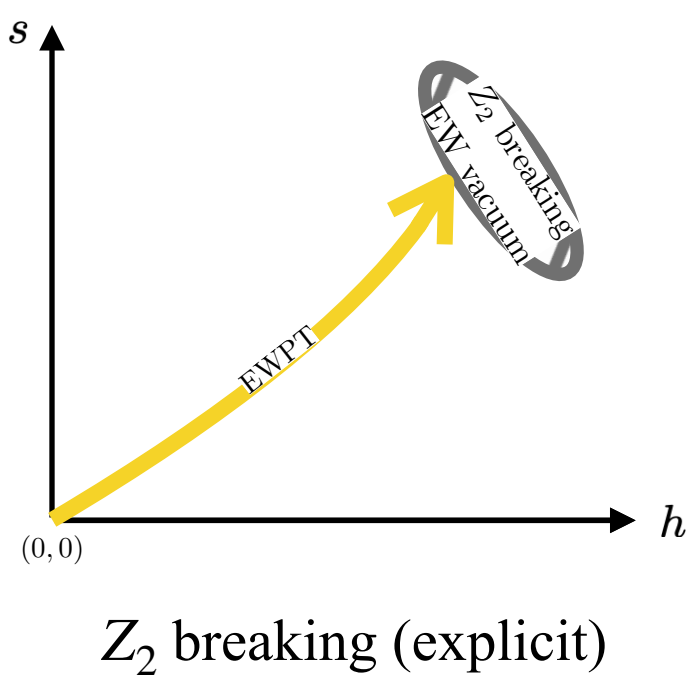
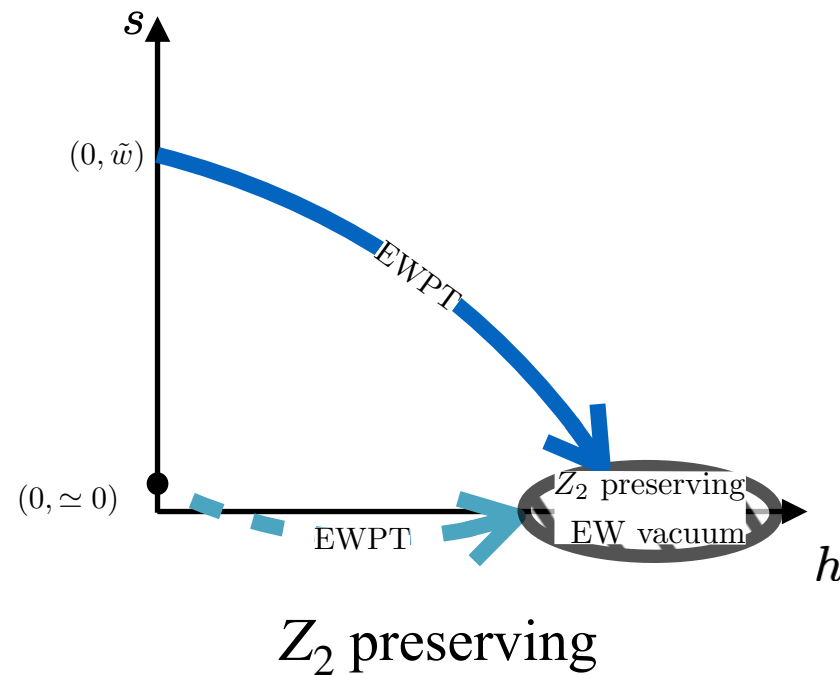
Electroweak phase transition and Higgs properties (at zero T)

□ Tree-level Effects



Electroweak phase transition and Higgs properties (at zero T)

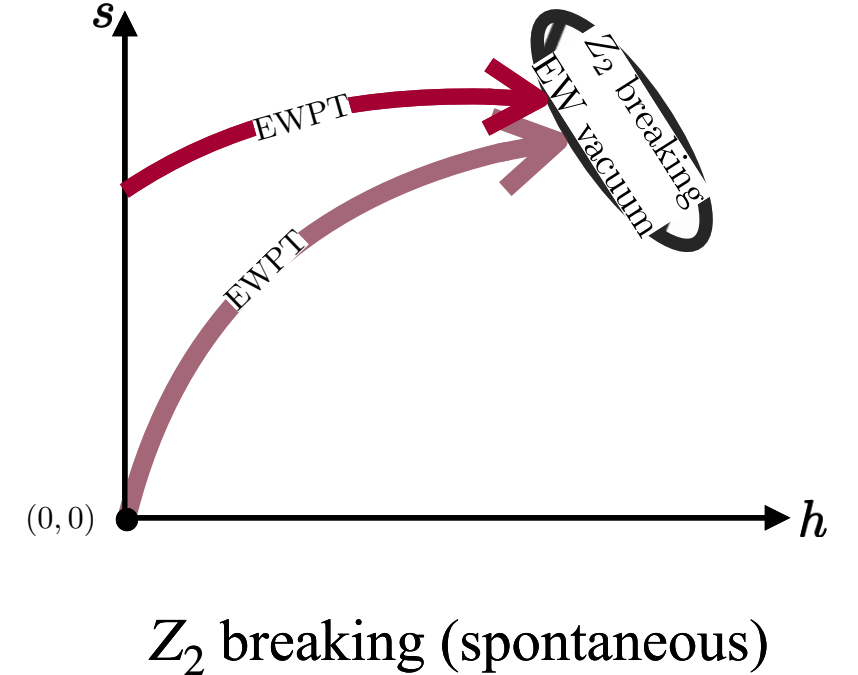
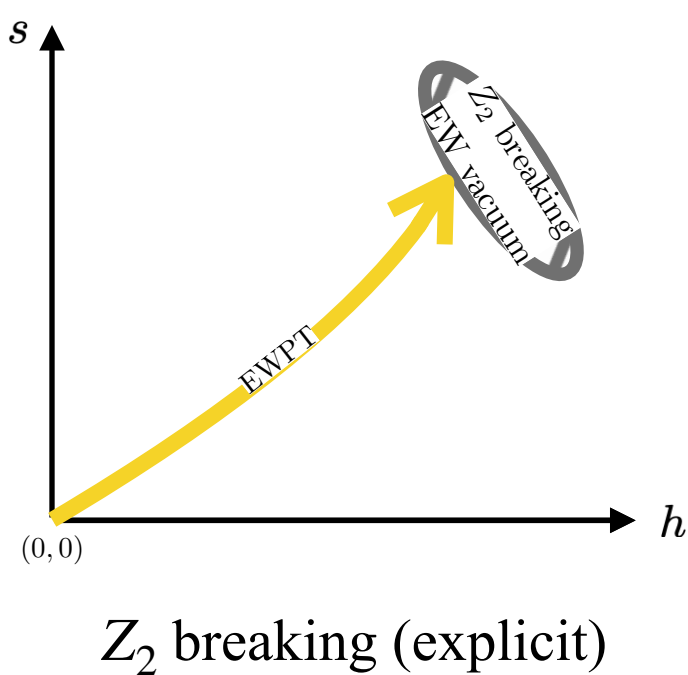
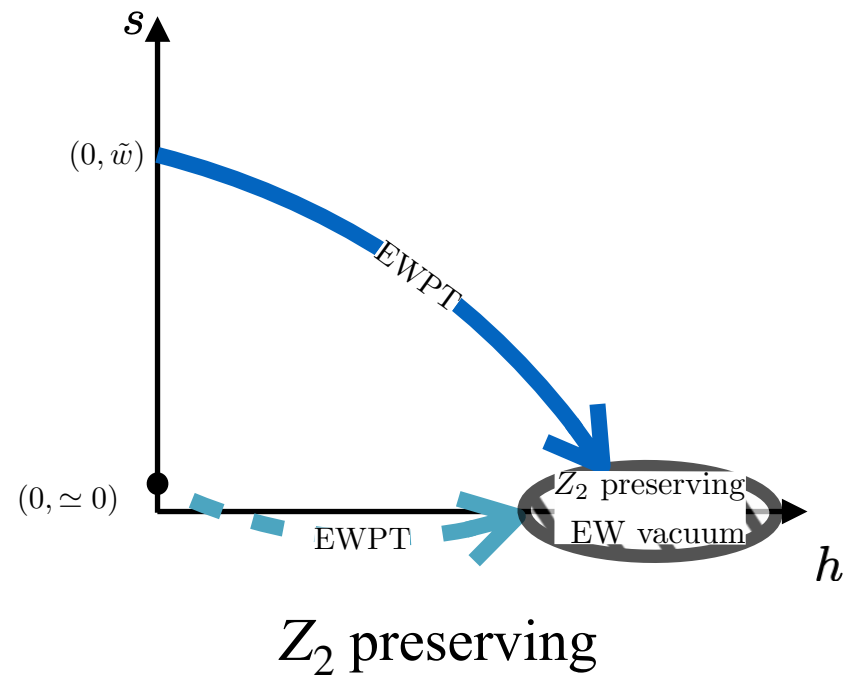
□ Tree-level Effects



Electroweak phase transition and Higgs properties (at zero T)

$$V_0(h, s) = -\frac{1}{2}\mu_h^2 h^2 + \frac{1}{4}\lambda_h h^4 + \frac{1}{2}\mu_s^2 s^2 + \frac{1}{4}\lambda_s s^4 + \frac{1}{4}\lambda_m h^2 s^2 + (\text{explicit } Z_2 - \text{breaking terms})$$

□ Tree-level Effects

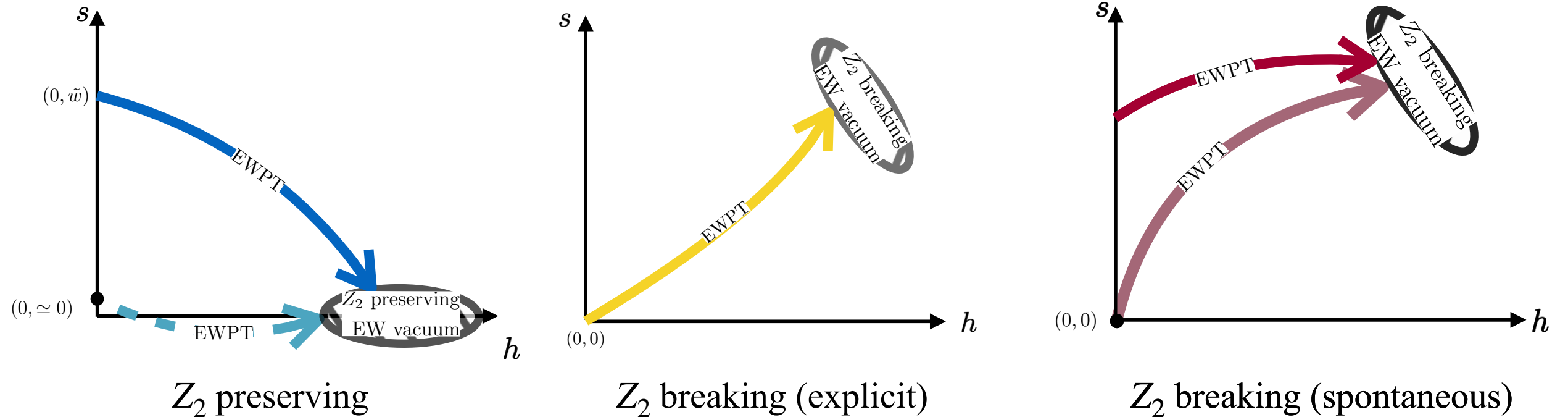


Electroweak phase transition and Higgs properties (at zero T)

$$V_0(h, s) = -\frac{1}{2}\mu_h^2 h^2 + \frac{1}{4}\lambda_h h^4 + \frac{1}{2}\mu_s^2 s^2 + \frac{1}{4}\lambda_s s^4 + \frac{1}{4}\lambda_m h^2 s^2 + (\text{explicit } Z_2 - \text{breaking terms})$$

$$\rightarrow V_{\text{EFF}}(h, s, T)$$

□ Tree-level Effects



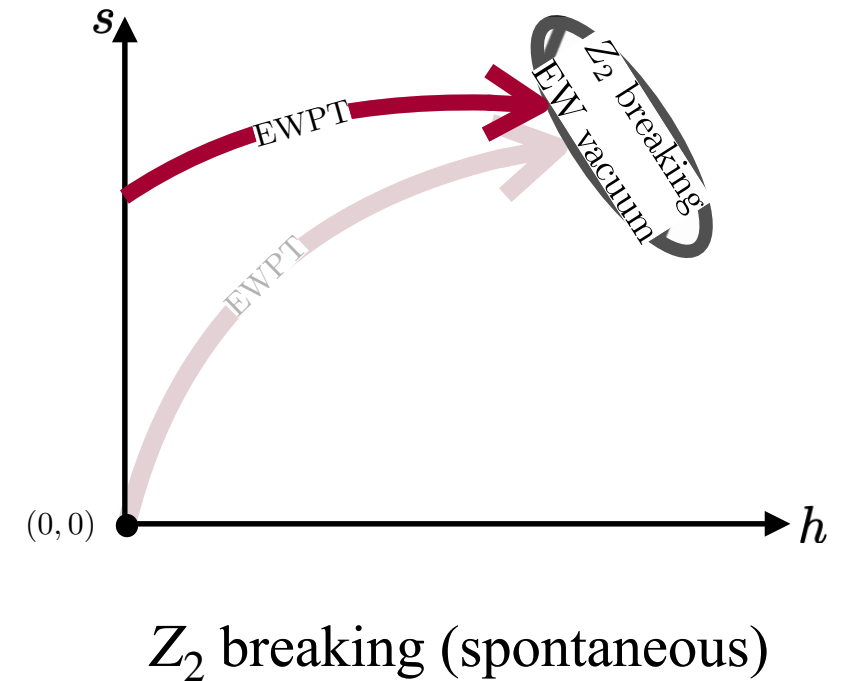
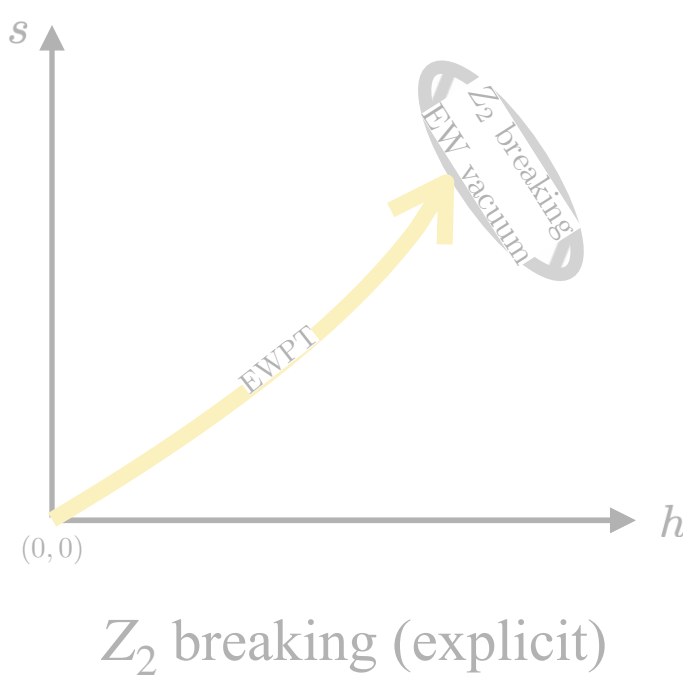
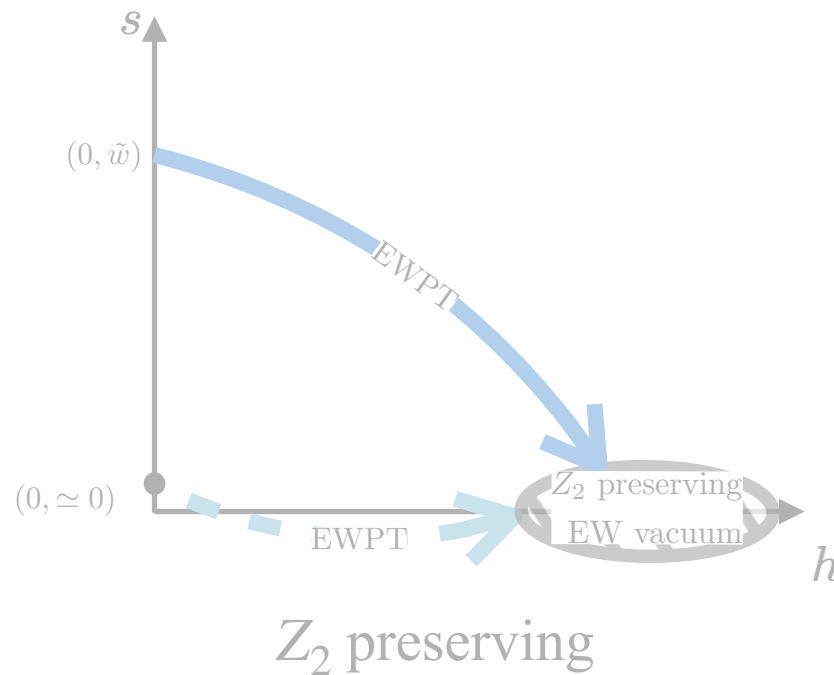
Electroweak phase transition and Higgs properties (at zero T)

$$V_0(h, s) = -\frac{1}{2}\mu_h^2 h^2 + \frac{1}{4}\lambda_h h^4 + \frac{1}{2}\mu_s^2 s^2 + \frac{1}{4}\lambda_s s^4 + \frac{1}{4}\lambda_m h^2 s^2 + (\text{explicit } Z_2 - \text{breaking terms})$$

$$\rightarrow V_{\text{EFF}}(h, s, T)$$

[Carena, et al, 22']

□ Tree-level Effects



Example: Order of the Phase Transition $\propto \left(\lambda_h - \frac{\lambda_m^2}{4\lambda_s} \right)^{-1}$

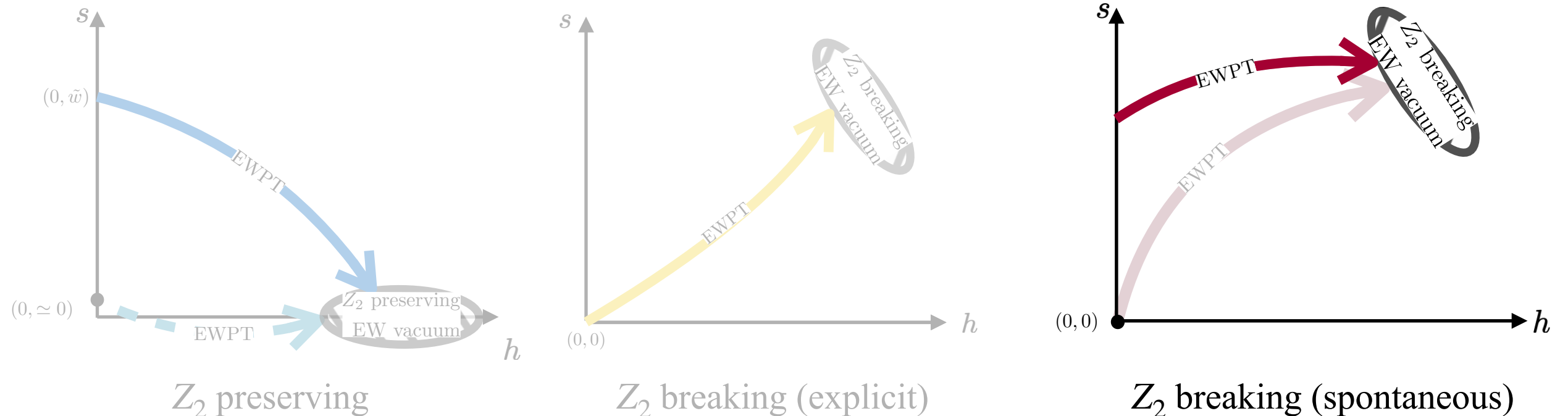
Electroweak phase transition and Higgs properties (at zero T)

$$V_0(h, s) = -\frac{1}{2}\mu_h^2 h^2 + \frac{1}{4}\lambda_h h^4 + \frac{1}{2}\mu_s^2 s^2 + \frac{1}{4}\lambda_s s^4 + \frac{1}{4}\lambda_m h^2 s^2 + (\text{explicit } Z_2 - \text{breaking terms})$$

$$\rightarrow V_{\text{EFF}}(h, s, T)$$

[Carena, et al, 22']

□ Tree-level Effects



Example: Order of the Phase Transition $\propto \left(\lambda_h - \frac{\lambda_m^2}{4\lambda_s} \right)^{-1}$

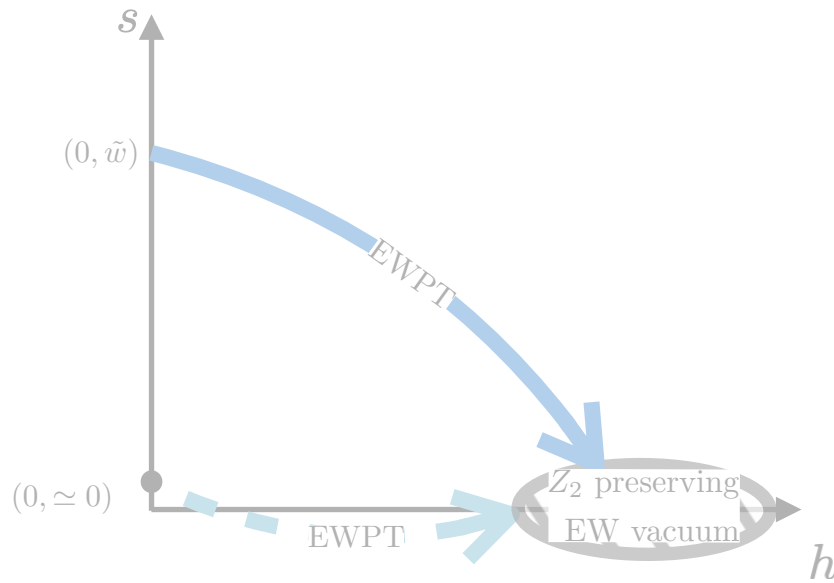
Electroweak phase transition and Higgs properties (at zero T)

$$V_0(h, s) = -\frac{1}{2}\mu_h^2 h^2 + \frac{1}{4}\lambda_h h^4 + \frac{1}{2}\mu_s^2 s^2 + \frac{1}{4}\lambda_s s^4 + \frac{1}{4}\lambda_m h^2 s^2 + (\text{explicit } Z_2 - \text{breaking terms})$$

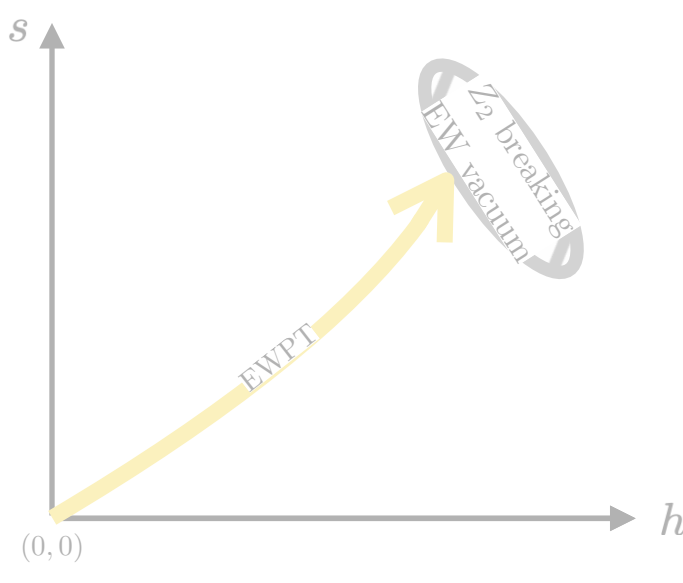
$$\rightarrow V_{\text{EFF}}(h, s, T)$$

[Carena, et al, 22']

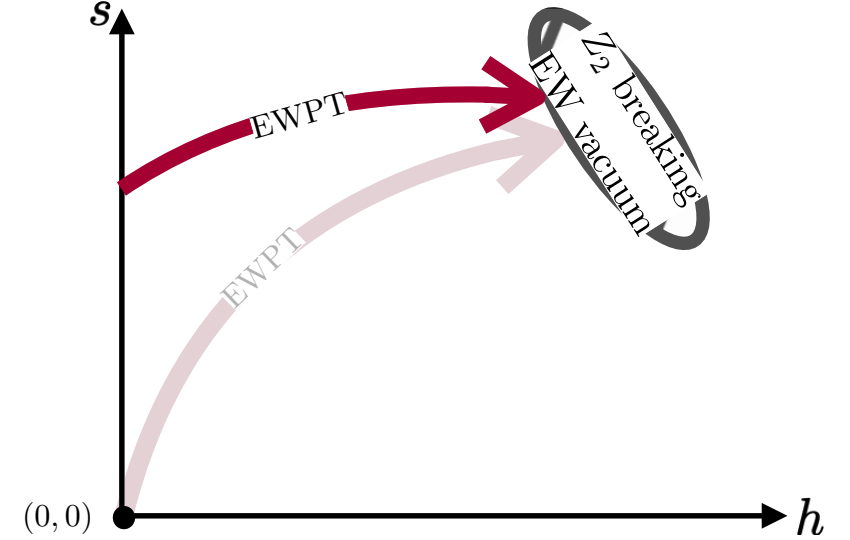
□ Tree-level Effects



Z_2 preserving



Z_2 breaking (explicit)



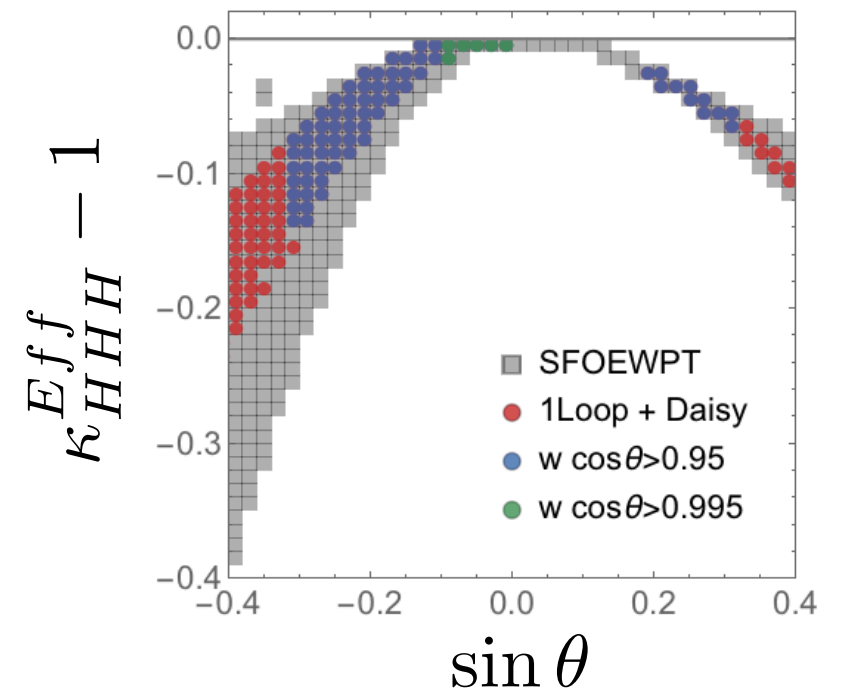
Z_2 breaking (spontaneous)

Example: Order of the Phase Transition $\propto \left(\lambda_h - \frac{\lambda_m^2}{4\lambda_s} \right)^{-1}$

$$\Lambda_{HHH} = \frac{m_H^2 (-\sin^3 \theta + \tan \beta \cos^3 \theta)}{2 \tan \beta v}$$

$$\Lambda_{SHH} = \frac{(2m_H^2 + m_S^2)(\sin \theta + \tan \beta \cos \theta) \sin 2\theta}{4 \tan \beta v}$$

$$\kappa_{HHH}^{\text{Eff}} \equiv \frac{\Lambda_{HHH}^{\text{Eff}}}{\Lambda_{HHH}^{\text{SM}}}$$



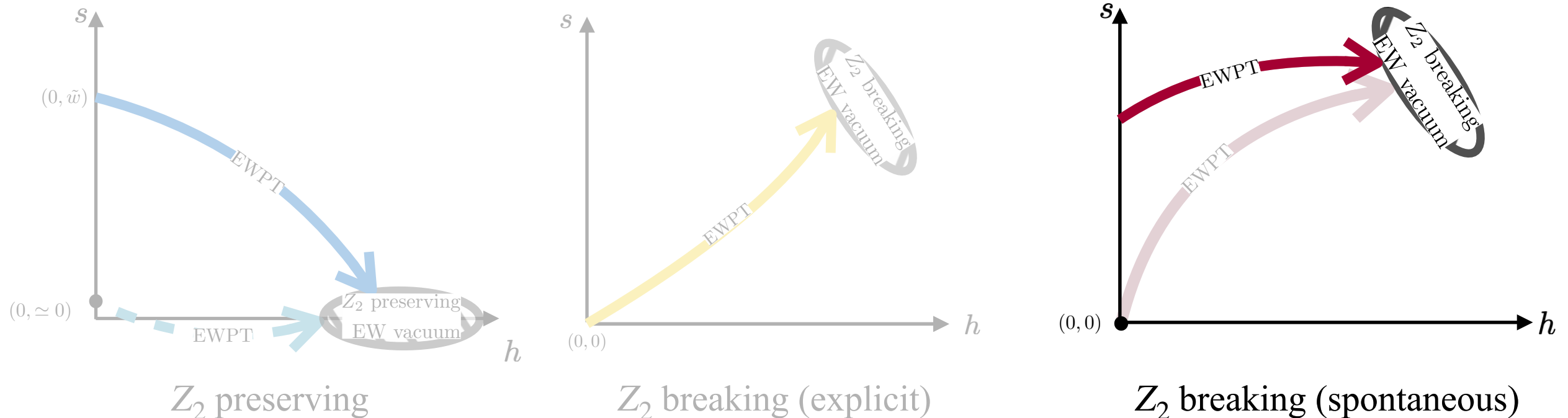
Electroweak phase transition and Higgs properties (at zero T)

$$V_0(h, s) = -\frac{1}{2}\mu_h^2 h^2 + \frac{1}{4}\lambda_h h^4 + \frac{1}{2}\mu_s^2 s^2 + \frac{1}{4}\lambda_s s^4 + \frac{1}{4}\lambda_m h^2 s^2 + (\text{explicit } Z_2 - \text{breaking terms})$$

$$\rightarrow V_{\text{EFF}}(h, s, T)$$

[Carena, et al, 22']

□ Tree-level Effects



Example: Order of the Phase Transition $\propto \left(\lambda_h - \frac{\lambda_m^2}{4\lambda_s} \right)^{-1} \propto 1 + \sin^2 \theta \left(\frac{(125\text{GeV})^2}{m_S^2} - 1 \right)$

- $\sin \theta \lesssim 0.4$ bounded by **Higgs precision measurements**
- A firm prediction of a **light scalar**
- **BR($H \rightarrow SS$) bounded from below**

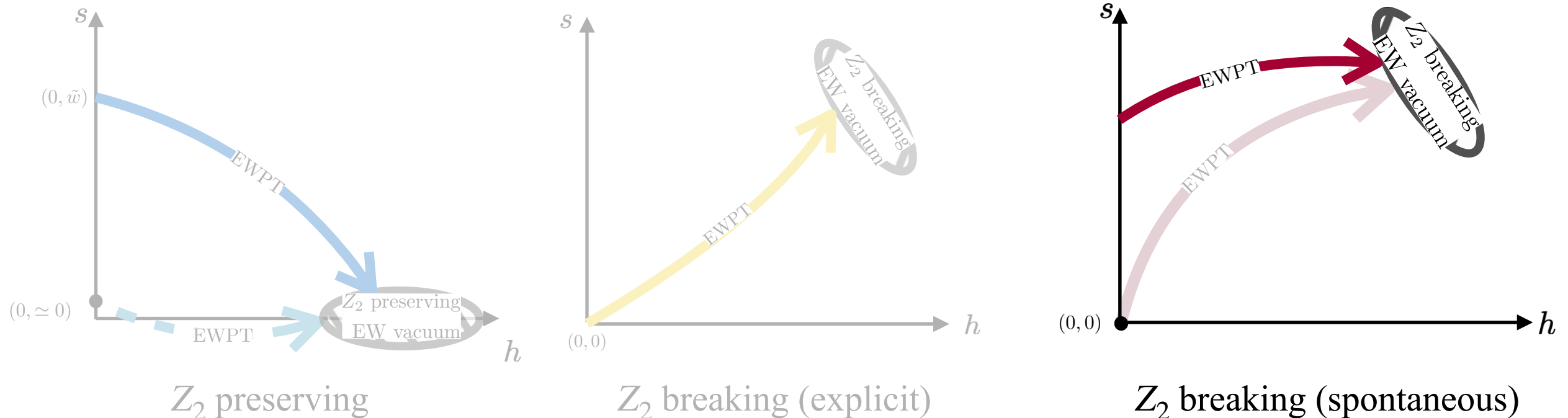
Electroweak phase transition and Higgs properties (at zero T)

$$V_0(h, s) = -\frac{1}{2}\mu_h^2 h^2 + \frac{1}{4}\lambda_h h^4 + \frac{1}{2}\mu_s^2 s^2 + \frac{1}{4}\lambda_s s^4 + \frac{1}{4}\lambda_m h^2 s^2 + (\text{explicit } Z_2 - \text{breaking terms})$$

$$\rightarrow V_{\text{EFF}}(h, s, T)$$

[Carena, et al, 22']

□ Tree-level Effects



Example: Order of the Phase Transition $\propto \left(\lambda_h - \frac{\lambda_m^2}{4\lambda_s} \right)^{-1} \propto 1 + \sin^2 \theta \left(\frac{(125\text{GeV})^2}{m_S^2} - 1 \right)$

- $\sin \theta \lesssim 0.4$ bounded by **Higgs precision measurements**
- A firm prediction of a **light scalar**
- **BR($H \rightarrow SS$) bounded from below**

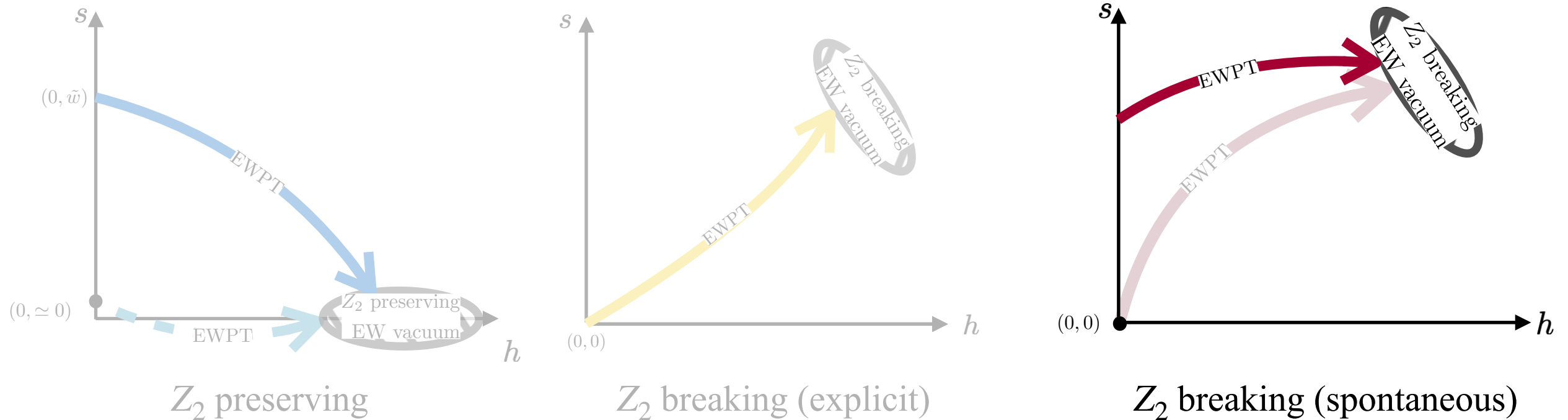
Electroweak phase transition and Higgs properties (at zero T)

$$V_0(h, s) = -\frac{1}{2}\mu_h^2 h^2 + \frac{1}{4}\lambda_h h^4 + \frac{1}{2}\mu_s^2 s^2 + \frac{1}{4}\lambda_s s^4 + \frac{1}{4}\lambda_m h^2 s^2 + (\text{explicit } Z_2 - \text{breaking terms})$$

$$\rightarrow V_{\text{EFF}}(h, s, T)$$

[Carena, et al, 22']

□ Tree-level Effects

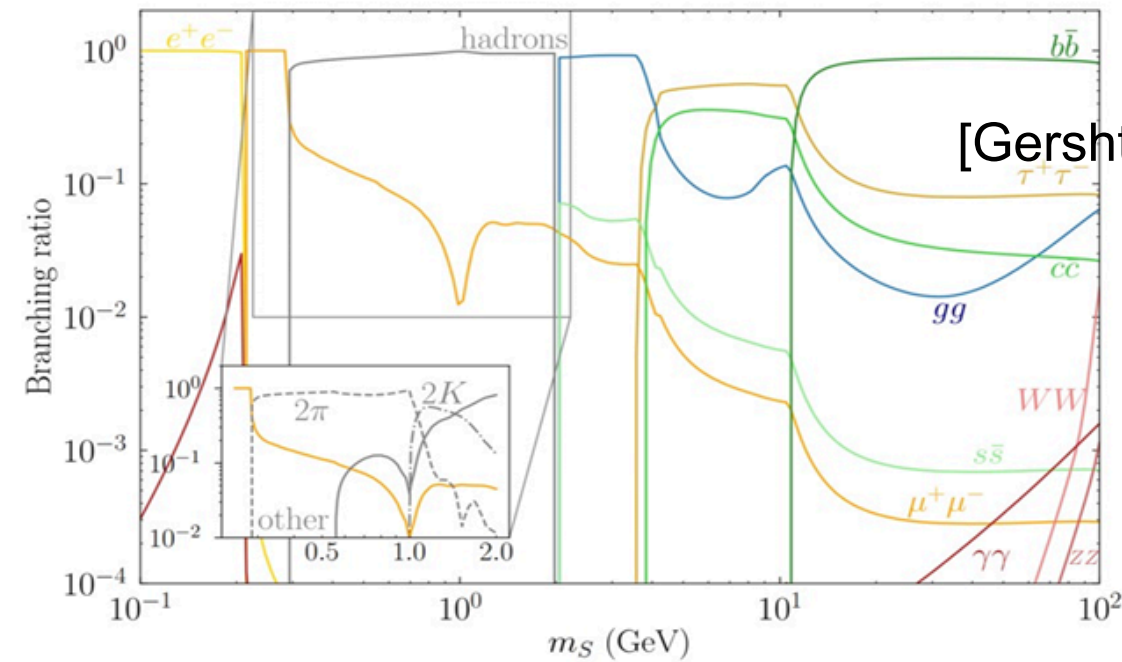
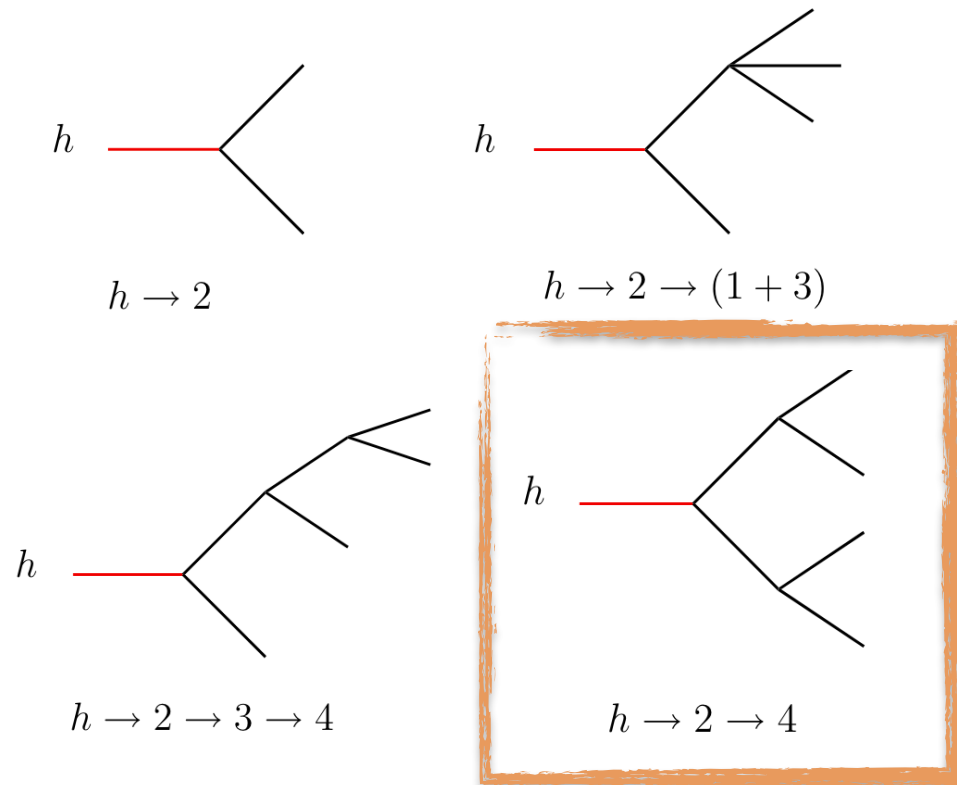


Example: Order of the Phase Transition $\propto \left(\lambda_h - \frac{\lambda_m^2}{4\lambda_s} \right)^{-1} \propto 1 + \sin^2 \theta \left(\frac{(125\text{GeV})^2}{m_S^2} - 1 \right)$

- $\sin \theta \lesssim 0.4$ bounded by **Higgs precision measurements**
- A firm prediction of a **light scalar**
- **BR($H \rightarrow SS$) bounded from below**

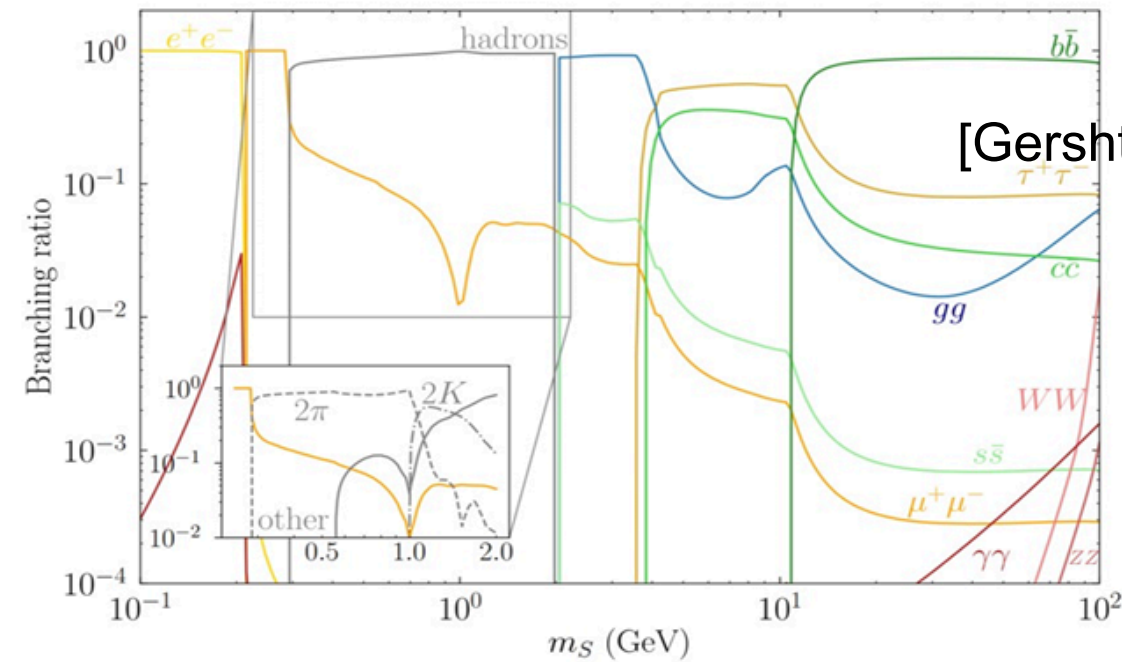
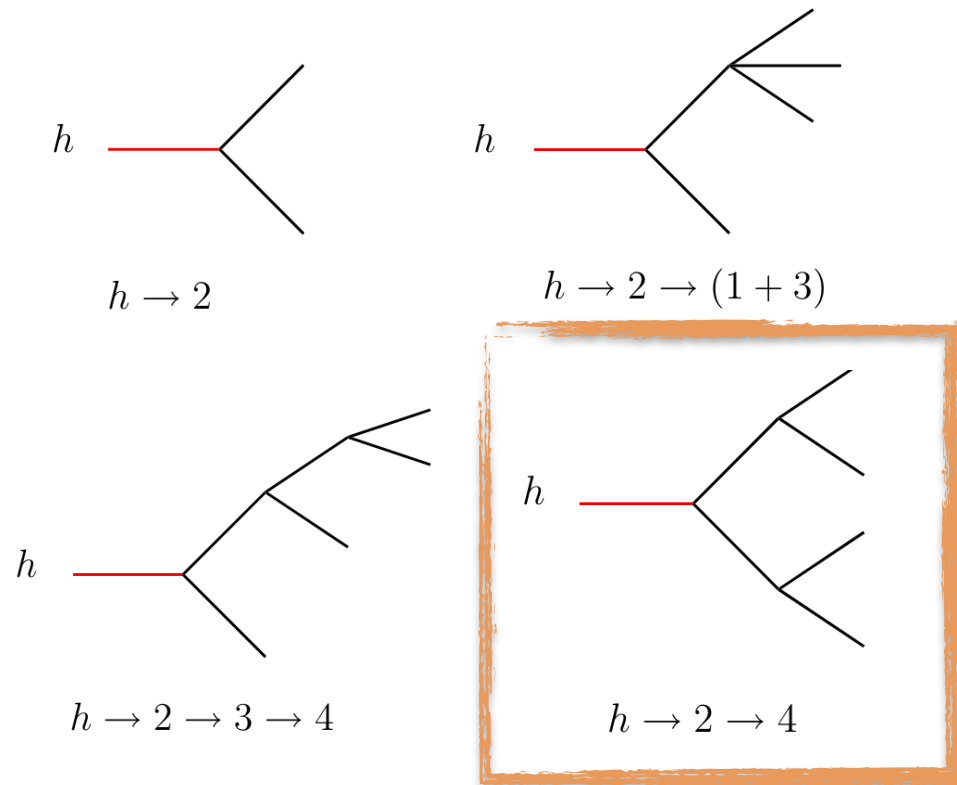
Observation window: Higgs exotic decay

Electroweak phase transition and Higgs Exotic Decays



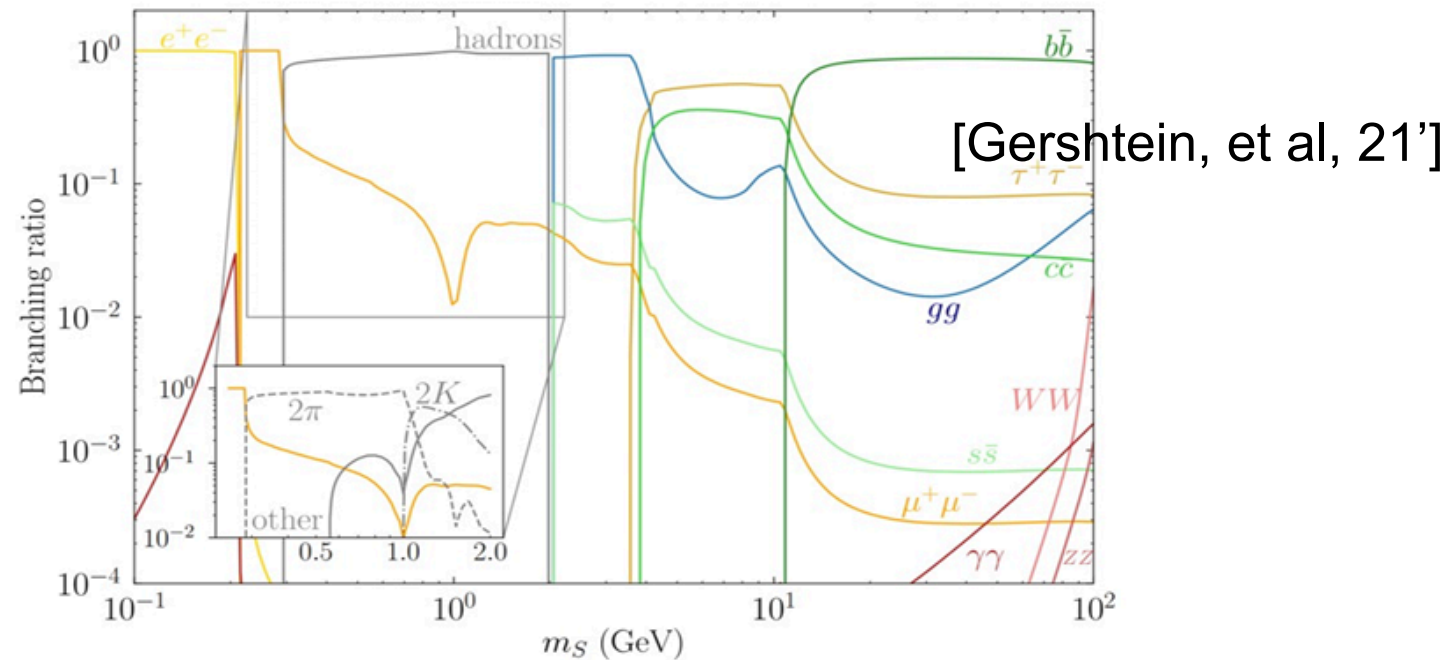
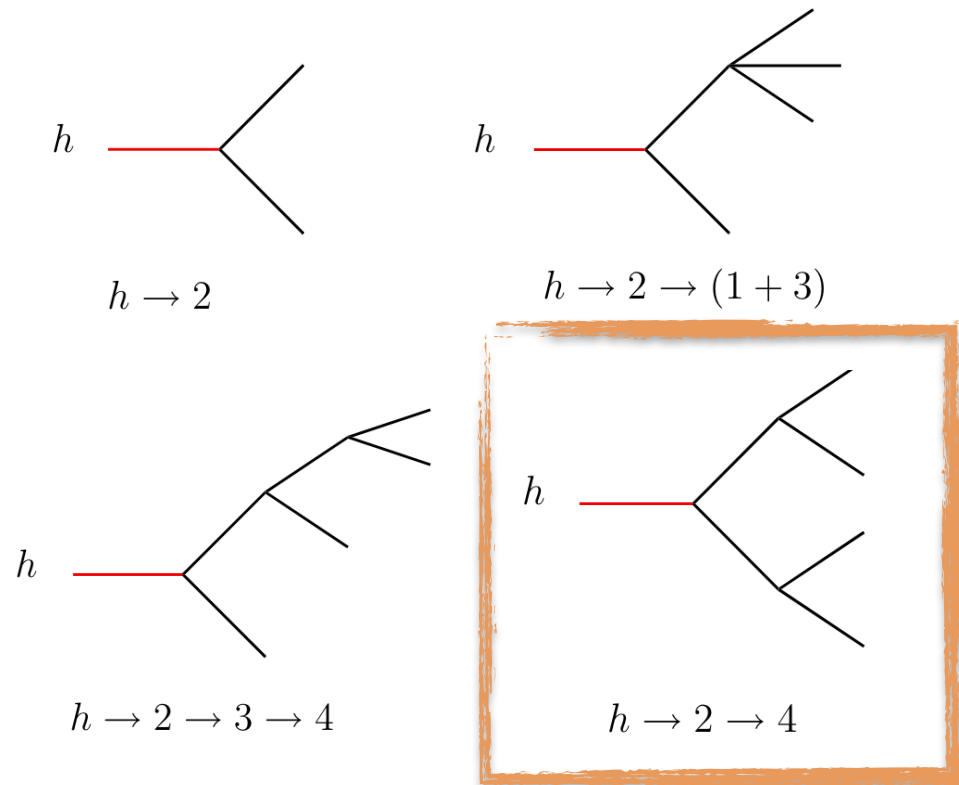
Higgs exotic decay $H \rightarrow SS$ and S branching fraction into $XXYY$ final states mediated through mixing.

Electroweak phase transition and Higgs Exotic Decays

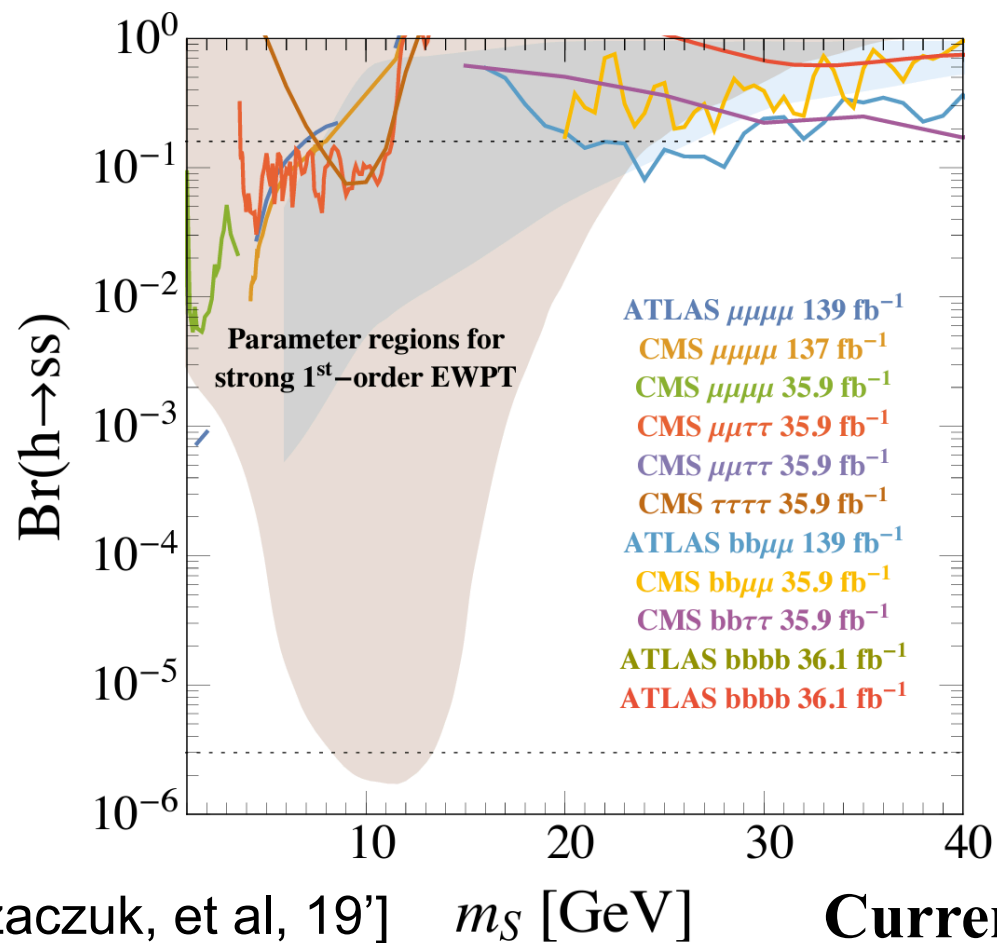


Higgs exotic decay $H \rightarrow SS$ and S branching fraction into $XXYY$ final states mediated through mixing.

Electroweak phase transition and Higgs Exotic Decays

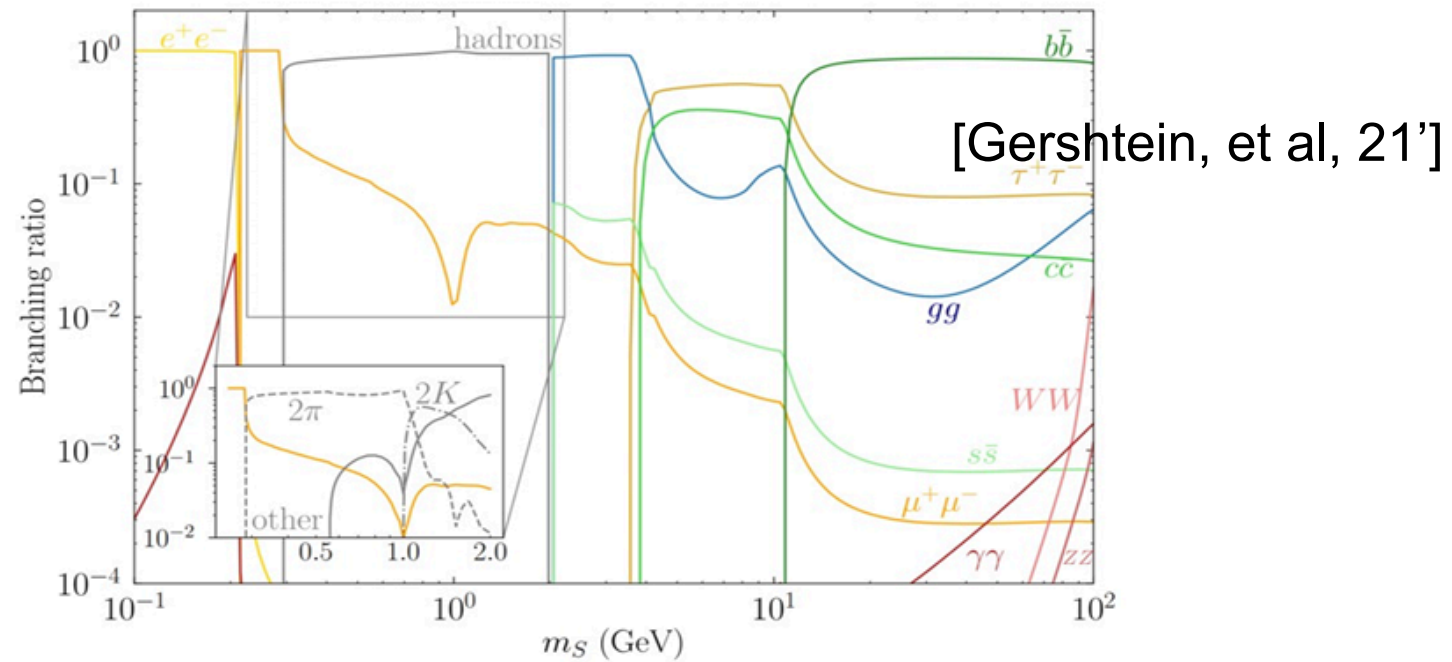
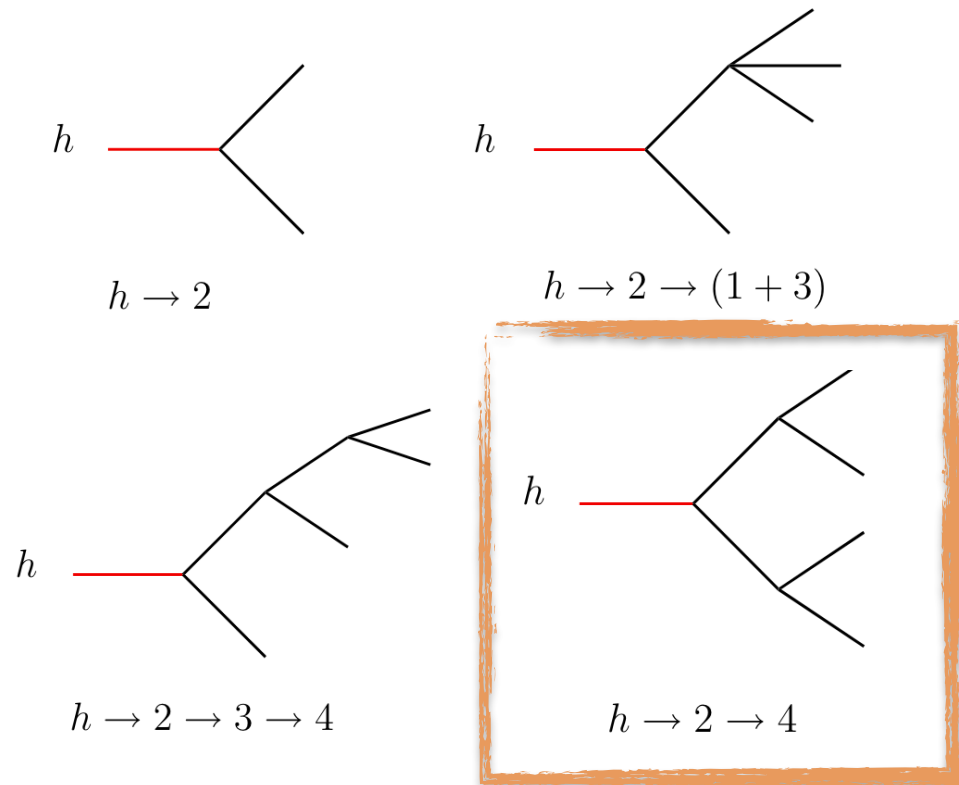


Higgs exotic decay $H \rightarrow SS$ and S branching fraction into $XXYY$ final states mediated through mixing.

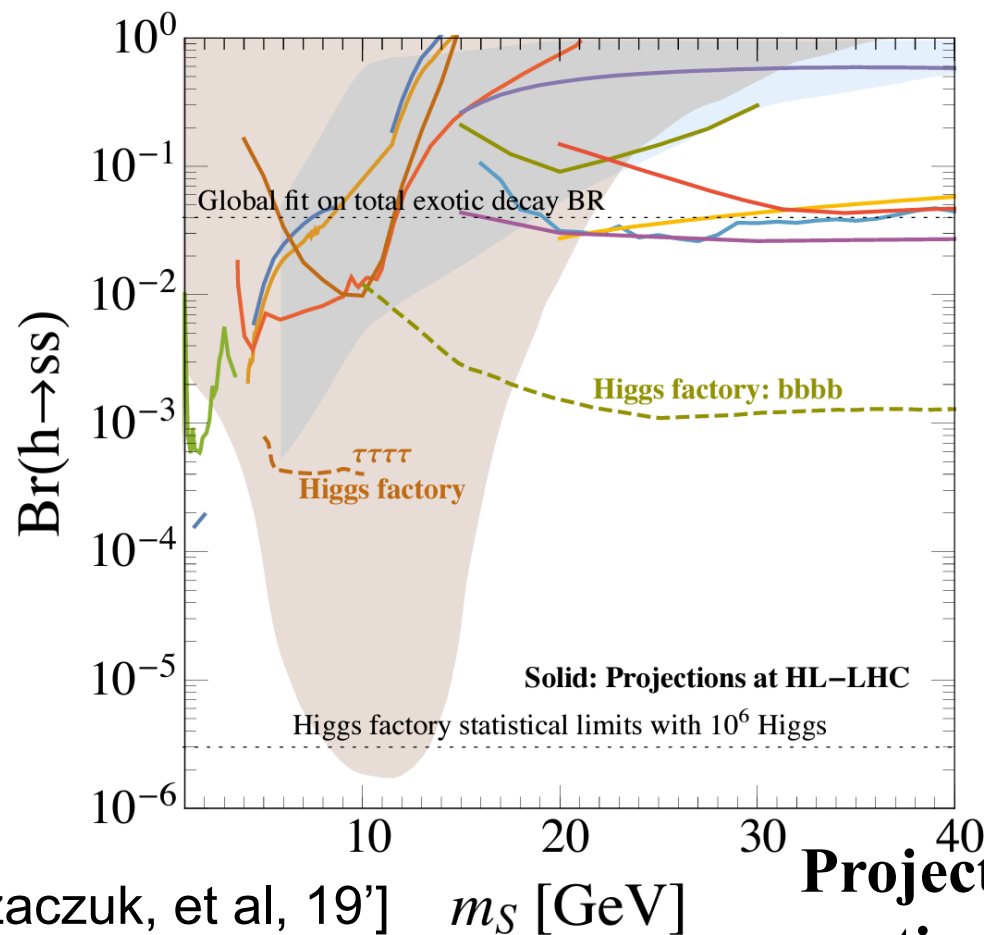


Current bounds on Higgs exotic decay $H \rightarrow SS$

Electroweak phase transition and Higgs Exotic Decays



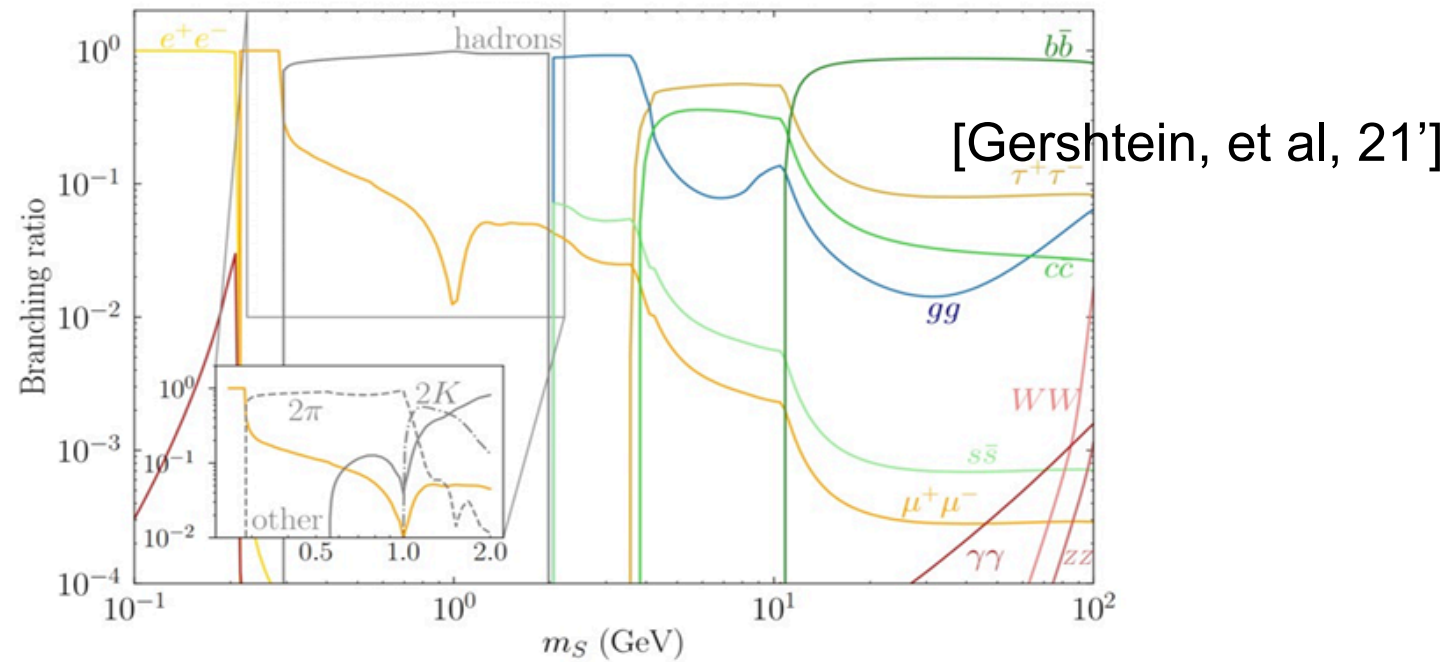
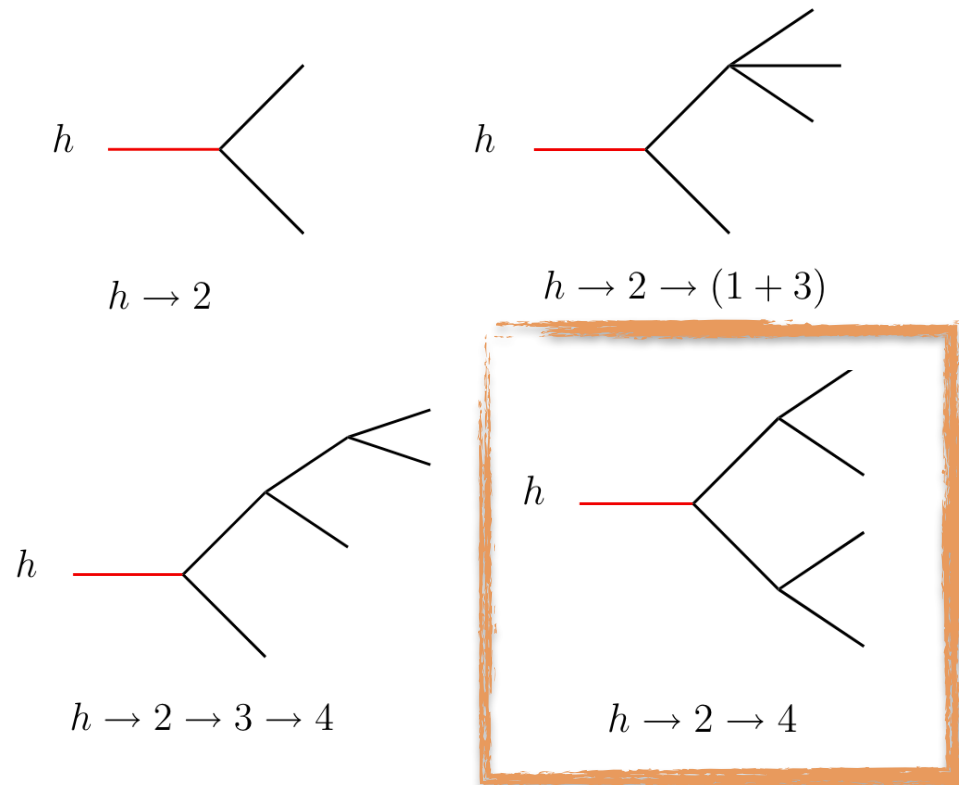
Higgs exotic decay $H \rightarrow SS$ and S branching fraction into $XXYY$ final states mediated through mixing.



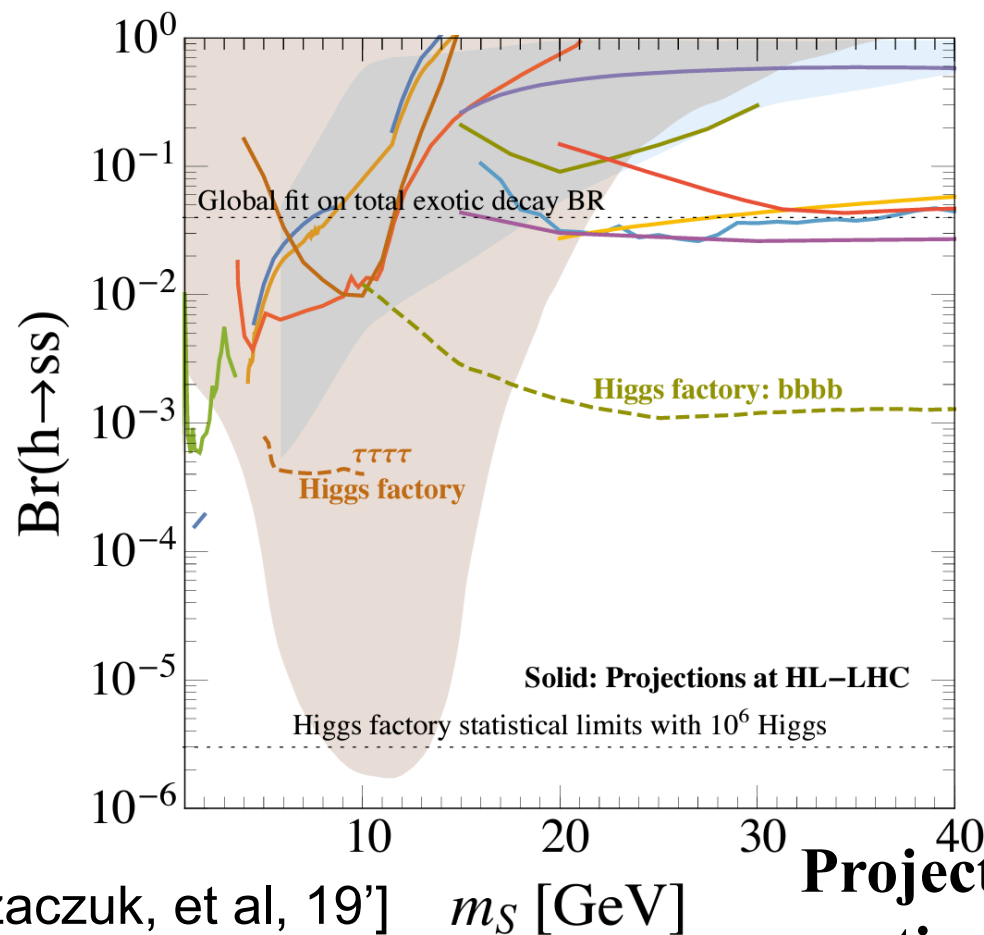
Projections at HL-LHC and Higgs factories on Higgs exotic decay $H \rightarrow SS$

[Kozaczuk, et al, 19']

Electroweak phase transition and Higgs Exotic Decays



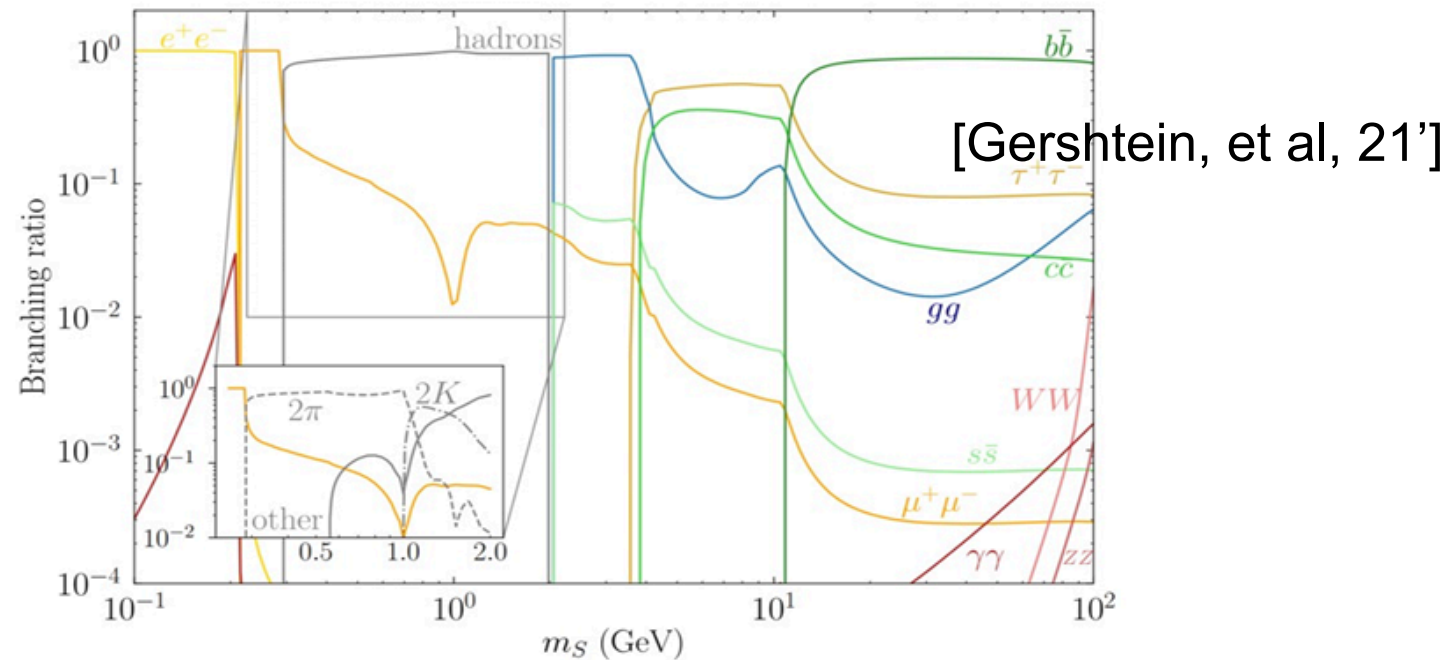
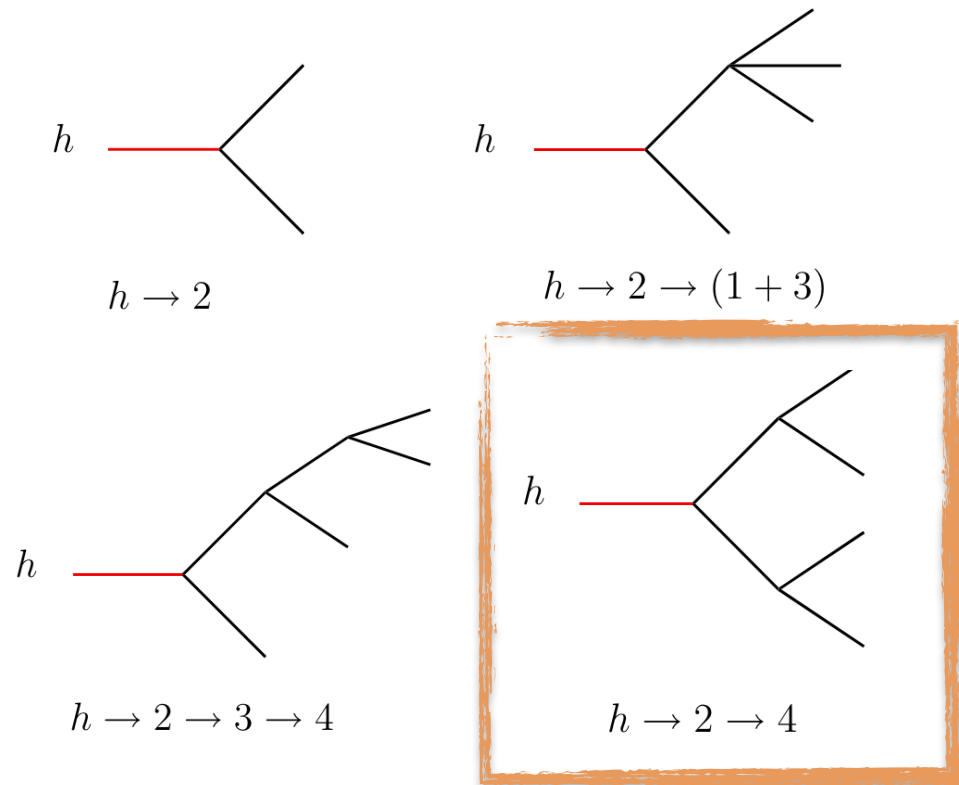
Higgs exotic decay $H \rightarrow SS$ and S branching fraction into $XXYY$ final states mediated through mixing.



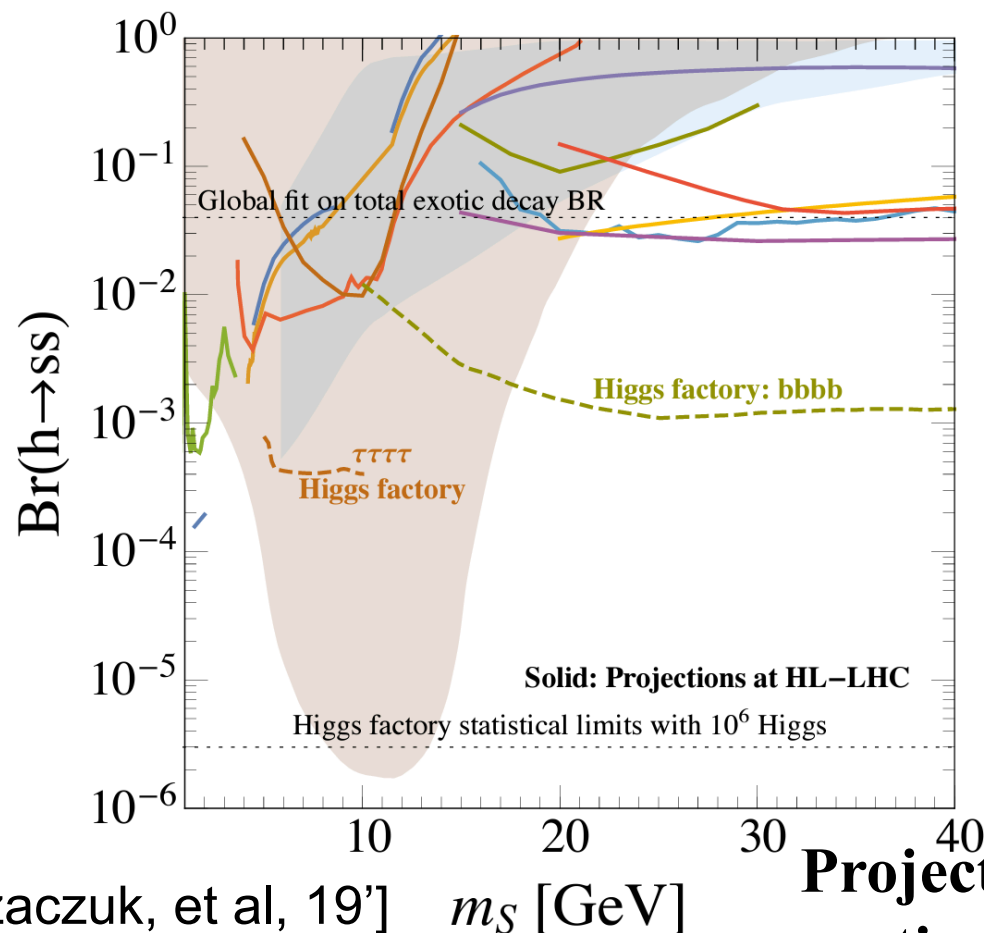
[Kozaczuk, et al, 19'] m_S [GeV]

Projections at HL-LHC and Higgs factories on Higgs exotic decay $H \rightarrow SS$

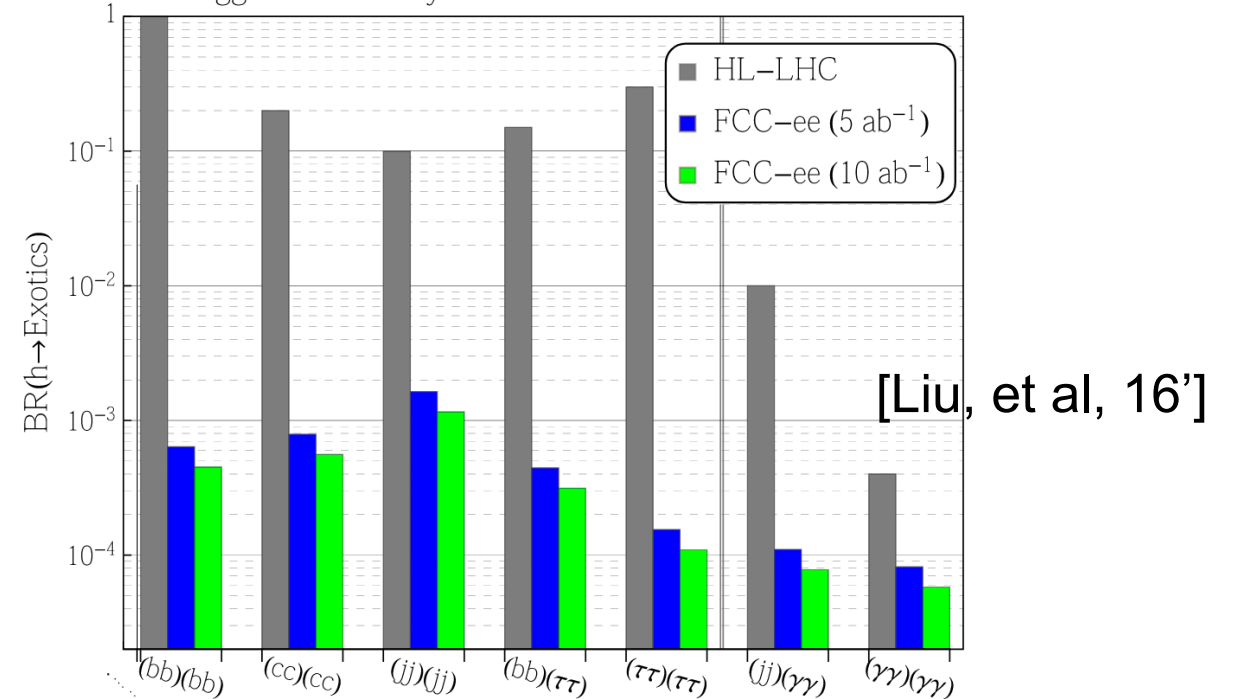
Electroweak phase transition and Higgs Exotic Decays



Higgs exotic decay $H \rightarrow SS$ and S branching fraction into $XXYY$ final states mediated through mixing.



95% C.L. upper limit on selected BRs



Projections at HL-LHC and Higgs factories on Higgs exotic decay $H \rightarrow SS$

[Kozaczuk, et al, 19']

Summary and Outlook

- ▶ An important goal of the Higgs physics is to explore the nature of the Electroweak Phase Transition, and its potential role in BAU generation;
- ▶ Higgs exotic decay is a powerful channel to probe scenarios involving rendering strongly first order Electroweak Phase Transition otherwise inaccessible by other channels;
- ▶ FCC-ee and other Higgs factories can improve the bounds on Higgs exotic decay branching ratios by many orders of magnitude and have the potential to make discoveries in or excluding phenomenologically interesting parameter space;
- ▶ Further theoretical and collider studies are needed: extensions beyond real singlet (complex scalar, doublet, triplet, etc); perturbative convergence for very light scalars; room for improvement; more final states for lighter masses...