



FUTURE
CIRCULAR
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What can we say about the Higgs self-coupling with the hadronic ZH process at FCC-ee?

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Higgs self-coupling

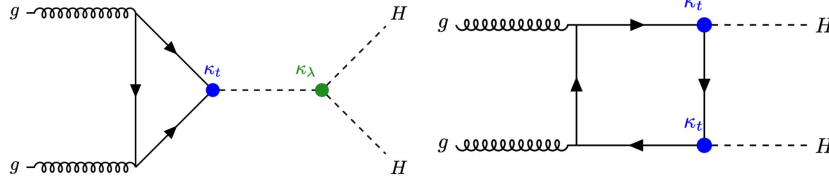
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 - Fundamental test of **SM**, use to search for **BSM**
- Estimated precision at HL-LHC: **~50%** (conservative) w/ **Higgs pair production**



- Estimated precision at FCC-hh: **~5%**

	collider	single- H	HH	combined
●	HL-LHC	100-200%	50%	50%
	CEPC ₂₄₀	49%	–	49%
	ILC ₂₅₀	49%	–	49%
●	ILC ₅₀₀	38%	27%	22%
●	ILC ₁₀₀₀	36%	10%	10%
	CLIC ₃₈₀	50%	–	50%
	CLIC ₁₅₀₀	49%	36%	29%
●	CLIC ₃₀₀₀	49%	9%	9%
	FCC-ee	33%	–	33%
●	FCC-ee (4 IPs)	24%	–	24%
	HE-LHC	–	15%	15%
●	* FCC-hh	–	5%	5%

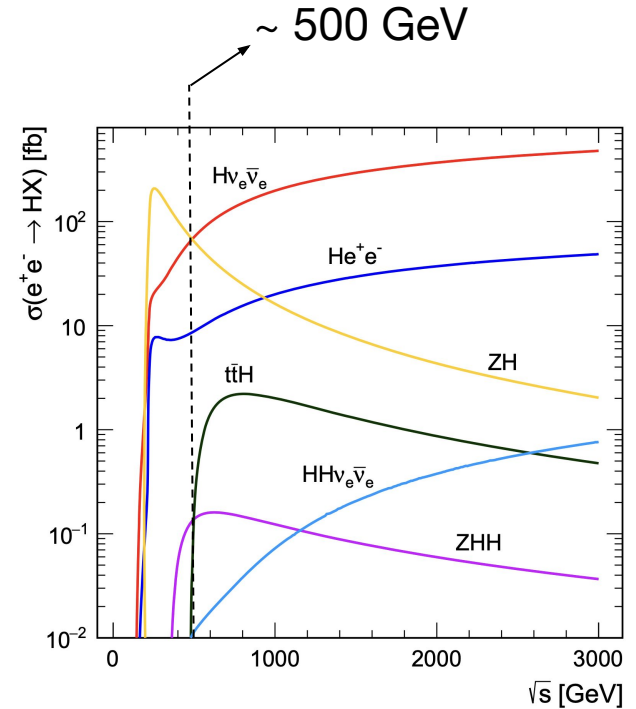
These values are combined with an independent determination of the self-coupling with uncertainty 50% from the HL-LHC.

Sally Dawson, Caterina Vernieri @ [LHC Higgs Working Group](#), December 3, 2021

* arXiv:2004.03505 2.9-5.5%
depending on the systematic assumptions

Self-coupling access at FCC-ee

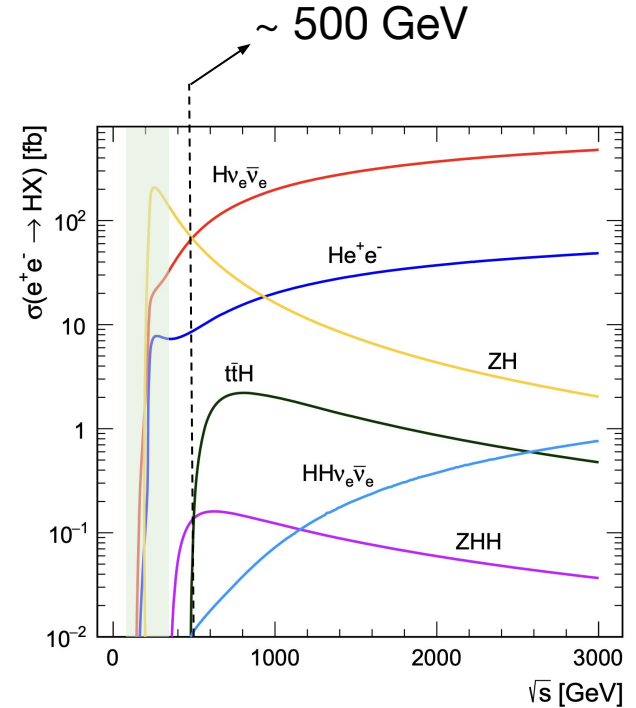
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 - Even higher for **HH $\nu\nu$**



[σ vs. √s, including HH](#)

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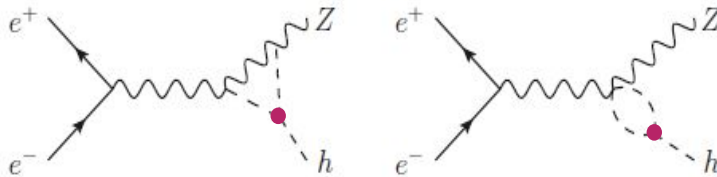
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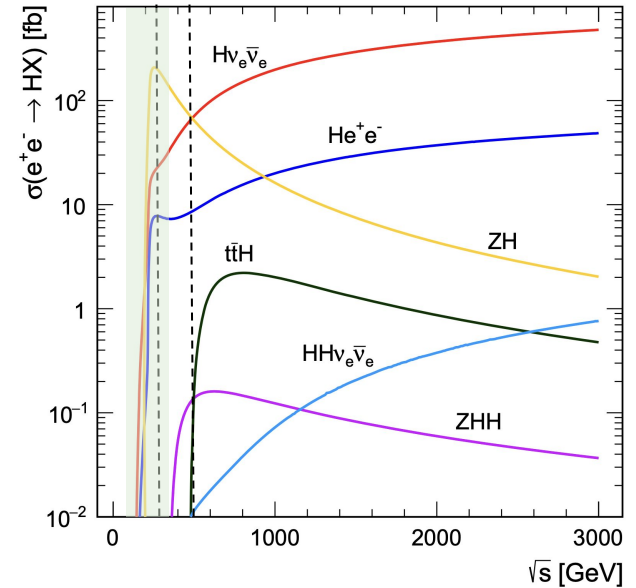
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- Indirect sensitivity from **higher order** contributions to **ZH** (main production mode)



~ 240 GeV ~ 500 GeV



[σ vs. √s, including HH](#)

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H(bb, cc, gg, ss, $\tau\tau$, WW, Zy, ZZ)
q = (u, d)

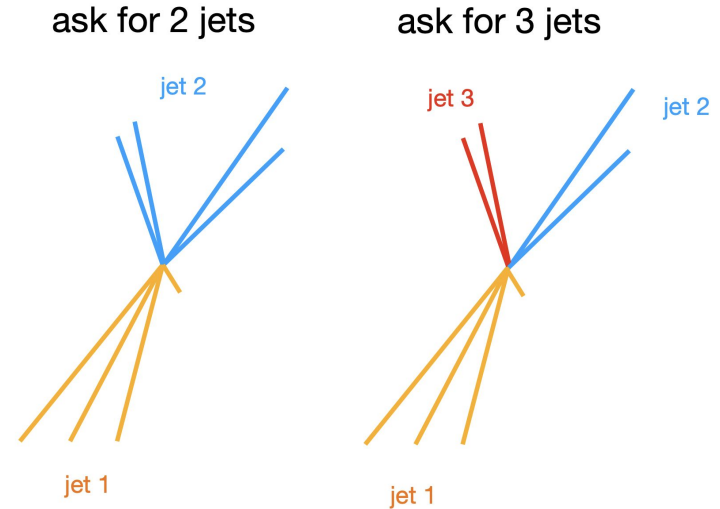
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Durham kt algorithm, require **4 jets**



Same event,
two interpretations!

Selections

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- $N_{\text{jets}} == 4, \leq 2$ leptons \rightarrow **Select expected final state particles**
- Selections on clustering distance parameter: \longrightarrow
- For each **jet**, **tag** flavor based on highest **ParticleNet** flavor score among **{b, c, s, d, u, g, τ }**
 - Ignore events with 4 different flavor tagged jets (small percentage)

Parameter [GeV] ²	min	max
d_{12}	15000	58000
d_{23}	400	18000
d_{34}	100	6000

$$\sqrt{(m_{z_{jj}} - m_W)^2 + (m_{H_{jj}} - m_W)^2} > 10, \sqrt{(m_{z_{jj}} - m_Z)^2 + (m_{H_{jj}} - m_Z)^2} > 10$$

Remove WW
Remove ZZ

- $50 < m_{z_{jj}} < 125$ GeV, $m_{H_{jj}} > 91$ GeV \rightarrow **Minimize H/Z faking Z/H**

Categorization

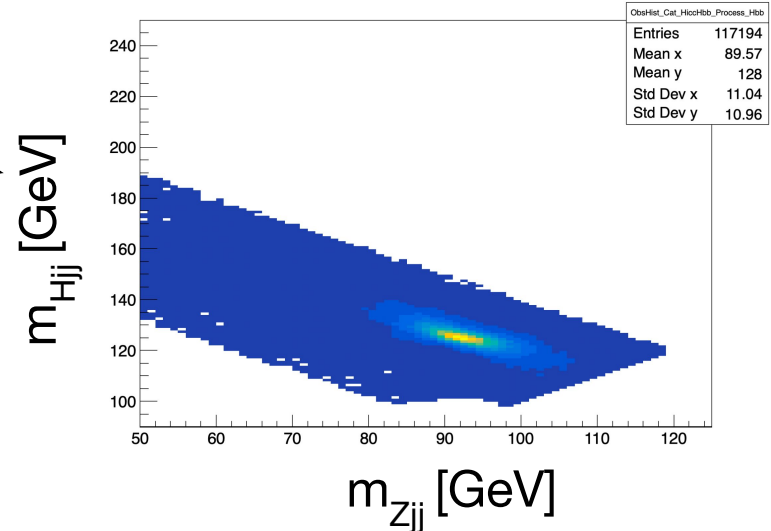
- Categorize events by **pair flavor scores** with different purity categories

	bb, cc, gg	ss
Low	< 1.1	< 0.8
Medium	[1.1, 1.8]	[0.8, 1.4]
High	> 1.8	> 1.4

Categorization

- Categorize events by **pair flavor scores** with different purity categories
- Example: H_{bb} process reco Higgs mass vs. reco Z mass
- Aim to maximize signal over background near Higgs, Z mass peaks

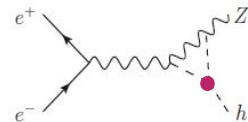
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Self-coupling scan

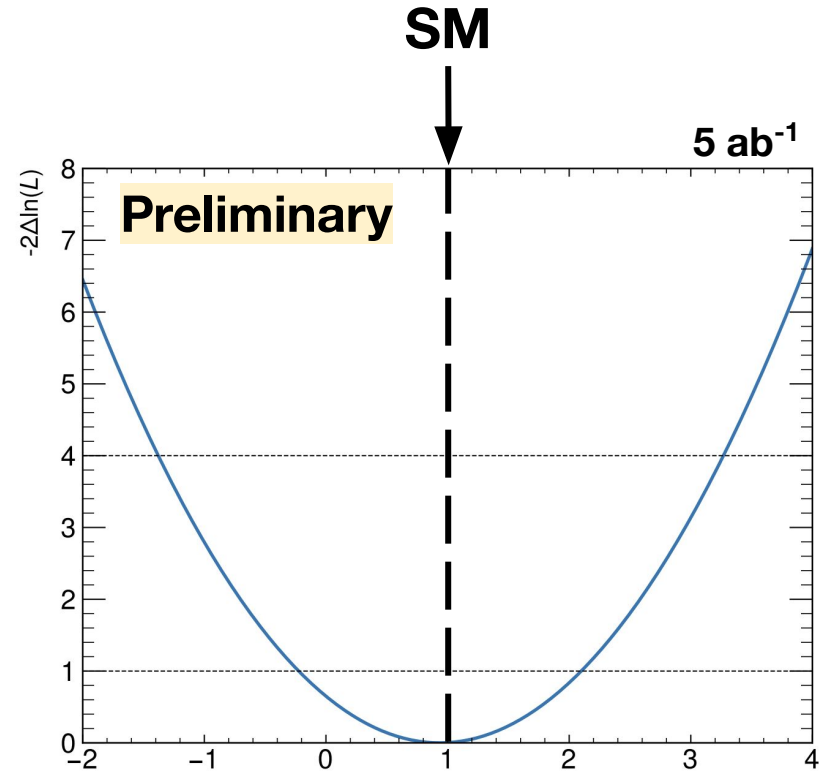
- For each κ_λ ($\lambda / \lambda_{\text{SM}}$) value:
 - Scale ZH signal strength
 - Compute **likelihood**

$$\kappa_\lambda = \lambda / \lambda_{\text{SM}}$$

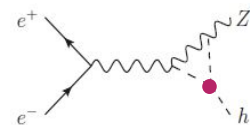


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- Evaluate **1 σ constraint** on self-coupling as **intersect points at 1**
- **Initial** result: $\kappa_\lambda \in [0.2, 2.1]$ at 1σ

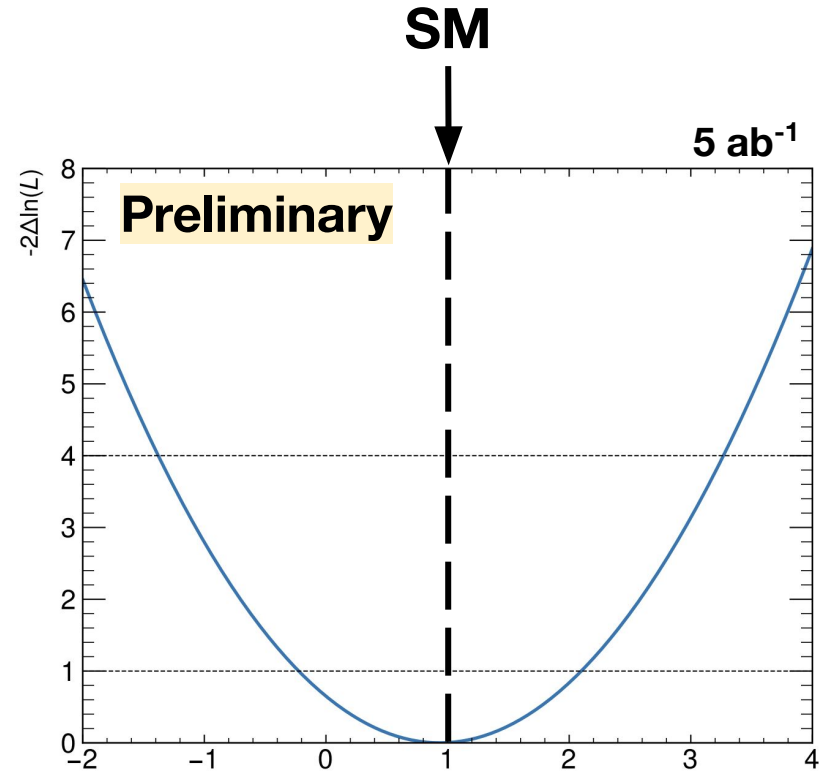


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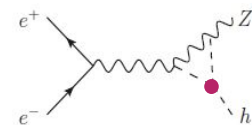
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- Expect to improve with additional selections, can use as **benchmark for detector optimization**



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κ_λ

Summary

- **The Higgs self-coupling can be measured indirectly at the FCC-ee, hopefully with higher precision than at the HL-LHC**
 - This measurement depends on defining a high sensitivity phase space, using data from runs at several center-of-mass energies

Summary

- **The Higgs self-coupling can be measured indirectly at the FCC-ee, hopefully with higher precision than at the HL-LHC**
 - This measurement depends on defining a high sensitivity phase space, using data from runs at several center-of-mass energies
- Use **Fully-Hadronic ZH** process, **flavor tagging** [\[ref.\]](#), obtains expected self-coupling constraint
 - $\kappa_\lambda \in [0.2, 2.1]$ → To be improved with further selections
 - **Will use as benchmark for detector optimization studies**
 - Can combine with $Z(\ell\ell)H$ final states for more sensitive result
 - Also investigating optimal **jet reclustering method** → See [Phil's talk](#)

Backup

Exclusive Durham k_t algorithm

[M. Cacciari, G. Salam G. Soyez](#)

- Combine low energy particles with neighbors
- Reiterate until you reach d_{cut} or n_{jets}

Simplest all-round decent e^+e^- algorithm the “exclusive” Durham k_t algorithm

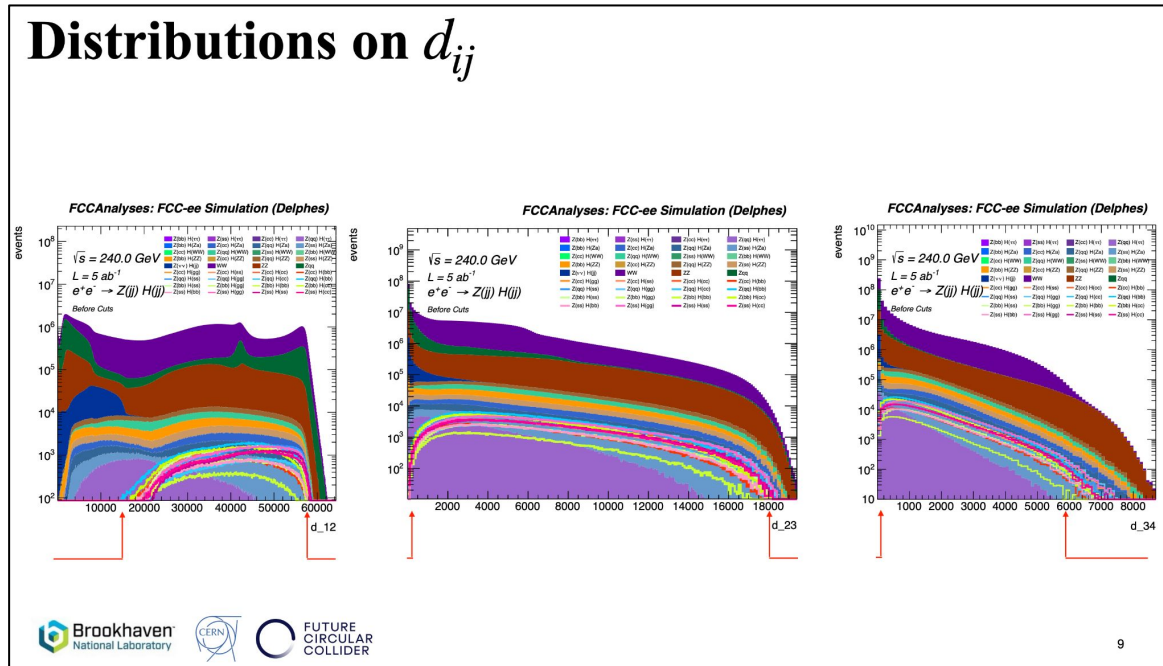
- determine $d_{ij} = 2 \min(E_i^2, E_j^2)(1 - \cos \theta_{ij})$ between each pair of particles i, j
- recombine i, j pair with smallest d_{ij} , and update all distances
- stop when:
 - n_{jets} mode.** you have reached a predetermined number of jets (e.g. $n = 4$ for $ZH \rightarrow q\bar{q}b\bar{b}$)
 - d_{cut} mode.** all remaining $d_{ij} >$ some threshold (called d_{cut})

In “ n_{jets} mode”, you often want to look at what the next d_{ij} *would* have been and discard the event if it is below some threshold. **Simple and effective.**

In “ d_{cut} mode”, you usually make sure you have at least n jets for your process (e.g. 4 for $ZH \rightarrow q\bar{q}b\bar{b}$), otherwise discard the event. If you have more than n jets, decide whether to keep the event, and if so which jets to use.

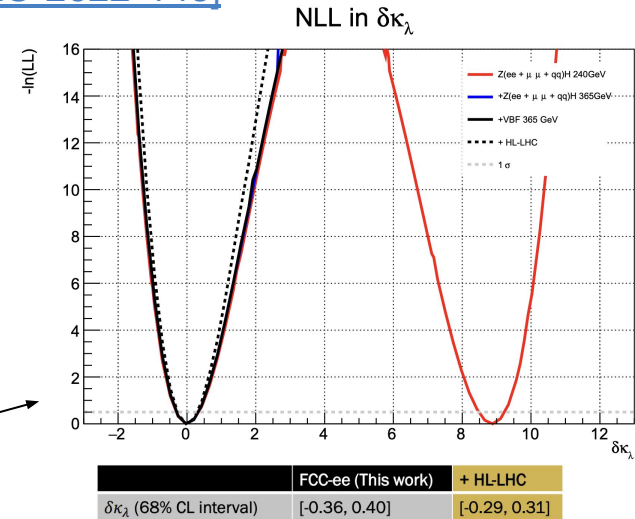
d_{ij} distributions from similar analysis

Slide from [George Iakovidis](#):



Existing hadronic ZH analysis

- **Extensive ZH analysis performed (240 and 365 GeV):**
 - FCC physics performance meeting: [\[17 October 2022 - Nico Härringer\]](#)
 - Documented as masters thesis: [\[CERN-THESIS-2022-143\]](#)
- Targets **leptonic** and **hadronic** Z decays, inclusive Higgs decays, VBF-H
- **Cut based** and **BDT based** analysis (depending on production mode / final state)
- Projected FCC-ee results include:
 - Higgs **mass** measurement
 - ZH, VBFH production **cross-section** measurements
 - **Self-coupling constraint**



κ_λ constraint - including **240** and **365 GeV** categories
(other parameters **fixed** to SM values)

Cross section parameterization

- Cross section parameterization as a function of k_l

$$\sigma_{i,\text{NLO}} = Z_H \sigma_{i,\text{LO}} (1 + \kappa_\lambda C_{1,i}),$$

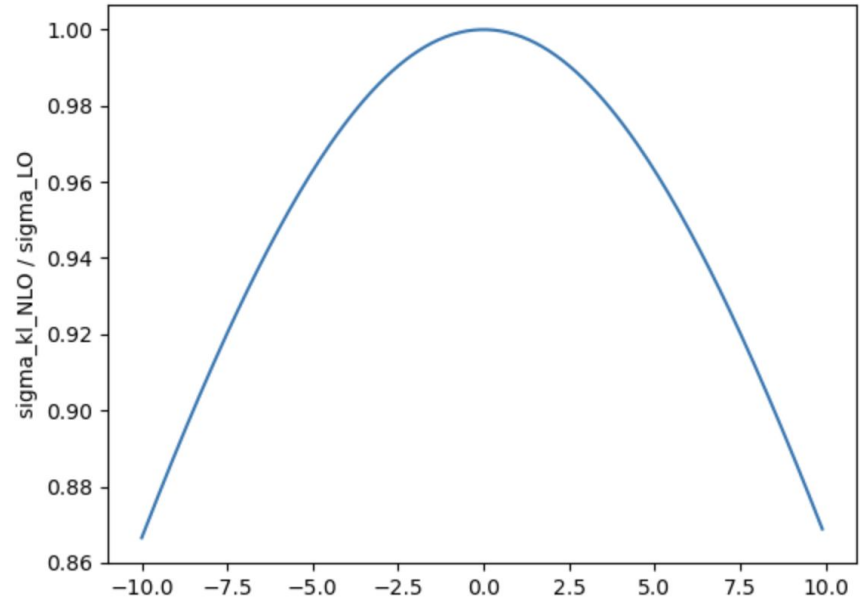
$$Z_H = \frac{1}{1 - \kappa_\lambda^2 \delta Z_H},$$

$$\delta Z_H = -\frac{9}{16} \frac{G_F m_H^2}{\sqrt{2} \pi^2} \left(\frac{2\pi}{3\sqrt{3}} - 1 \right) \approx -0.00154.$$

Equations from Nico Härringer's masters thesis:
[\[CERN-THESIS-2022-143\]](#)

σ_{kl}

- ZH(bb) NLO/LO cross-section as a function of $\delta(\kappa_\lambda)$
- Cross-section falls off, leads to changing likelihood.



$$\delta(\kappa_\lambda) = 1 - \kappa_\lambda \text{ (SM} = 0\text{)}$$

How to measure the Higgs self-coupling at the FCC-ee?

- The self-coupling measurement depends on measurements of Higgs production cross sections and decays to other particles.
- The κ analysis is expected to reach $\sim 20\%$ accuracy [[arXiv:1905.03764](https://arxiv.org/abs/1905.03764)], while the global effective field theory fit will reach $\sim 30\%$ [[arXiv:1711.03978](https://arxiv.org/abs/1711.03978)] (in combination with HL-LHC projections!)
- The ZH cross section (240 GeV run) is most sensitive to changes in the self-coupling
 - 365 GeV run is crucial for reducing uncertainties!

